



Computer Science 50

Introduction to Computer Science I

Harvard College

Week 7

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Trees

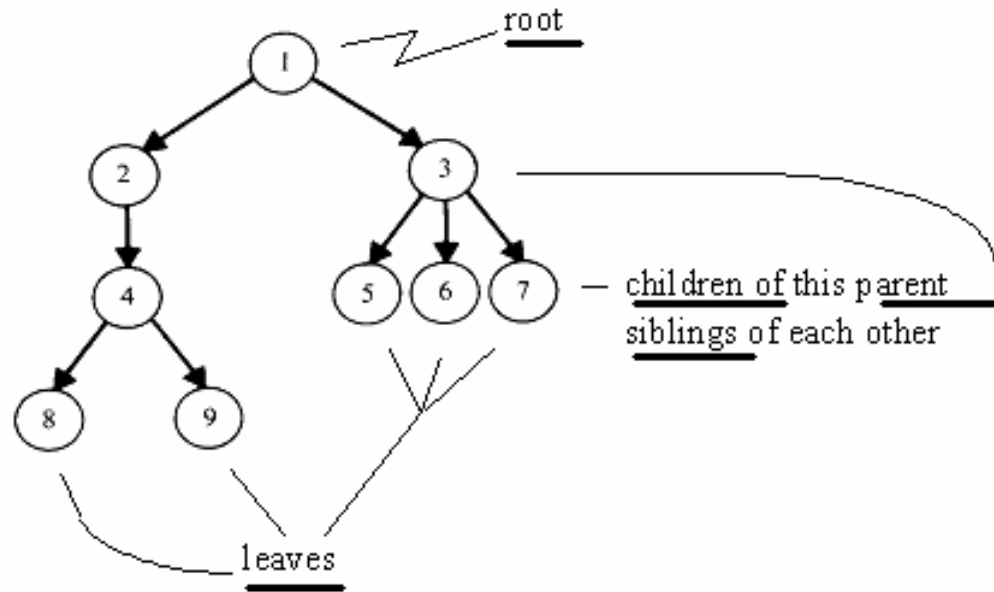
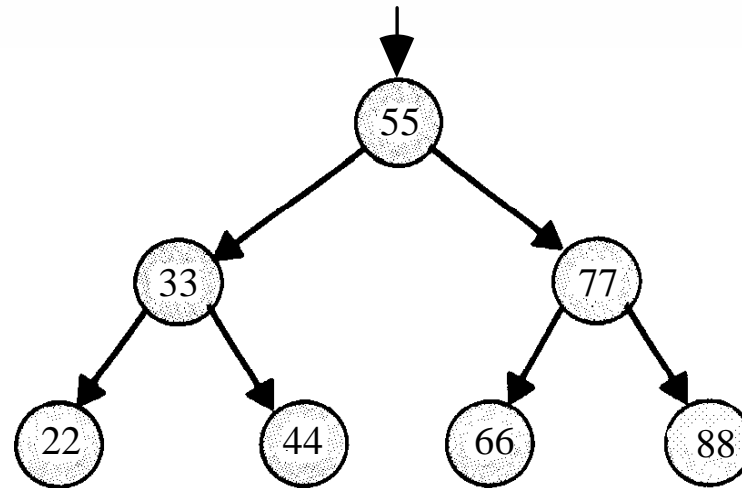


Figure by Larry Nyhoff.

Binary Search Trees



Tries

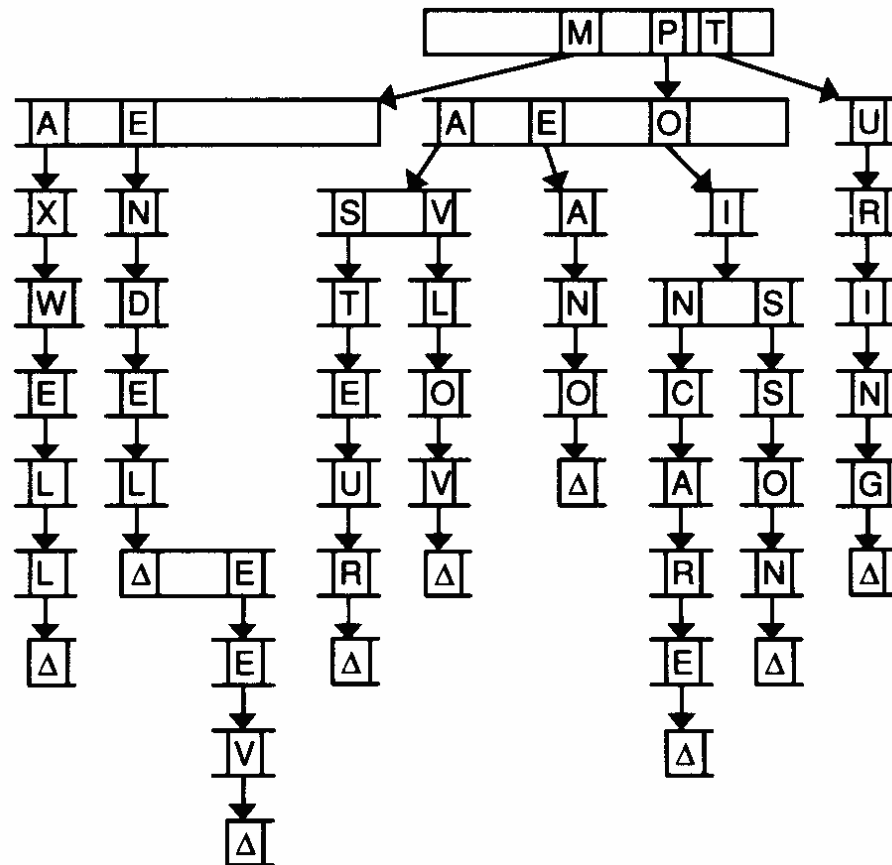
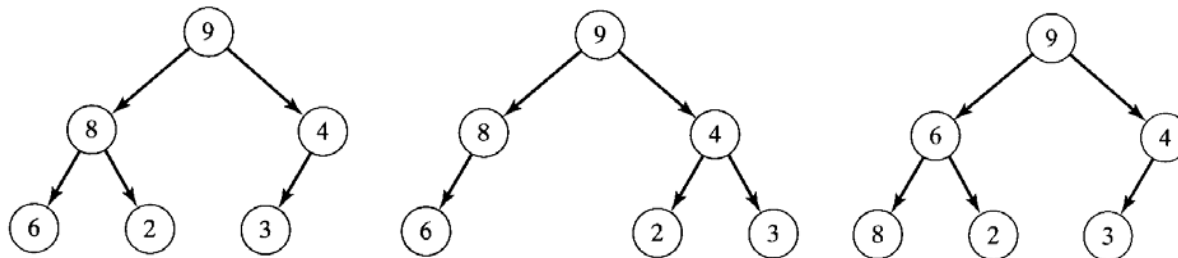


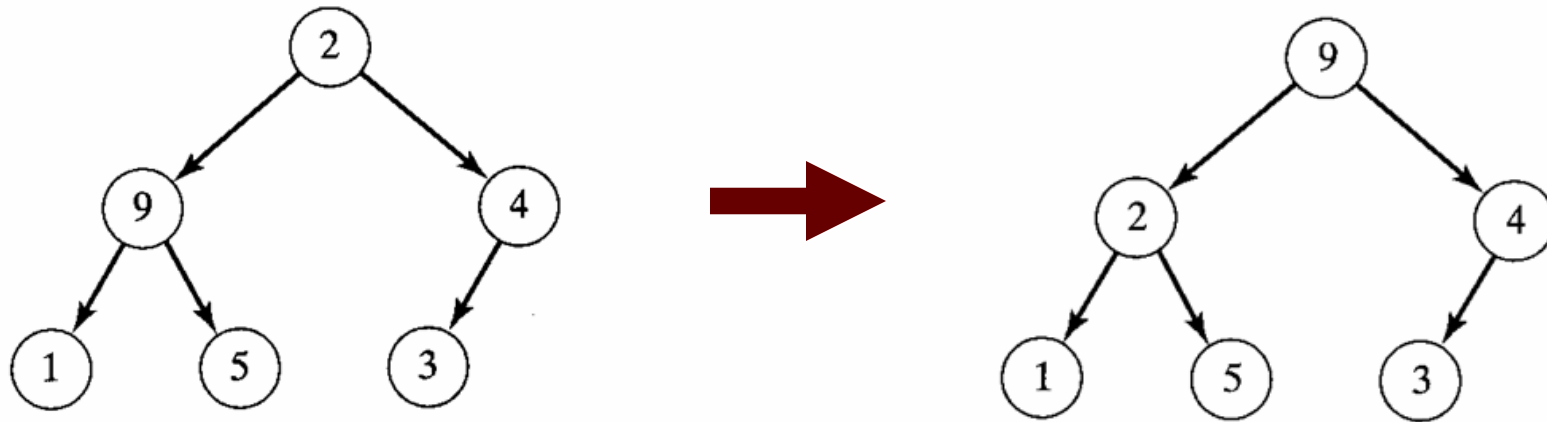
Figure from Lewis and Denenberg's *Data Structures & Their Algorithms*.

Heaps

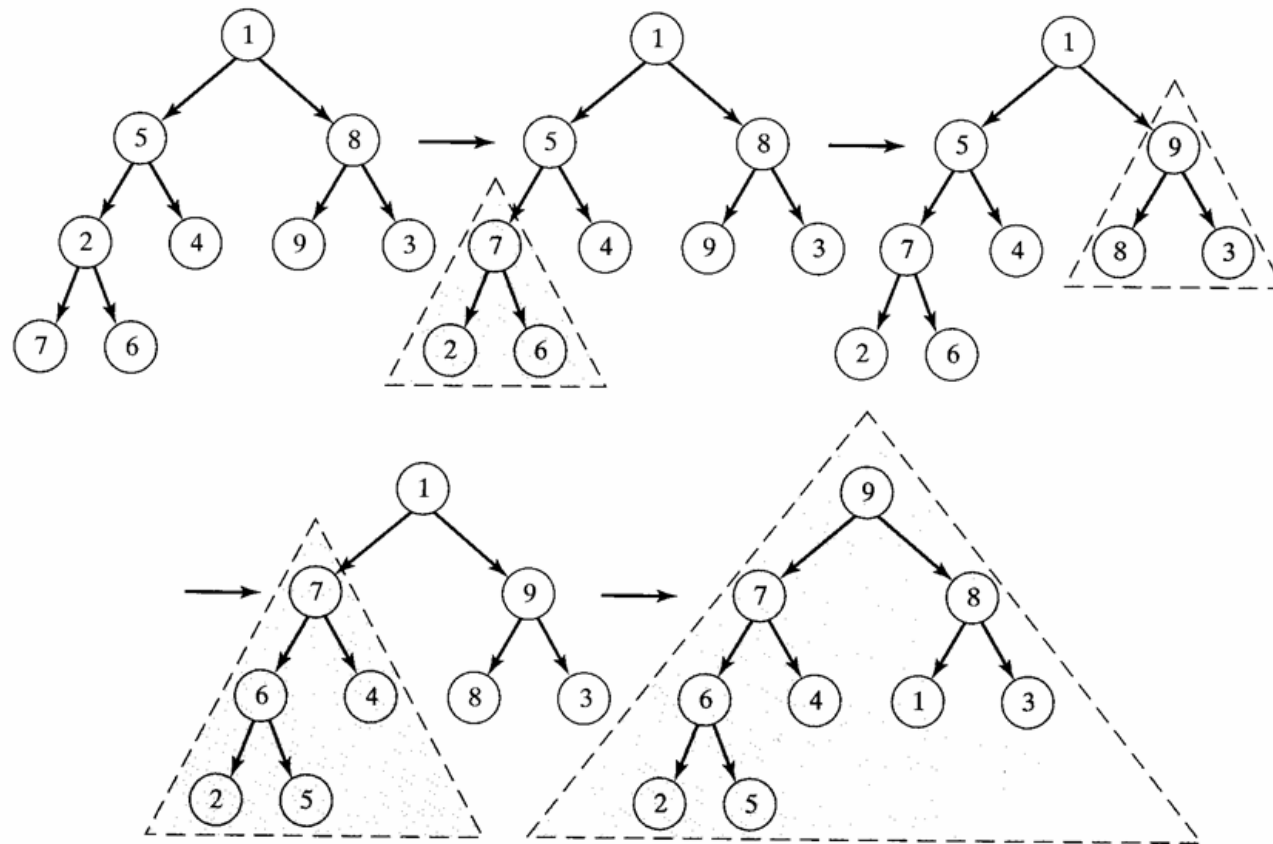
- ∴ A **heap** is a binary tree that
 - ∴ is **complete** (*i.e.*, every level of the tree is completely filled with nodes except for, perhaps, the bottommost level, whose nodes are in the leftmost locations)
 - ∴ satisfies the **heap-order property** (*i.e.*, each node's value is greater than or equal to that of each of its children, if any)



Heapifying an Almost Heap

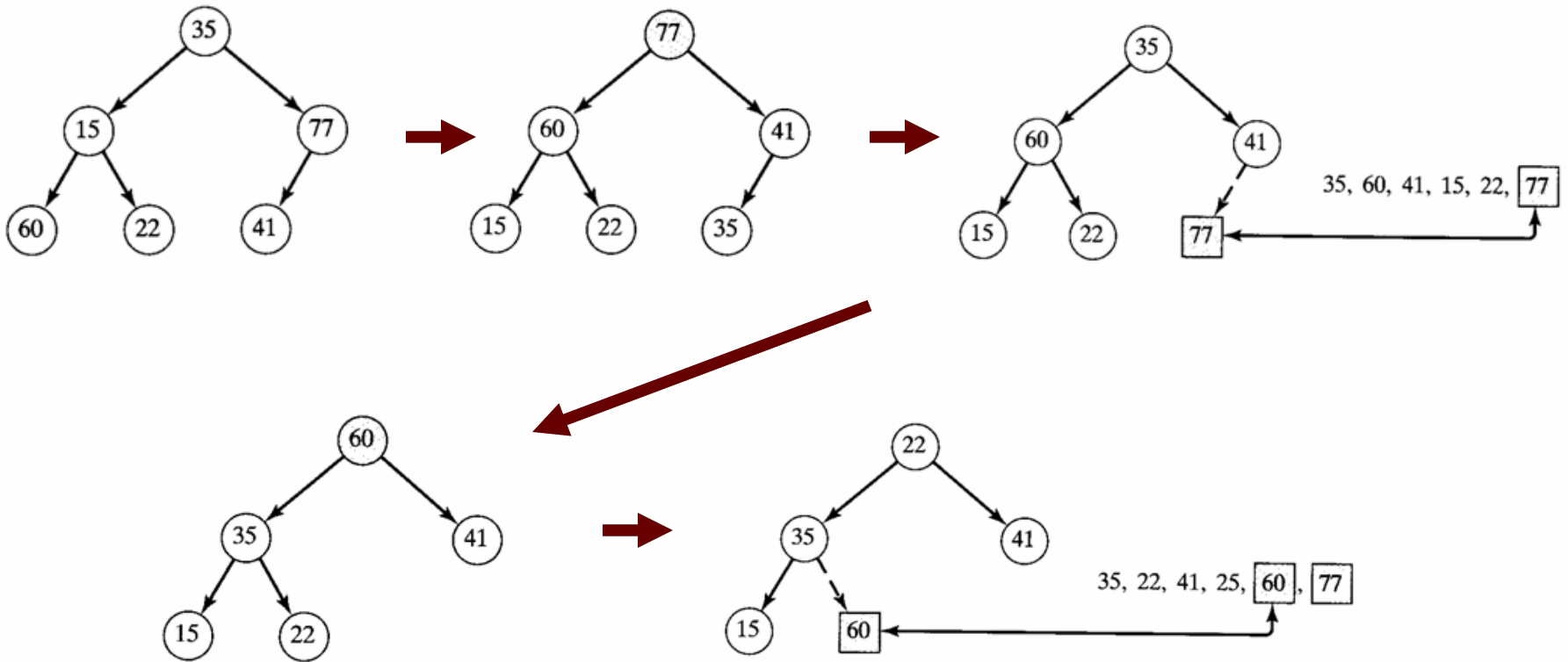


Heapifying a Binary Tree



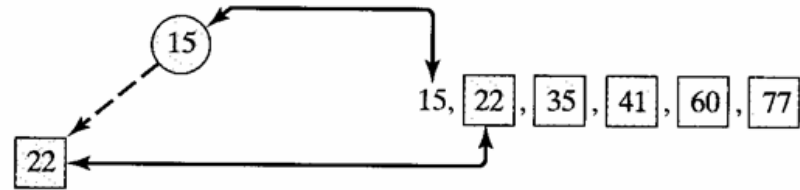
Heapsort

35 15 77 60 22 41



Heapsort

35 15 77 60 22 41





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