

CS50 for JDs

cs50.harvard.edu/hls

Algorithms, Data Structures

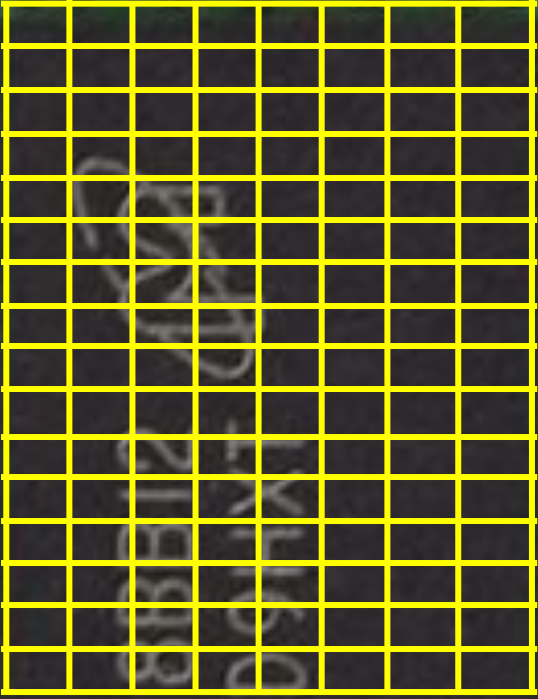
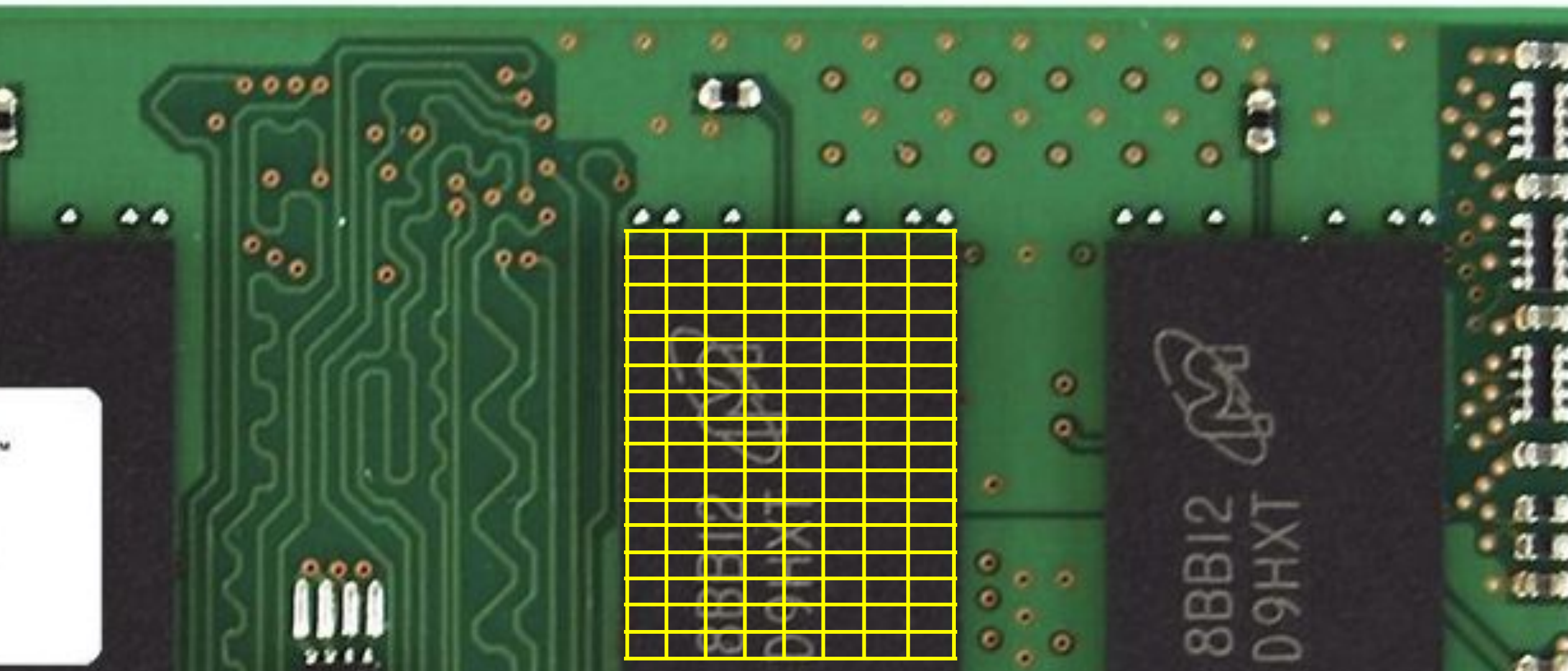


8BB12
D9HXT

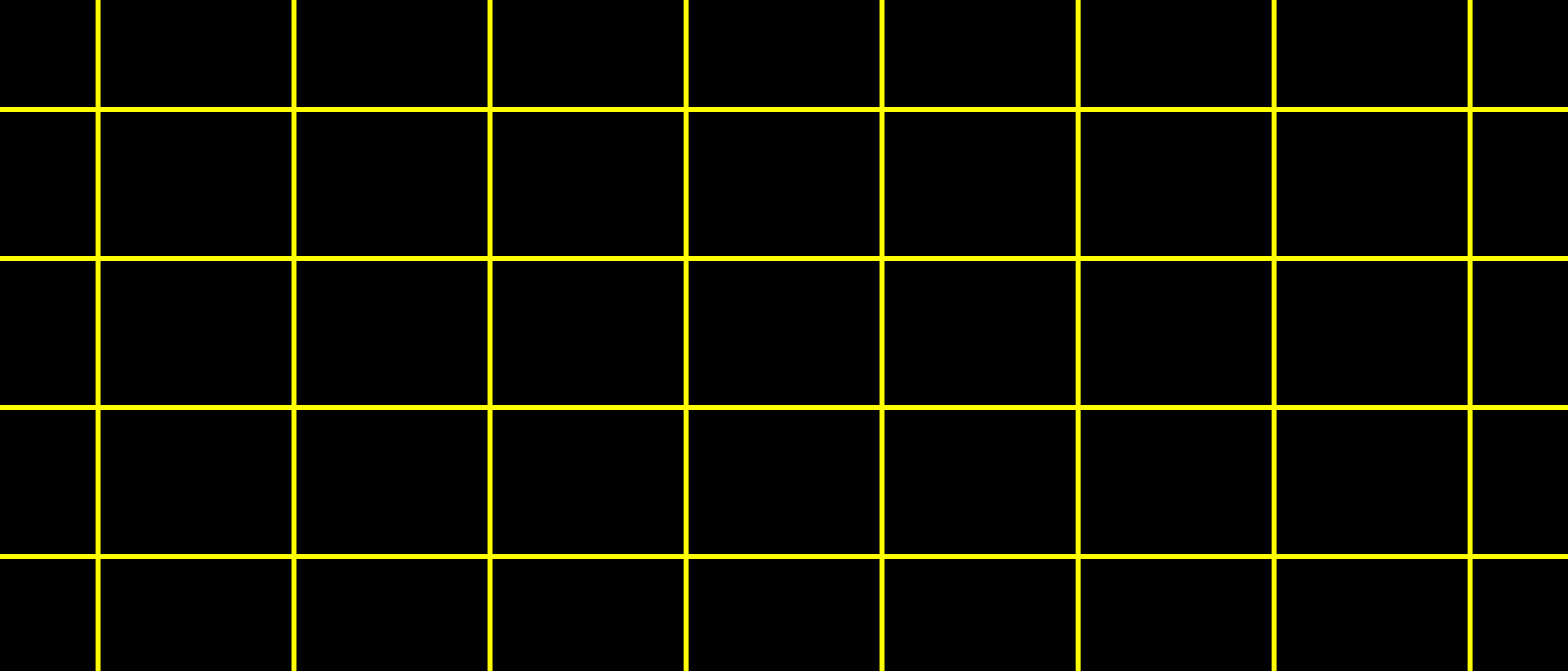


8BB12
D9HXT

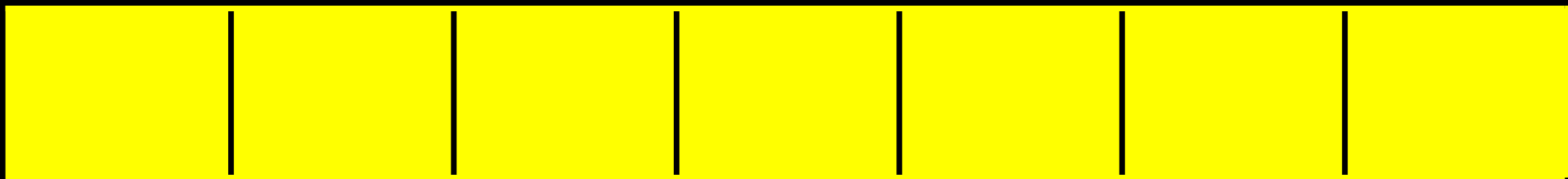




8BB12
D9HXT







arrays

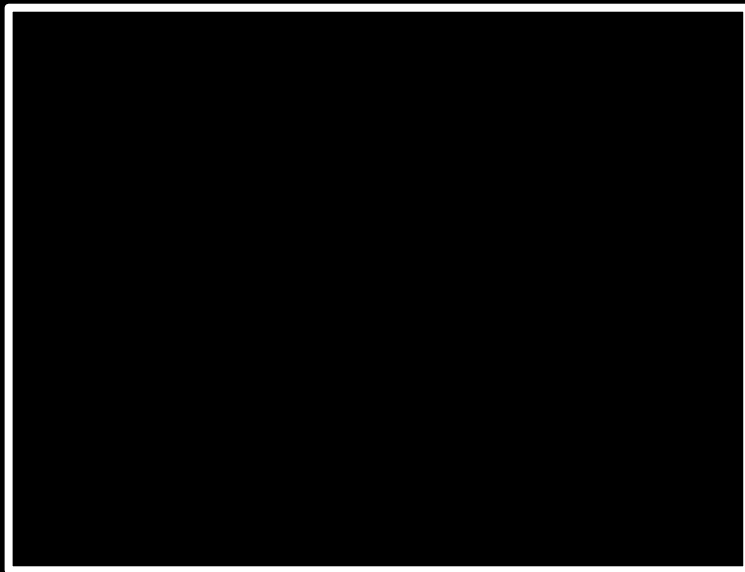
input →



→ output



→ output



bool



algorithms

linear search

```
For i from 0 to n-1
  If i'th element is 50
    Return true
Return false
```

binary search


```
If middle item is 50
```

```
    Return true
```

```
Else if 50 < middle item
```

```
    Search left half
```

```
Else if 50 > middle item
```

```
    Search right half
```

If no items

 Return false

If middle item is 50

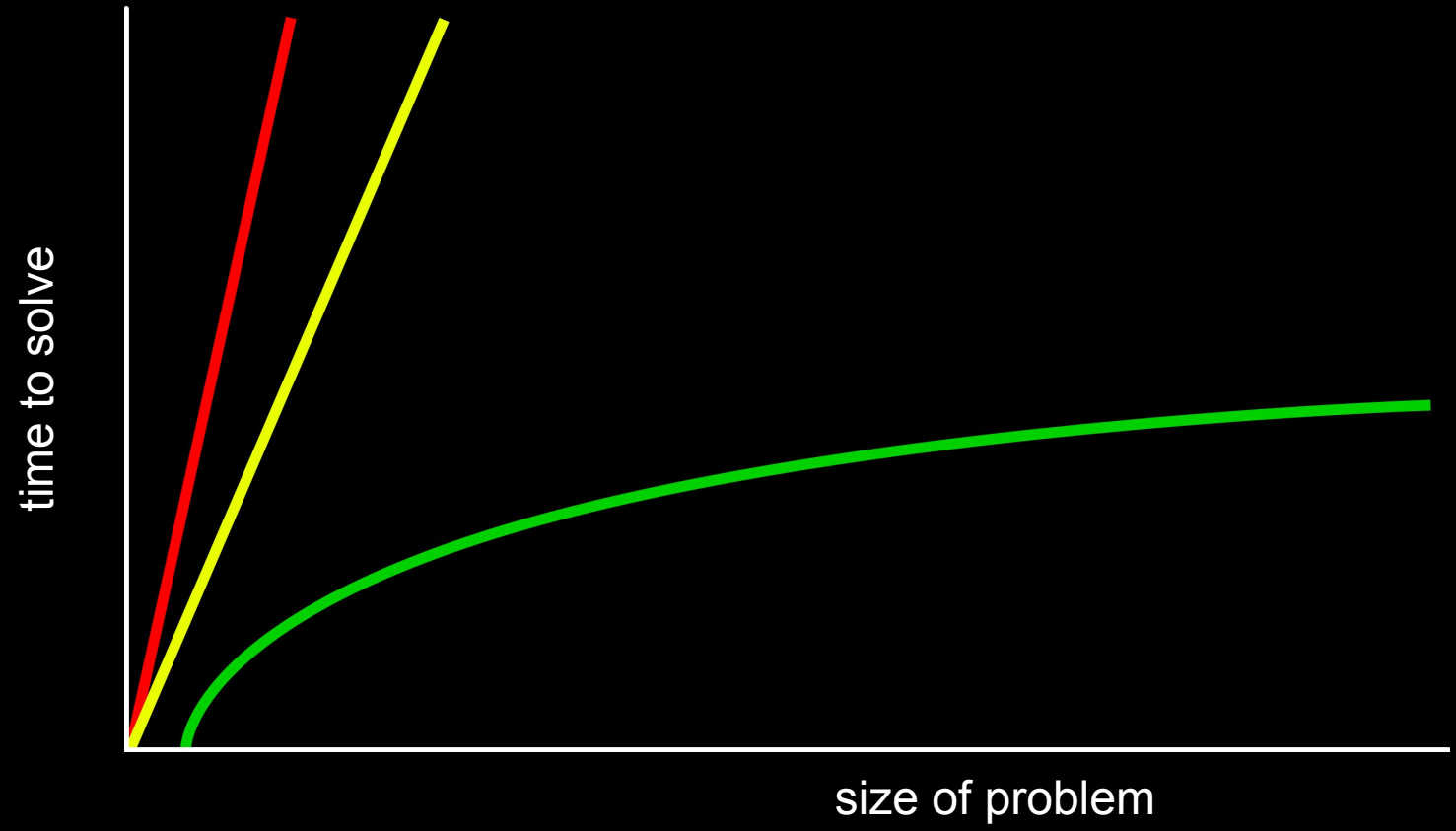
 Return true

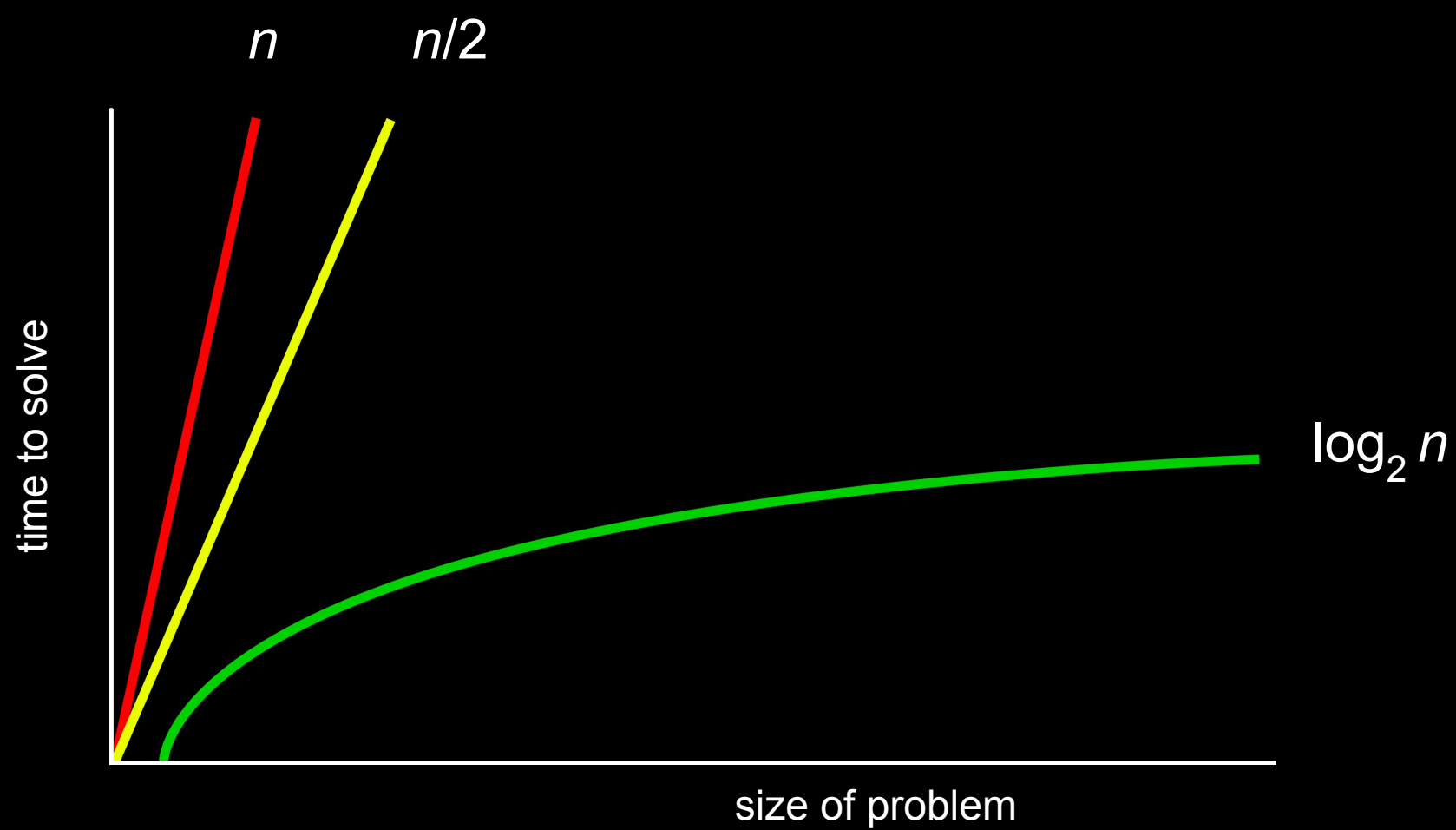
Else if $50 < \text{middle item}$

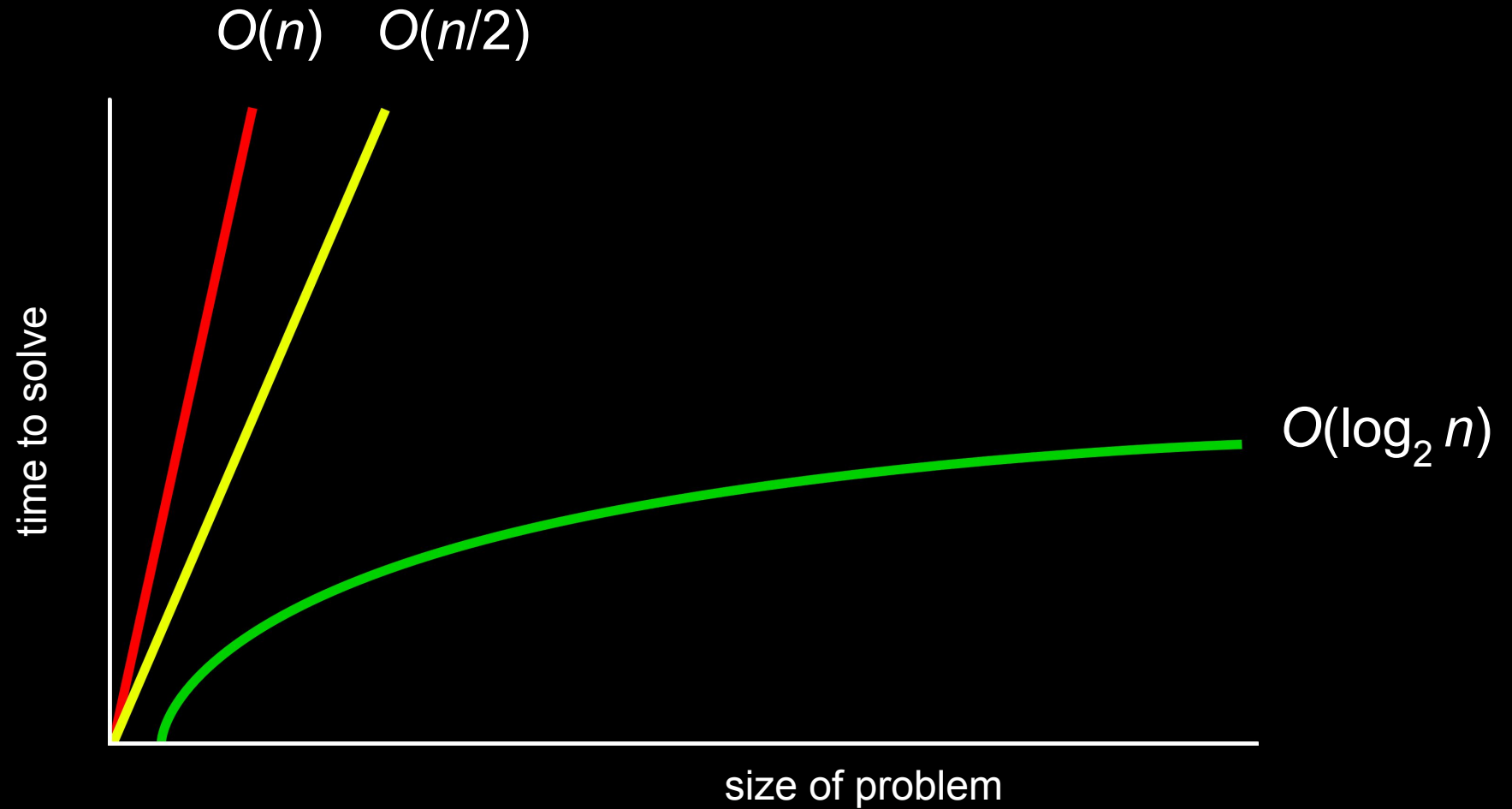
 Search left half

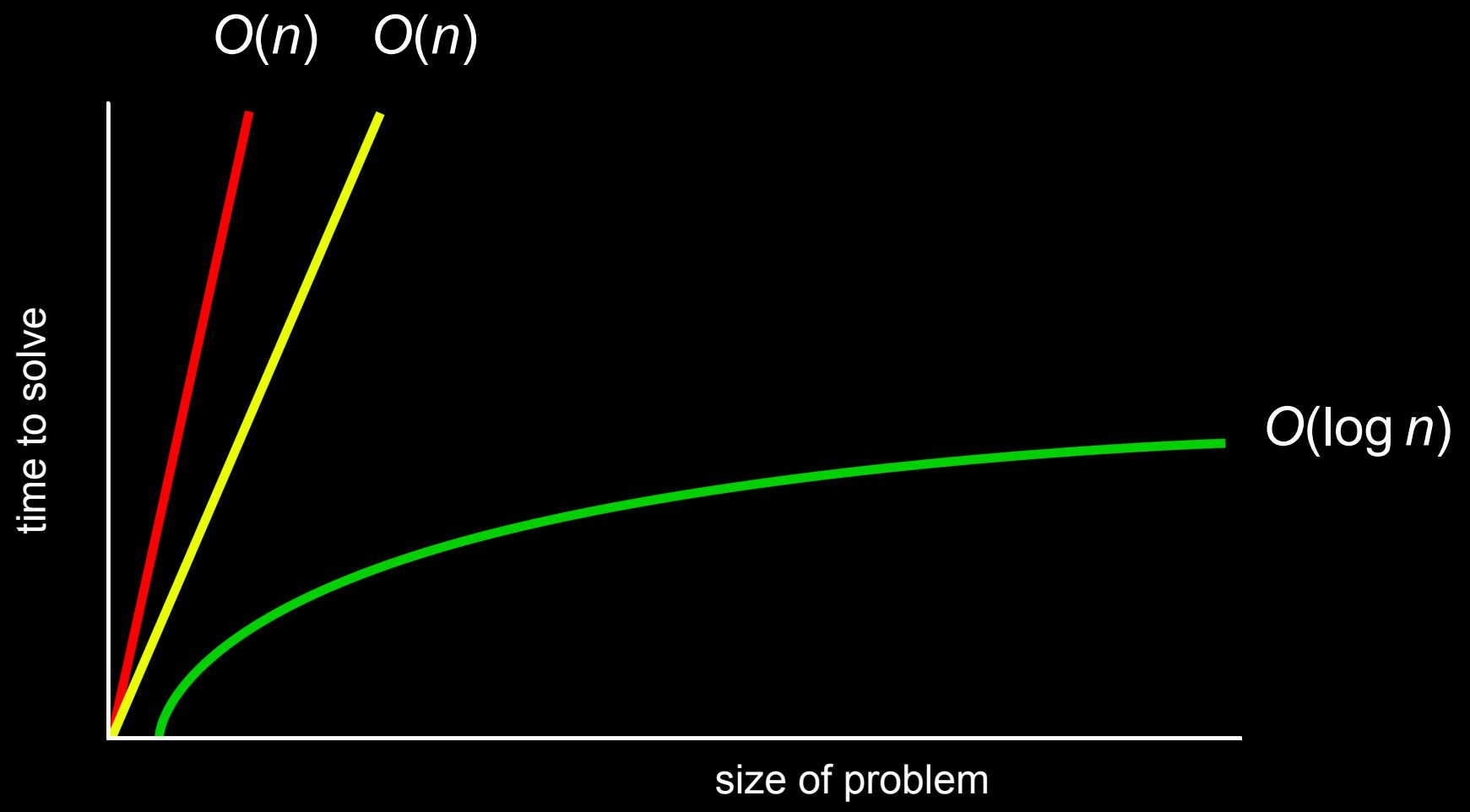
Else if $50 > \text{middle item}$

 Search right half









$O(n^2)$

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$O(n^2)$

$O(n \log n)$

$O(n)$ linear search

$O(\log n)$ binary search

$O(1)$

$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$ linear search, binary search

input →



→ output

unsorted →



→ output

unsorted →



→ sorted

7 2 1 6 3 4 50



→ sorted

6 3 8 5 2 7 4 1

bubble sort

Repeat $n-1$ times

 For i from 0 to $n-2$

 If i 'th and $i+1$ 'th elements out of order

 Swap them

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$

$$O(n^2)$$

$O(n^2)$ bubble sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$ bubble sort

$\Omega(\log n)$

$\Omega(1)$

selection sort

For i from 0 to $n-1$

 Find smallest item between i 'th item and last item

 Swap smallest item with i 'th item

$$n + (n - 1)$$

$$n + (n - 1) + (n - 2)$$

$$n + (n - 1) + (n - 2) + \dots + 1$$

$$n + (n - 1) + (n - 2) + \dots + 1$$

$$n(n + 1)/2$$

$$n + (n - 1) + (n - 2) + \dots + 1$$

$$n(n + 1)/2$$

$$(n^2 + n)/2$$

$$n + (n - 1) + (n - 2) + \dots + 1$$

$$n(n + 1)/2$$

$$(n^2 + n)/2$$

$$n^2/2 + n/2$$

$$n + (n - 1) + (n - 2) + \dots + 1$$

$$n(n + 1)/2$$

$$(n^2 + n)/2$$

$$n^2/2 + n/2$$

$$O(n^2)$$

$O(n^2)$ selection sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$\Omega(n^2)$ selection sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

bubble sort

Repeat $n-1$ times

 For i from 0 to $n-2$

 If i 'th and $i+1$ 'th elements out of order

 Swap them

Repeat until no swaps

 For i from 0 to $n-2$

 If i 'th and $i+1$ 'th elements out of order

 Swap them

$\Omega(n^2)$ bubble sort, selection sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$ linear search, binary search

$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$ bubble sort

$\Omega(\log n)$

$\Omega(1)$



recursion

```
1 Pick up phone book
2 Open to middle of phone book
3 Look at page
4 If person is on page
5     Call person
6 Else if person is earlier in book
7     Open to middle of left half of book
8     Go back to line 3
9 Else if person is later in book
10    Open to middle of right half of book
11    Go back to line 3
12 Else
13    Quit
```

```
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```

```
1 Pick up phone book
2 Open to middle of phone book
3 Look at page
4 If person is on page
5     Call person
6 Else if person is earlier in book
7     Search left half of book
8
9 Else if person is later in book
10    Search right half of book
11
12 Else
13    Quit
```

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1 Pick up phone book
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8 Else if person is later in book
9     Search right half of book
10 Else
11     Quit
```













merge sort

If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves

If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves

7 4 5 2 6 3 8 1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

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5 2 6 3 8 1

4 7

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4 7 2 5

6 3 8 1



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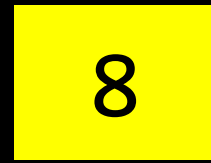
6

2

4

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3 6

2 4 5 7

8

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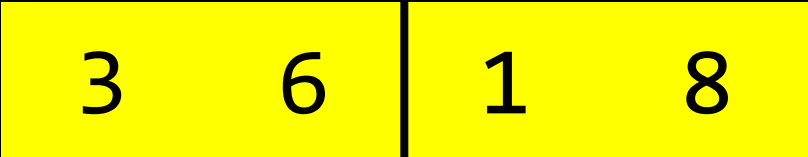
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2 4 5 7

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2	4	5	7		1	3	6	8
---	---	---	---	--	---	---	---	---

2

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8

1

4 5 7

3 6 8

1 2

4 5 7

6 8

1 2 3

1 2 3 4

5 7

6 8

1 2 3 4 5

7

6 8

1 2 3 4 5 6

7

8

1 2 3 4 5 6 7

8

1

2

3

4

5

6

7

8

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

2	4	5	7	1	3	6	8
---	---	---	---	---	---	---	---

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

2	4	5	7	1	3	6	8
---	---	---	---	---	---	---	---

1	2	3	4	5	6	7	8
---	---	---	---	---	---	---	---

$O(n^2)$

$O(n \log n)$ merge sort

$O(n)$

$O(\log n)$

$O(1)$

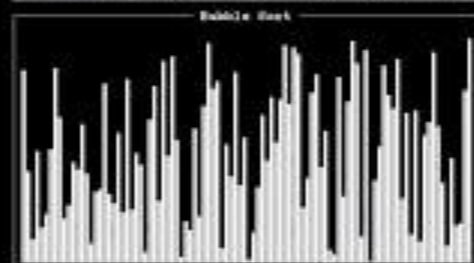
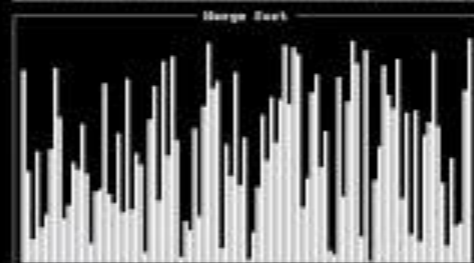
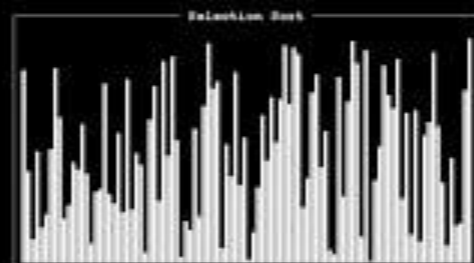
$\Omega(n^2)$

$\Omega(n \log n)$ merge sort

$\Omega(n)$

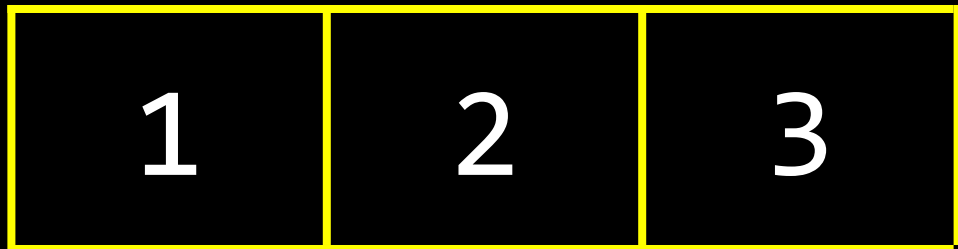
$\Omega(\log n)$

$\Omega(1)$



arrays

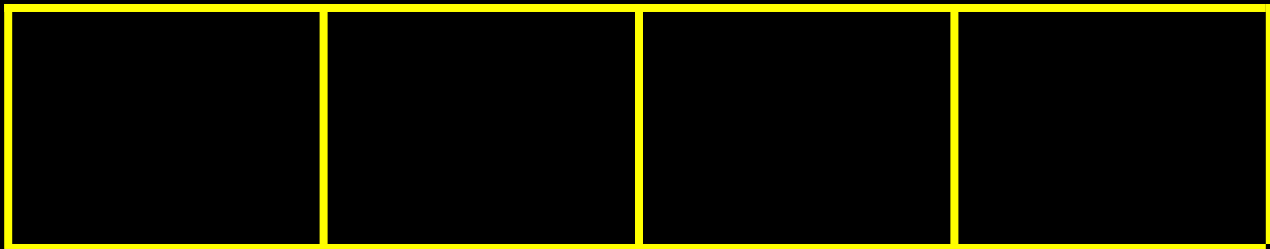


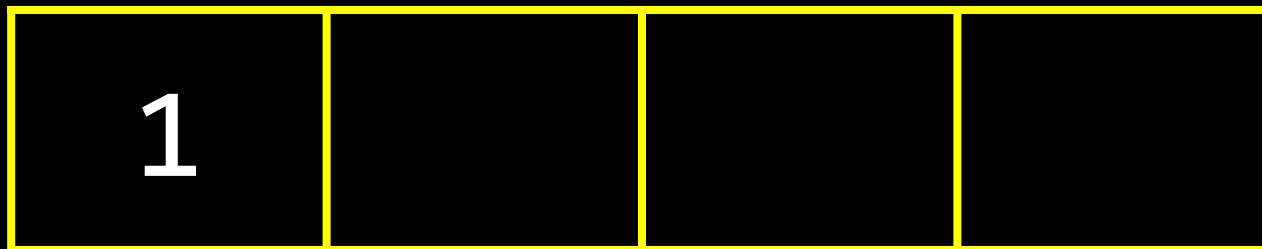
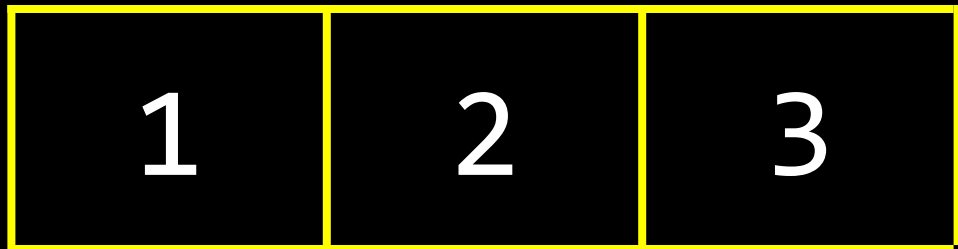


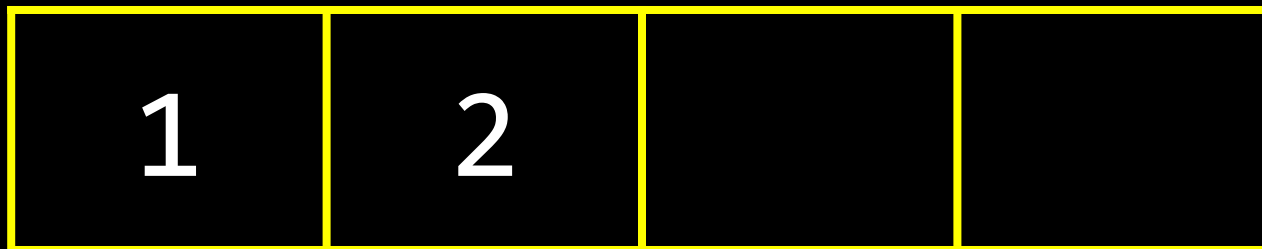
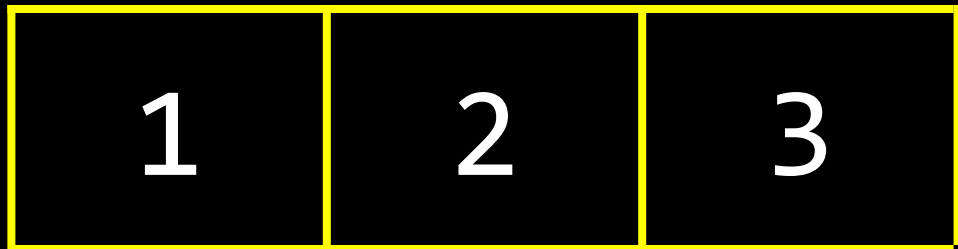
1	2	3	
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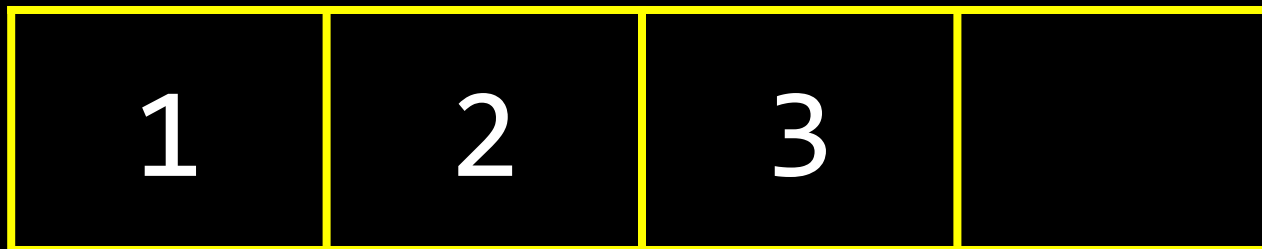
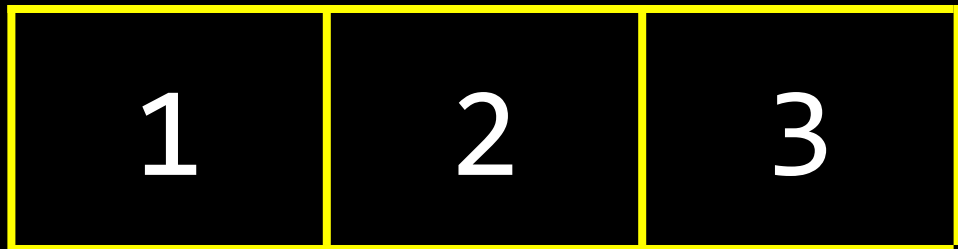
	1	2	3				

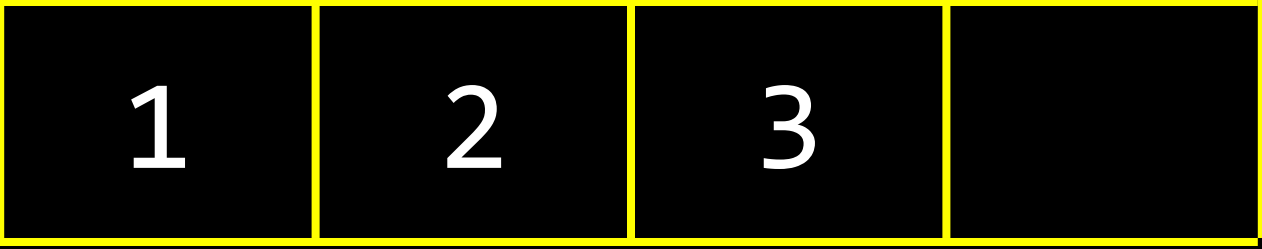
?	?	?	?	?	?	?	?
?	1	2	3	?	?	?	?
?	?	?	?	?	?	?	?
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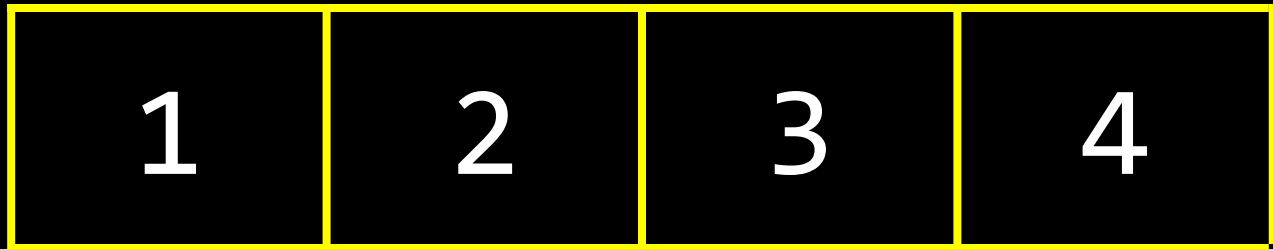












$O(n^2)$

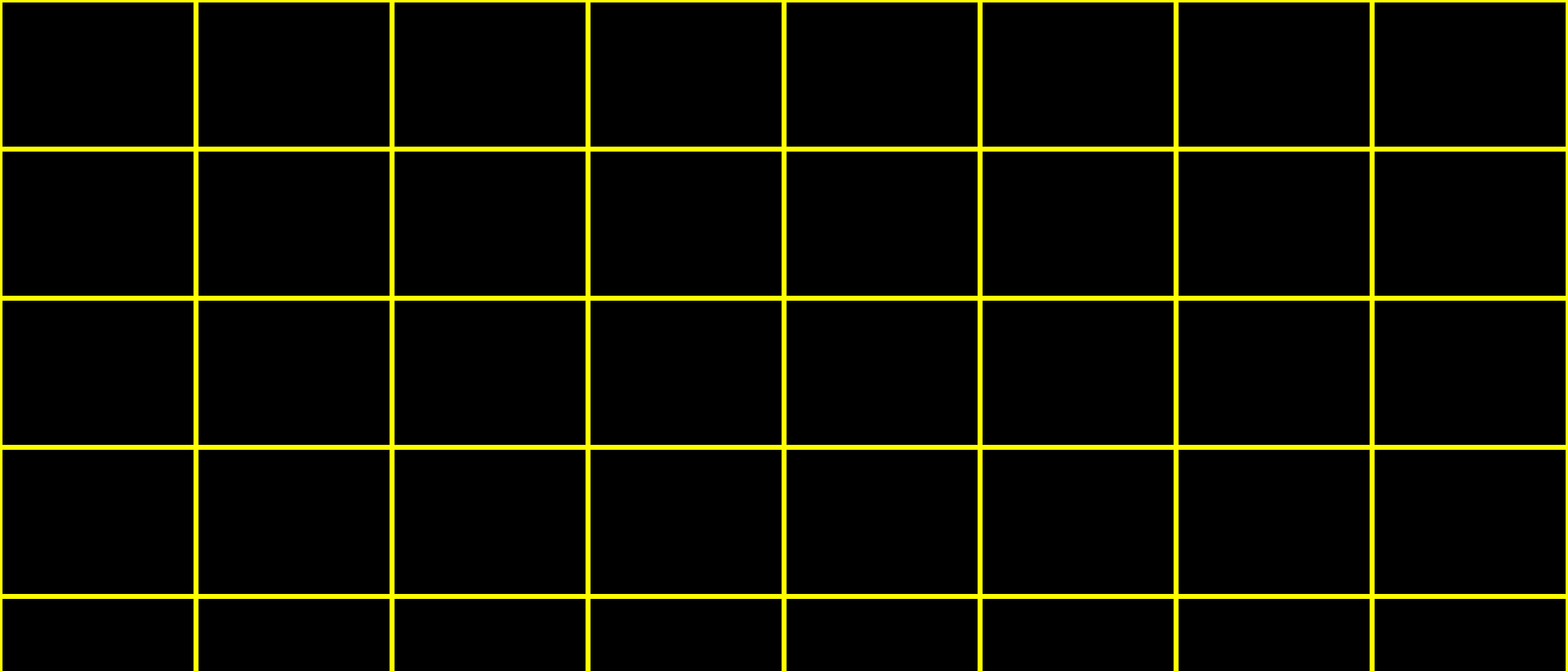
$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

linked lists



1

0x123

1

0x123

2

0x456

1

0x123

2

0x456

3

0x789

1

0x123

2

0x456

3

0x789

1

0x123

0x456

2

0x456

3

0x789

1

0x123

0x456

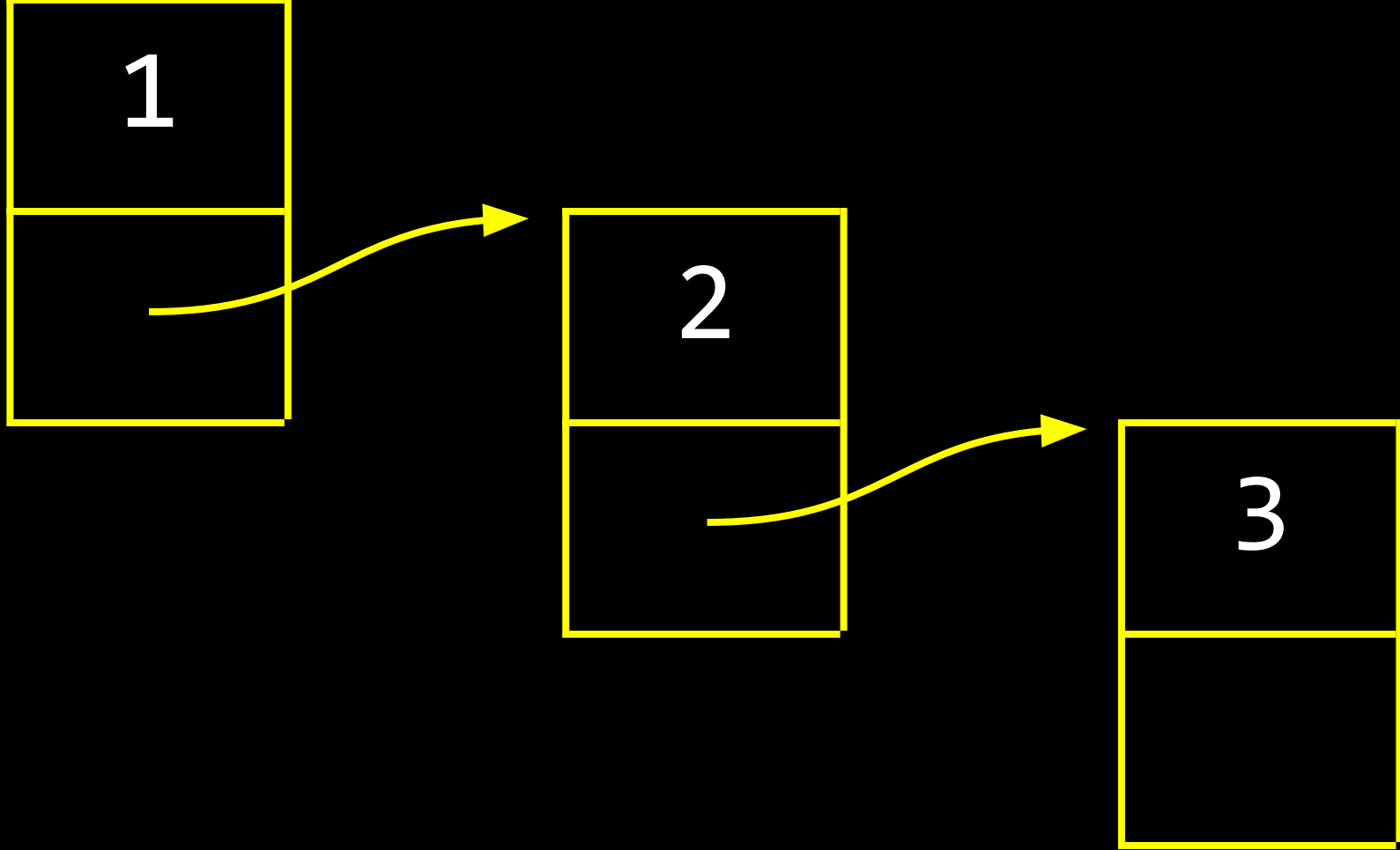
2

0x456

0x789

3

0x789



dict

list

range

set

tuple

...

trees

binary search trees

1

2

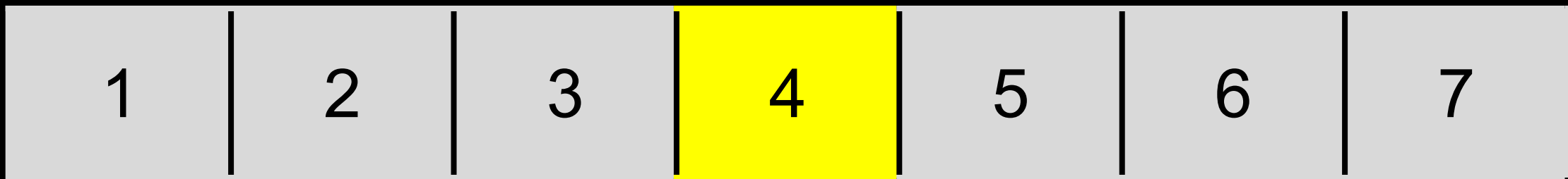
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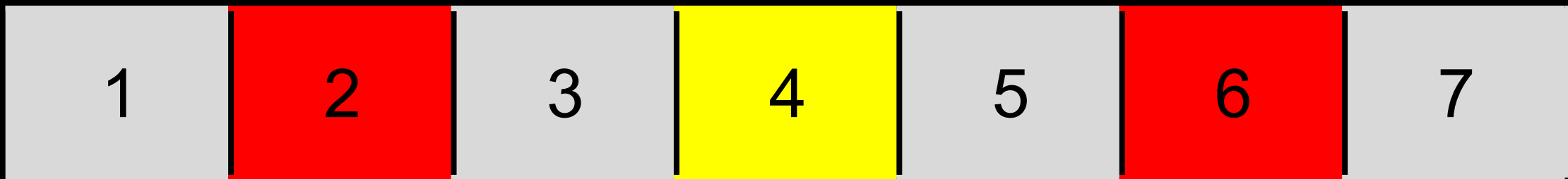
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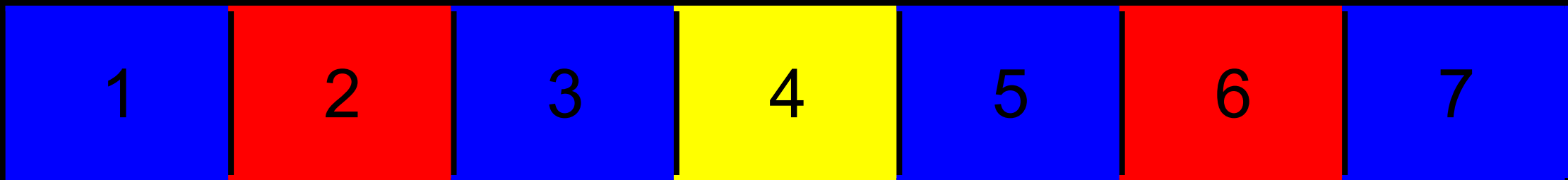
5

6

7







4

2

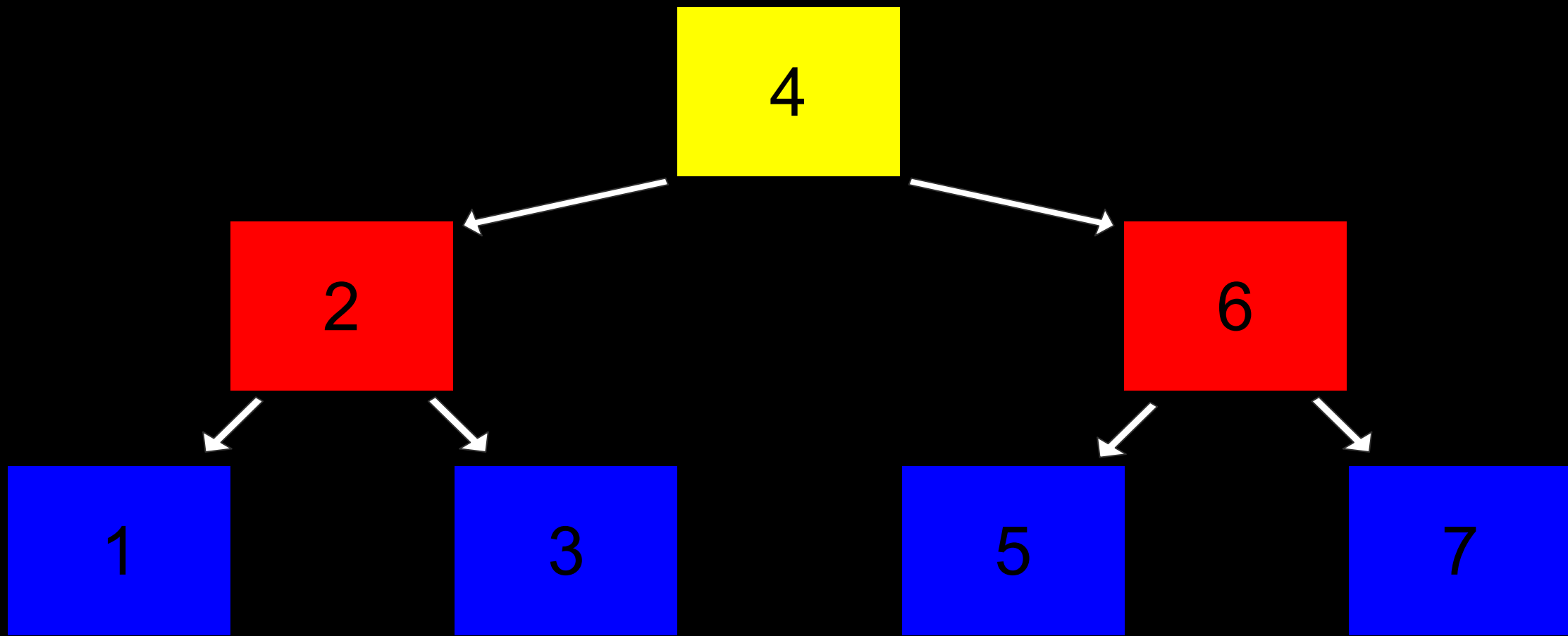
6

1

3

5

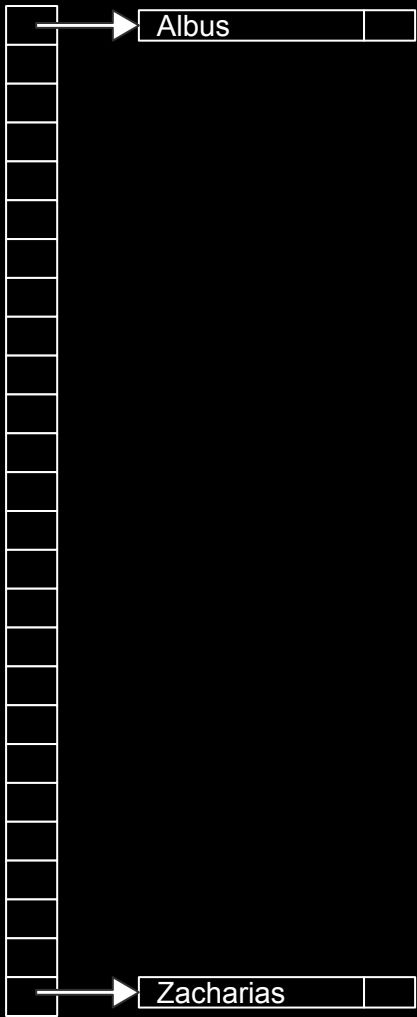
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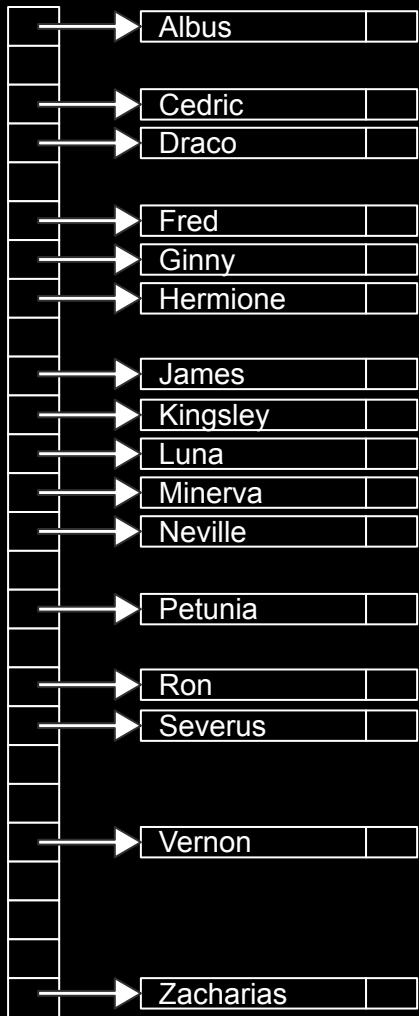


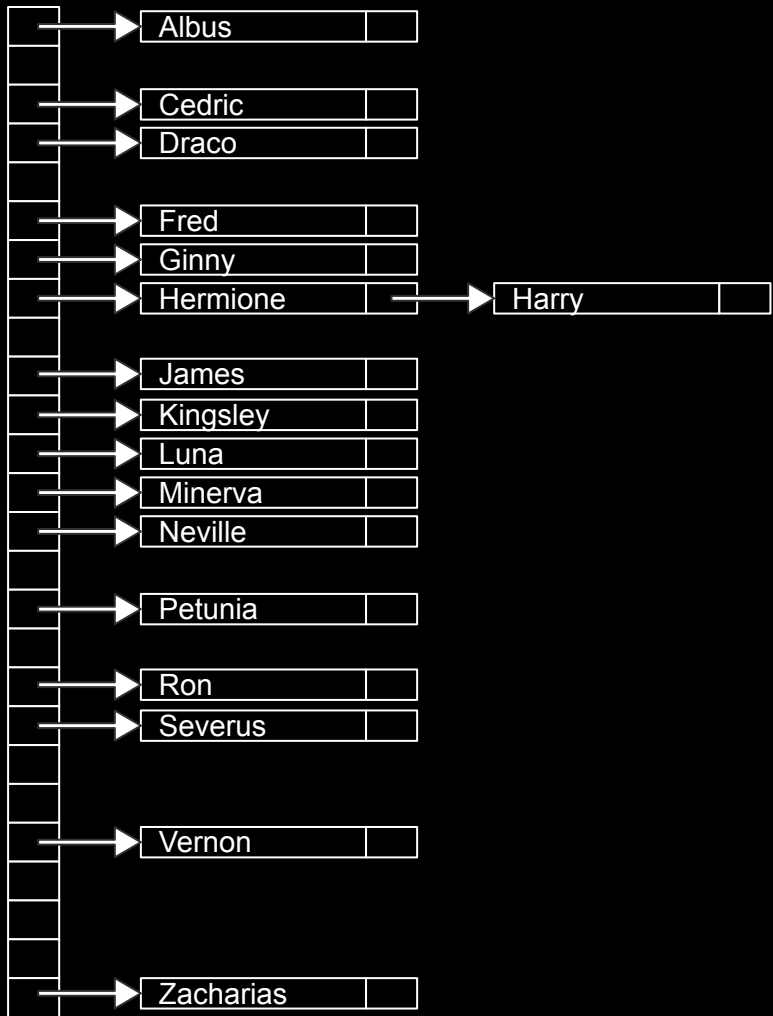
hash tables

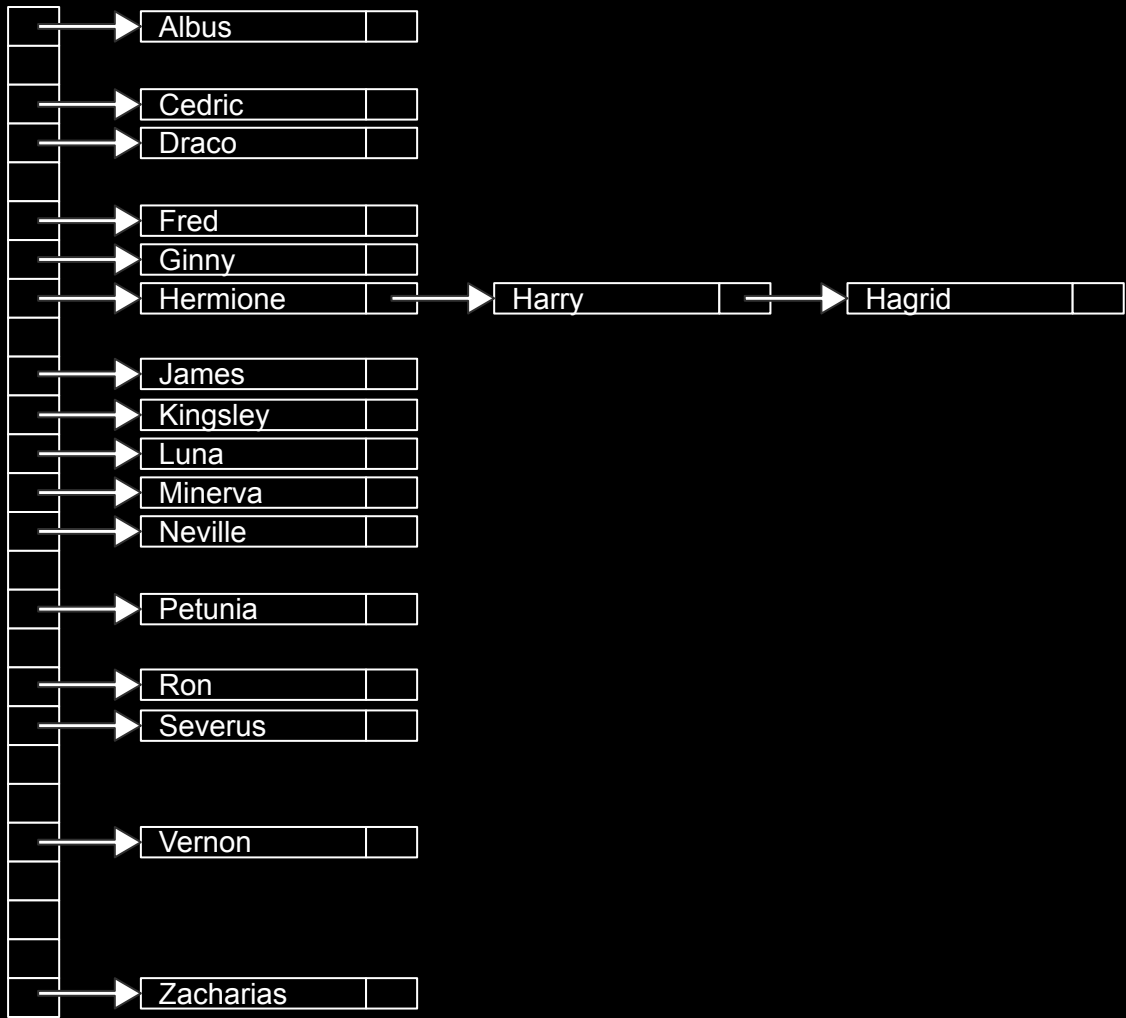
0
1
2
3
4
5
6
7
8
9
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11
12
13
14
15
16
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21
22
23
24
25

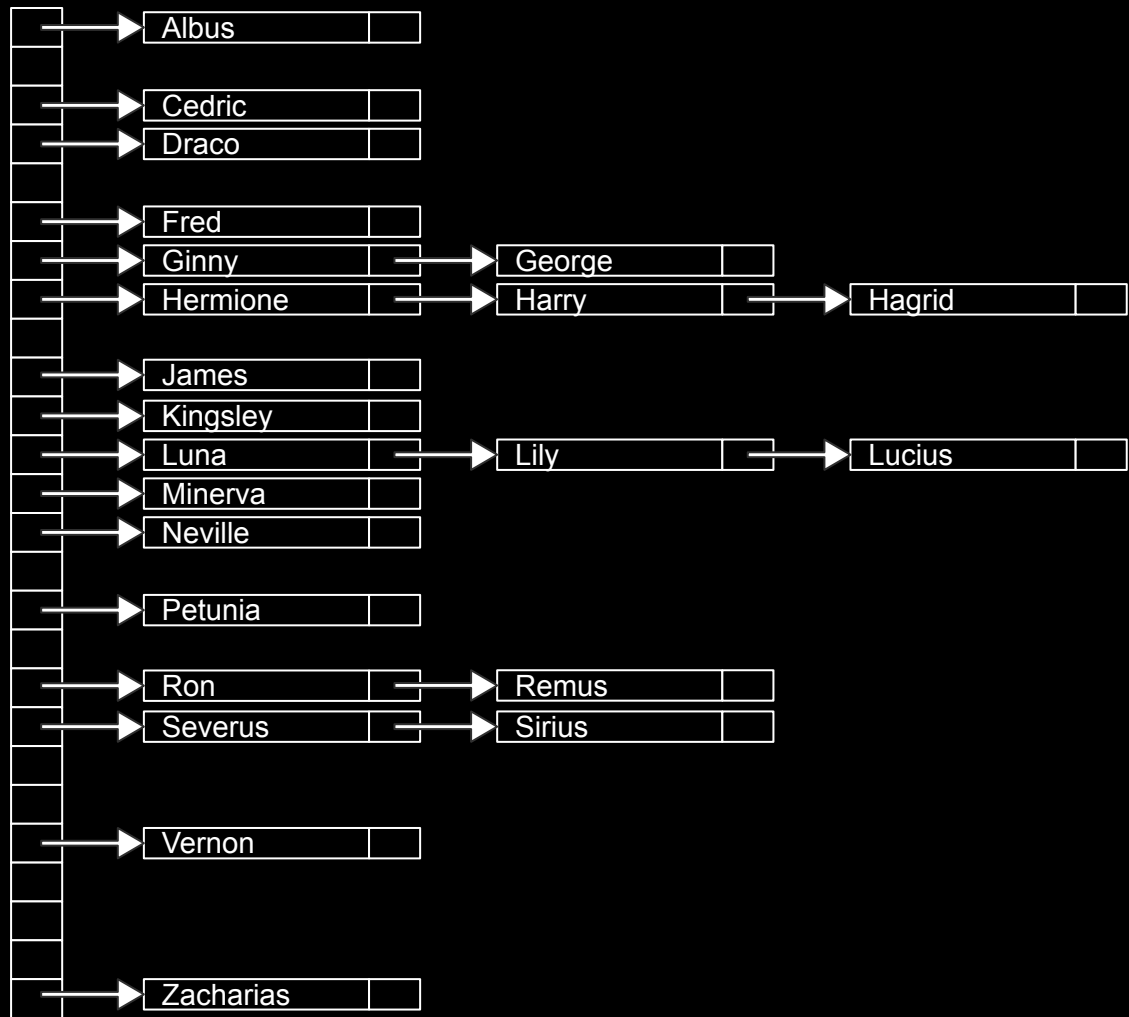
A	
B	
C	
D	
E	
F	
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I	
J	
K	
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M	
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O	
P	
Q	
R	
S	
T	
U	
V	
W	
X	
Y	
Z	



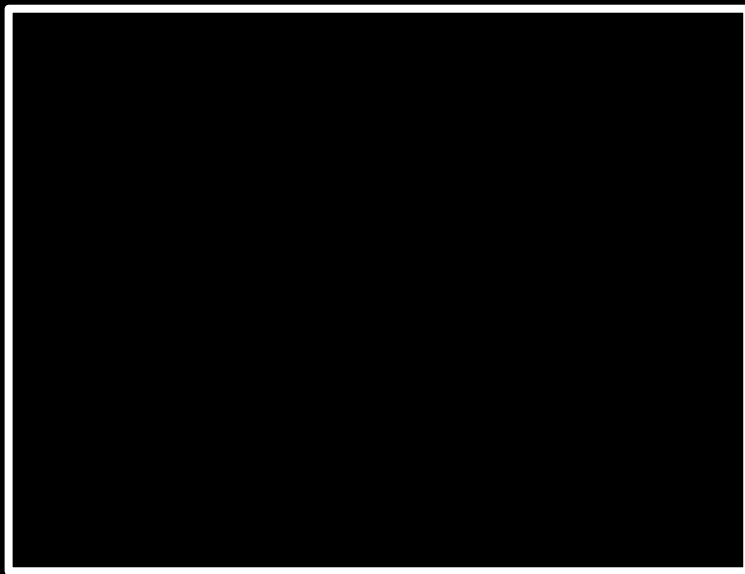








input →



→ output

hash function

Albus →

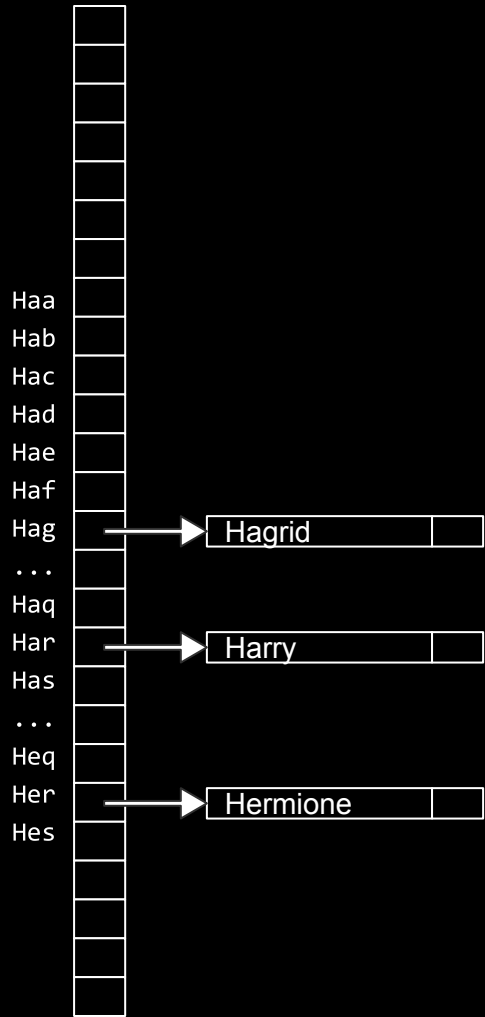


→ 0

Zacharias →



→ 25



$O(n^2)$

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$O(n^2)$

$O(n \log n)$

$O(n)$ search

$O(\log n)$

$O(1)$

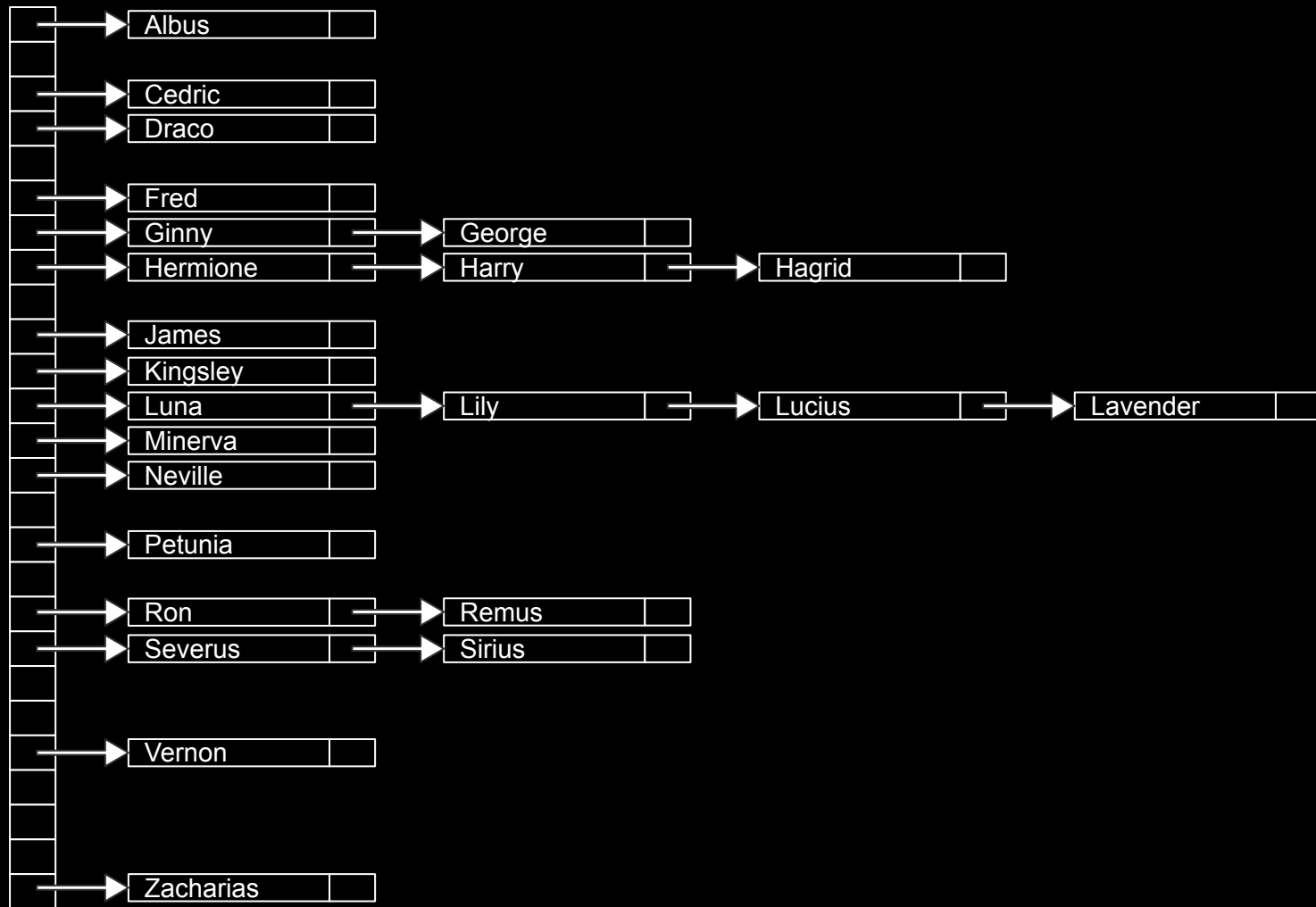
$O(n^2)$

$O(n \log n)$

$O(n)$ search

$O(\log n)$

$O(1)$ insert



dictionaries

dict

list

range

set

tuple

...

PICK ME UP



B C D E F G H I

K L M N O P Q R

T U- V W X Y Z



CHOKIN
FROM IL ABAY
ORION STORE RESPOND

queues

stacks

Lab

Python

Assignment 2

cs50.harvard.edu/hls/2021/winter/assignments/2

Office Hours

cs50.harvard.edu/hls/2021/winter/hours

CS50 for JDs

cs50.harvard.edu/hls