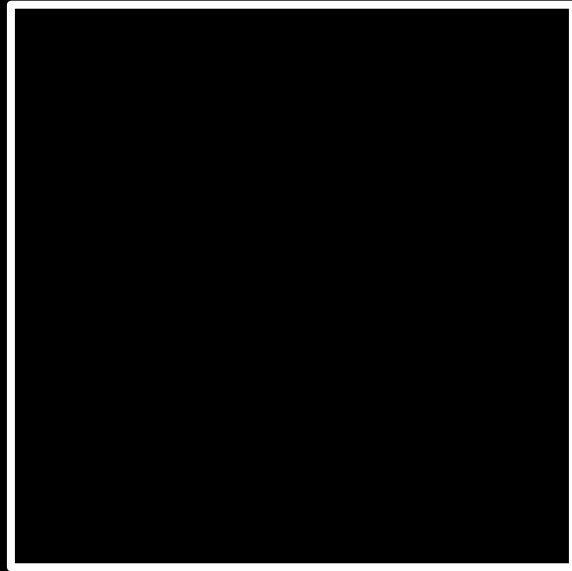


# CS50 for MBAs

Algorithms

shorts

input →



→ output



algorithms





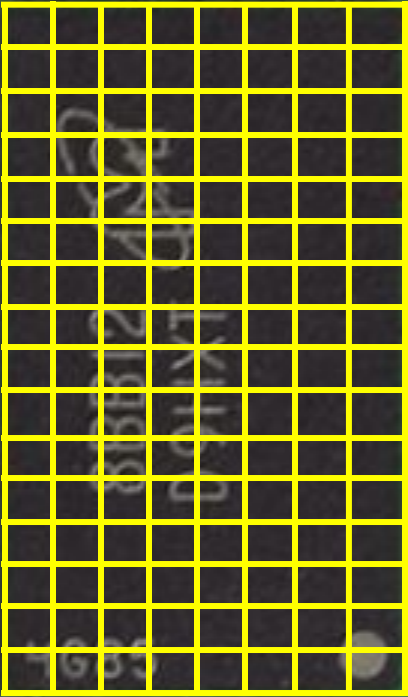
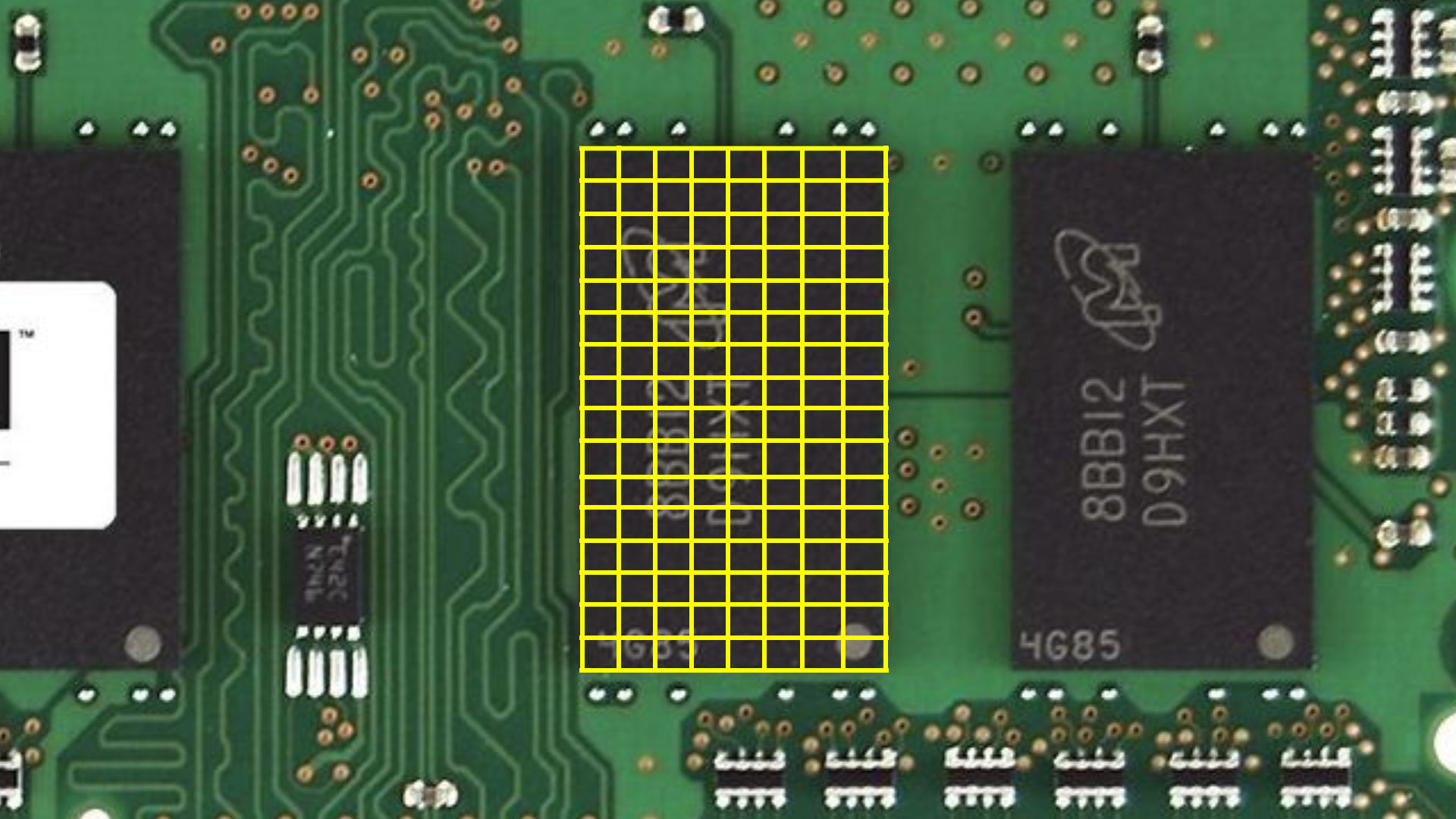
8BB12  
D9HXT

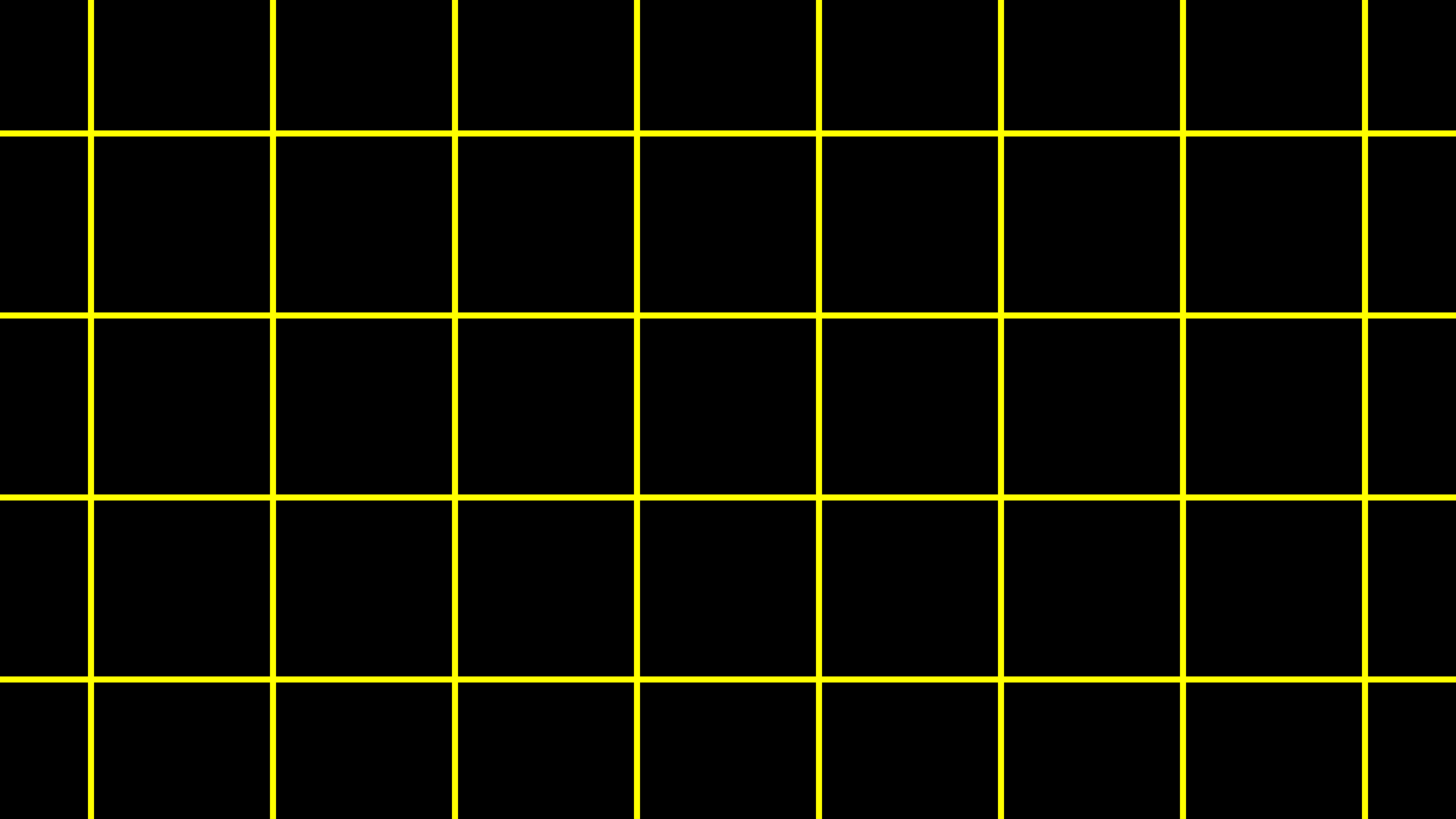
4G85



8BB12  
D9HXT

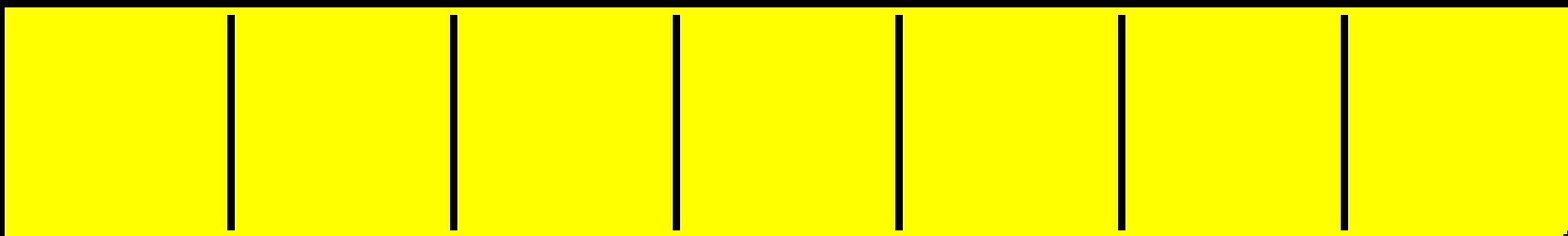
4G85







|  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|
|  |  |  |  |  |  |  |
|--|--|--|--|--|--|--|



linear search



```
For each door from left to right
  If number is behind door
    Answer is true
  Else
    Answer is false
```

binary search

```
If number behind middle door
    Return true
Else if number < middle door
    Search left half
Else if number > middle door
    Search right half
```

If no doors

If number behind middle door

Return true

Else if number < middle door

Search left half

Else if number > middle door

Search right half



If no doors

    Return false

If number behind middle door

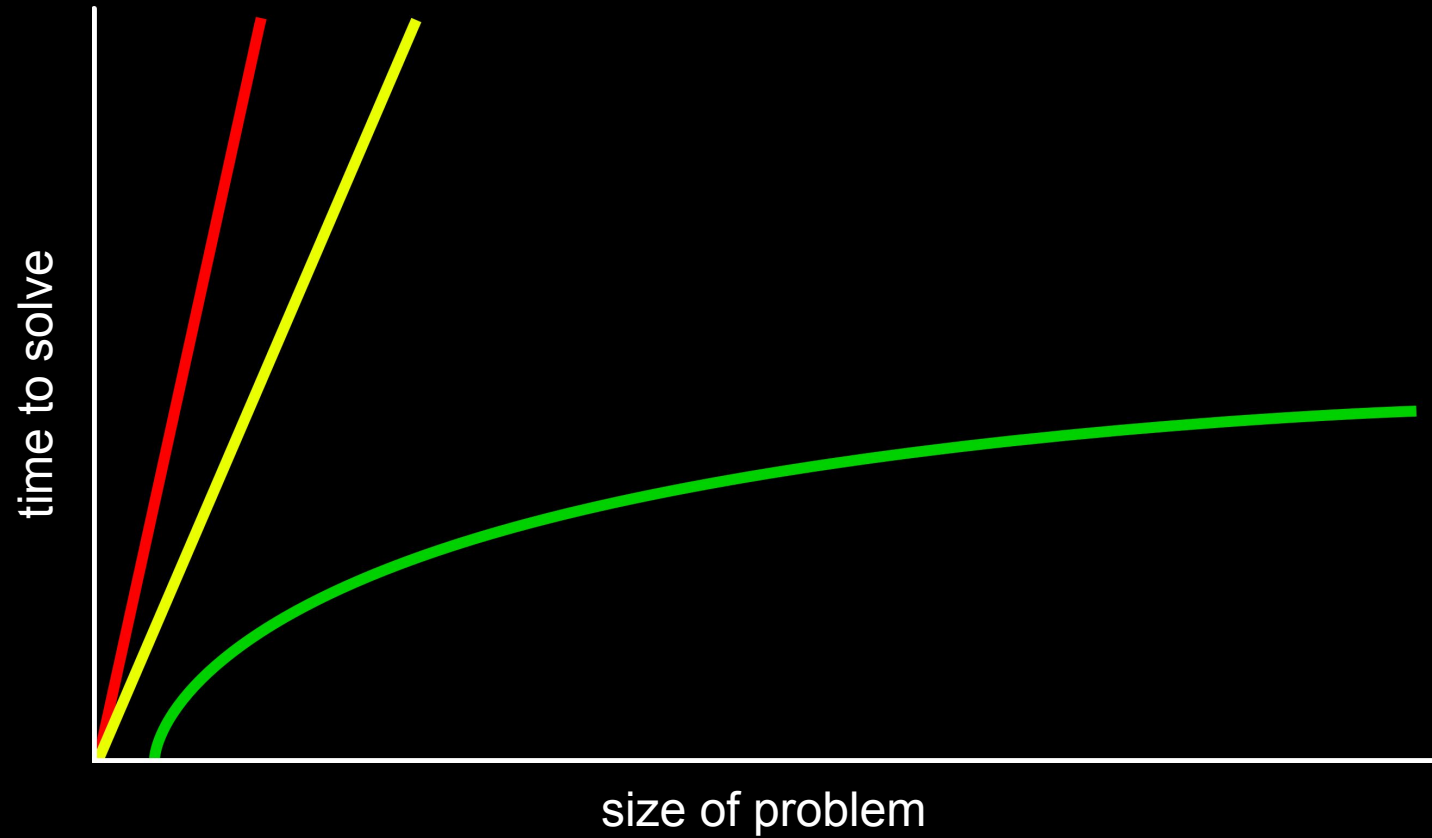
    Return true

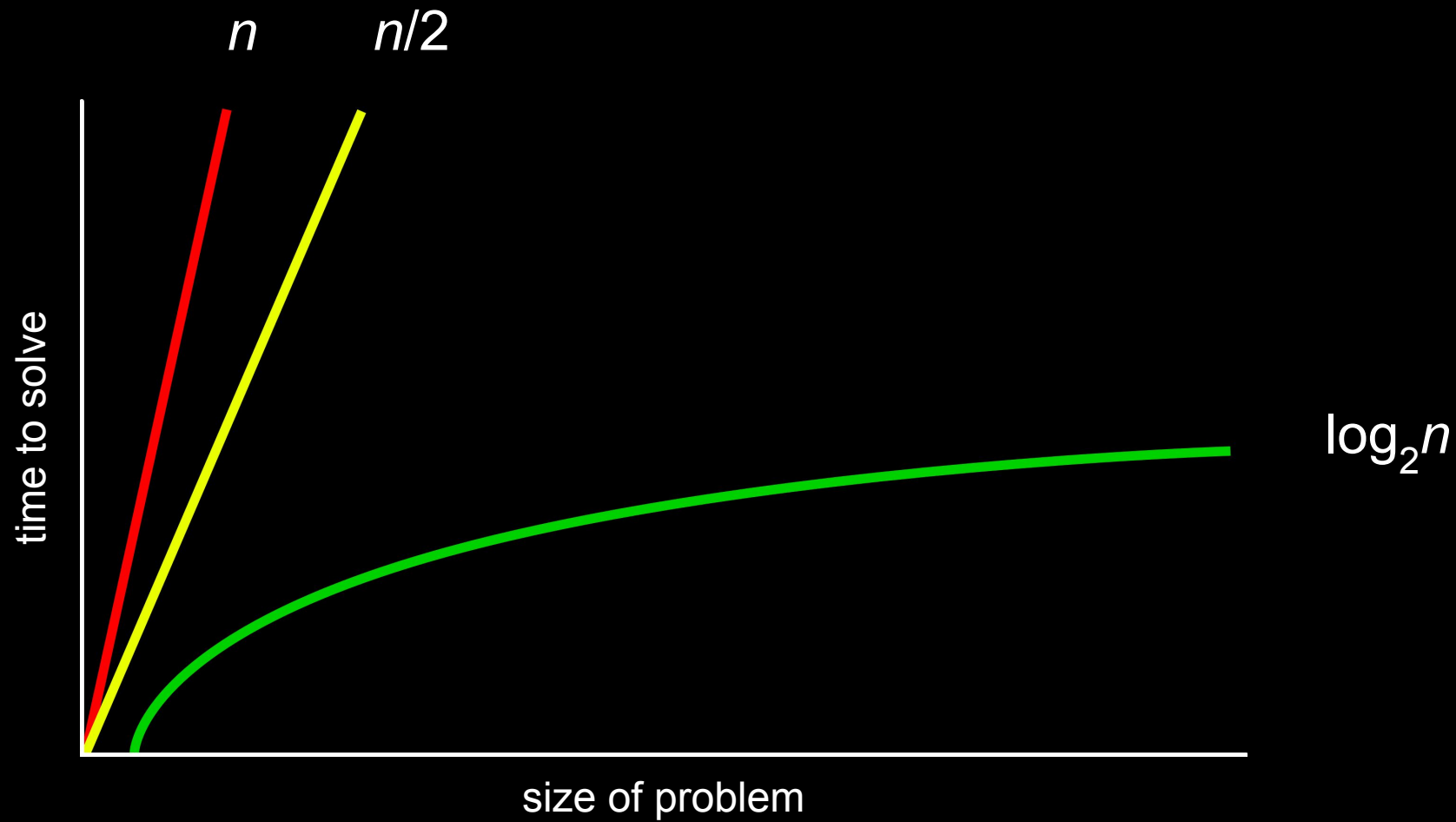
Else if number < middle door

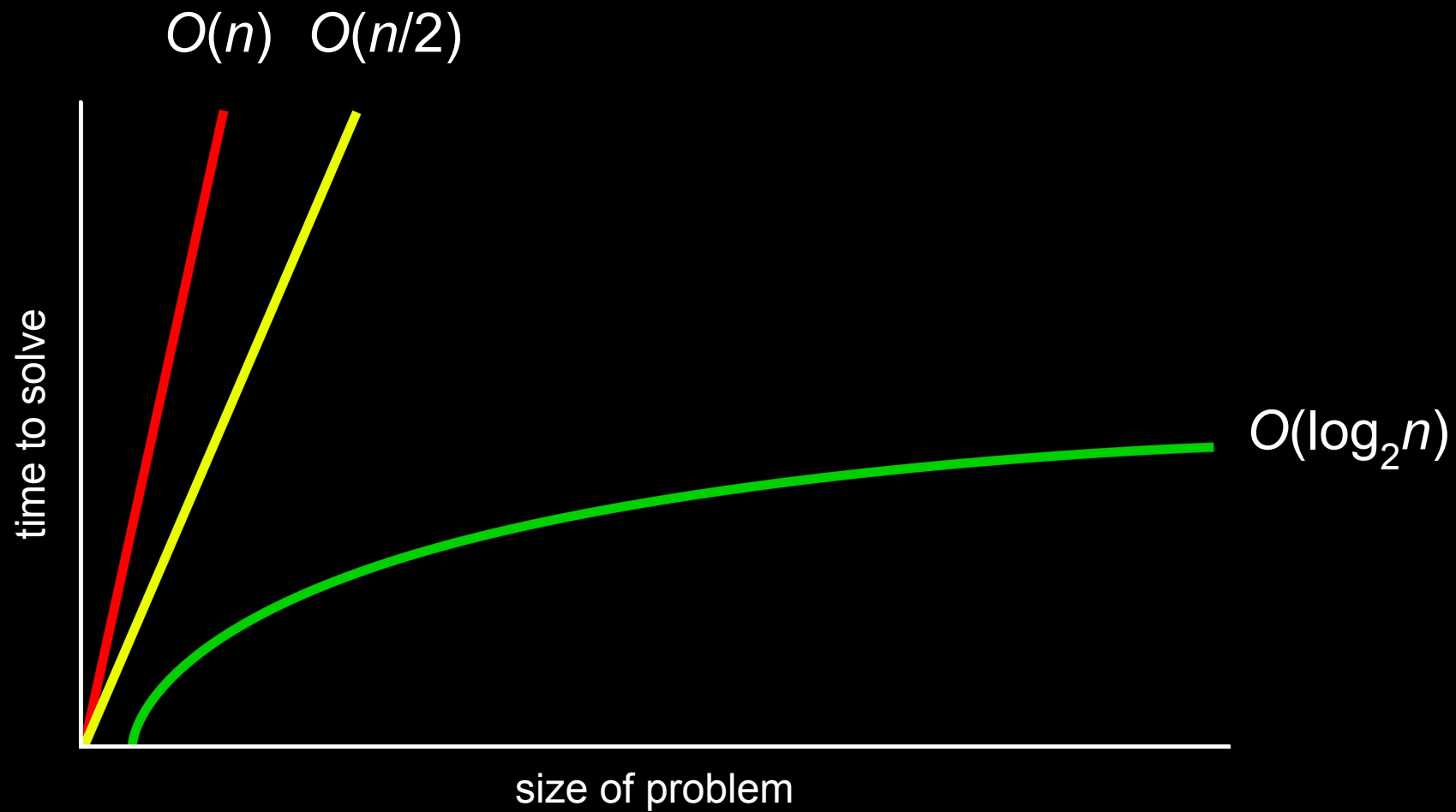
    Return result of searching left half

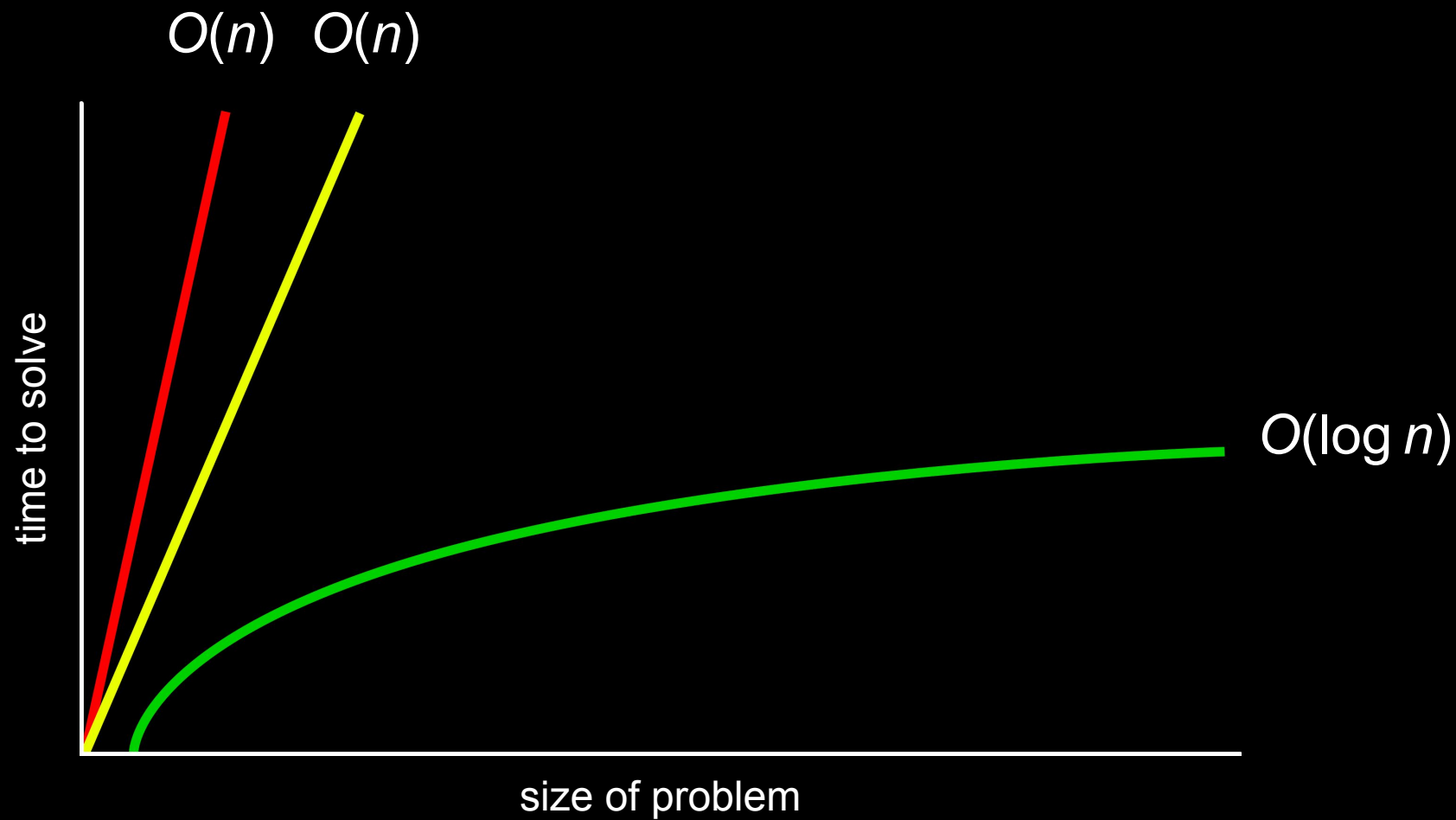
Else if number > middle door

    Return result of searching right half









$O(n^2)$

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$O(n^2)$

$O(n \log n)$

$O(n)$       linear search

$O(\log n)$       binary search

$O(1)$

$$\Omega(n^2)$$

$$\Omega(n \log n)$$

$$\Omega(n)$$

$$\Omega(\log n)$$

$$\Omega(1)$$



$\Omega(n^2)$

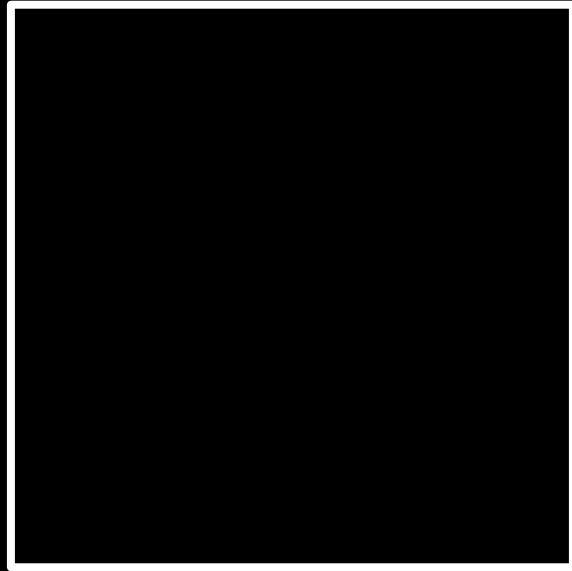
$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

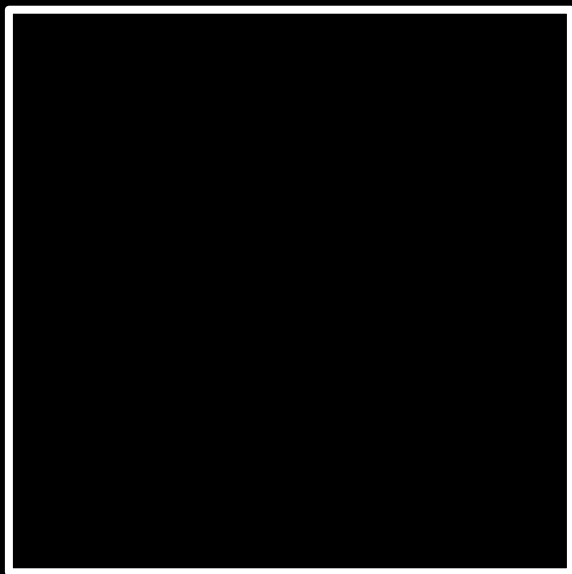
$\Omega(1)$       linear search, binary search

input →



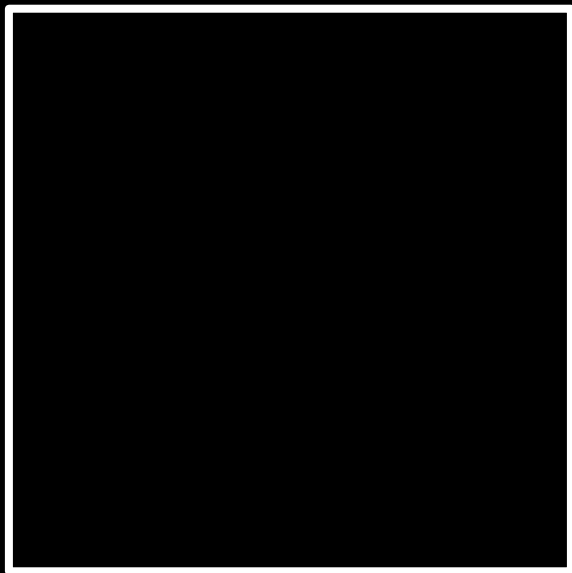
→ output

unsorted →



→ output

unsorted →



→ sorted

6 3 8 5 2 7 4 1

selection sort

For  $i$  from 0 to  $n-1$

    Find smallest item between  $i$ 'th item and last item

    Swap smallest item with  $i$ 'th item





$(n - 1)$

$$(n - 1) + (n - 2)$$

$$(n - 1) + (n - 2) + (n - 3)$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$n^2/2 - n/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$n^2/2 - n/2$$

$$O(n^2)$$



$O(n^2)$       selection sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$\Omega(n^2)$       selection sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

6 3 8 5 2 7 4 1

bubble sort

Repeat  $n-1$  times

  For  $i$  from  $0$  to  $n-2$

    If  $i$ 'th and  $i+1$ 'th elements out of order

      Swap them



$$(n - 1) \times (n - 1)$$

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$



$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$

$$O(n^2)$$

$O(n^2)$  bubble sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$\Omega(n^2)$       bubble sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

bubble sort

Repeat  $n-1$  times

For  $i$  from  $0$  to  $n-2$

    If  $i$ 'th and  $i+1$ 'th elements out of order

        Swap them

Repeat until no swaps

  For  $i$  from 0 to  $n-2$

    If  $i$ 'th and  $i+1$ 'th elements out of order

      Swap them

$O(n^2)$  bubble sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$



$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$           bubble sort

$\Omega(\log n)$

$\Omega(1)$



recursion

```
1 Pick up phone book
2 Open to middle of phone book
3 Look at page
4 If person is on page
5     Call person
6 Else if person is earlier in book
7     Open to middle of left half of book
8     Go back to line 3
9 Else if person is later in book
10    Open to middle of right half of book
11    Go back to line 3
12 Else
13    Quit
```

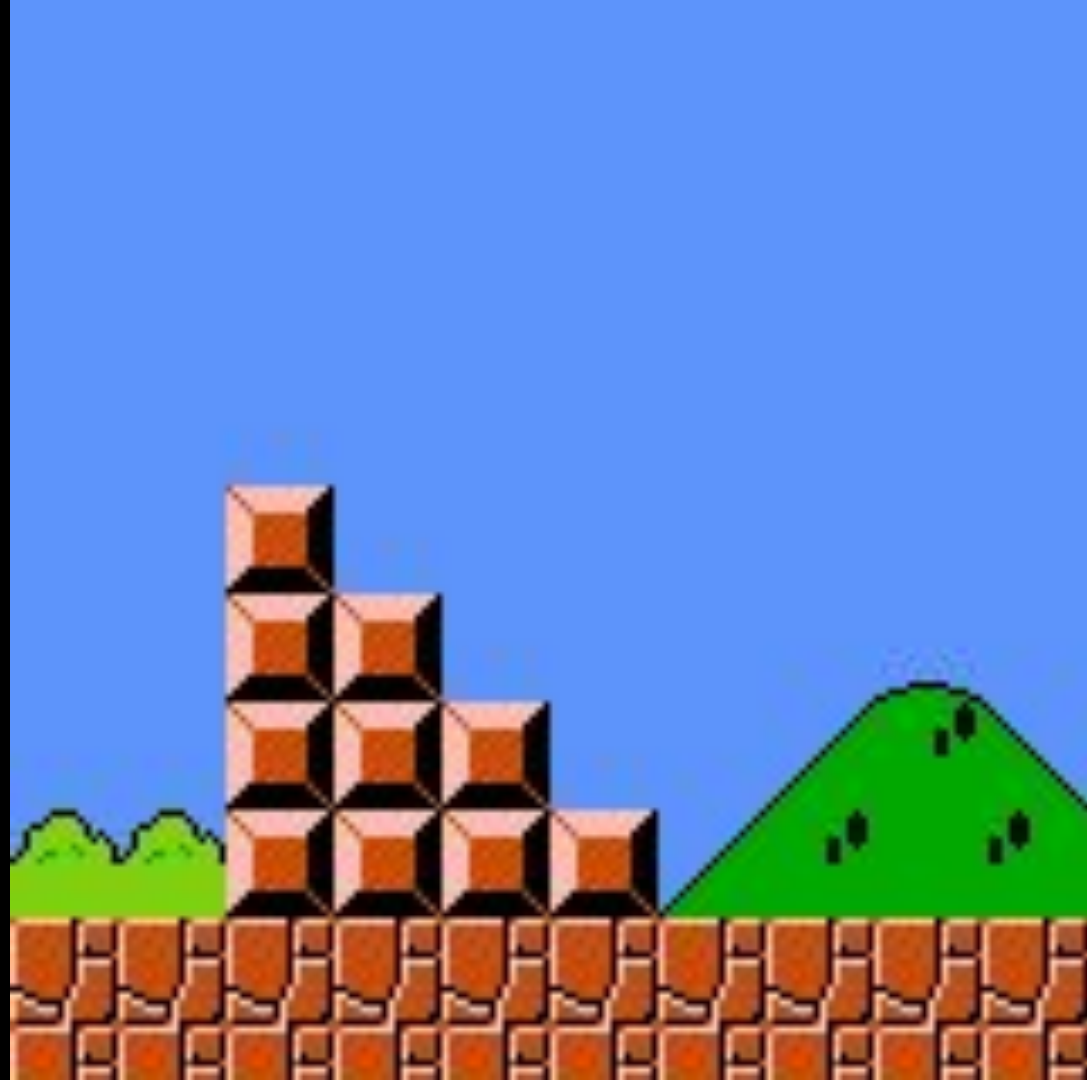
```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Open to middle of left half of book
8      Go back to line 3
9  Else if person is later in book
10     Open to middle of right half of book
11     Go back to line 3
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13     Quit
```

```
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7     Open to middle of left half of book
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10    Open to middle of right half of book
11    Go back to line 3
12 Else
13    Quit
```

```
1 Pick up phone book
2 Open to middle of phone book
3 Look at page
4 If person is on page
5     Call person
6 Else if person is earlier in book
7     Search left half of book
8
9 Else if person is later in book
10    Search right half of book
11
12 Else
13    Quit
```

```
1 Pick up phone book
2 Open to middle of phone book
3 Look at page
4 If person is on page
5     Call person
6 Else if person is earlier in book
7     Search left half of book
8 Else if person is later in book
9     Search right half of book
10 Else
11     Quit
```















merge sort

If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves



If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves

7 4 5 2 6 3 8 1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

5

2

6

3

8

1

4



5 2 6 3 8 1

4 7

5

2

6

3

8

1

4

7

5

2

6

3

8

1

4

7

5 2 6 3 8 1

4 7

5 2 6 3 8 1

4 7

5

6

3

8

1

4

7

2

6 3 8 1

4 7 2 5

6 3 8 1

|   |   |   |   |
|---|---|---|---|
| 4 | 7 | 2 | 5 |
|---|---|---|---|



6 3 8 1

4 7

5

2

6 3 8 1

7

5

2 4

6 3 8 1

7

2 4 5

6 3 8 1

2 4 5 7

6 3 8 1

2 4 5 7

6

3

8

1

2

4

5

7

6

3

8

1

2

4

5

7

6

3

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5

7

8 1

3 6

2 4 5 7

8 1

3 6

2 4 5 7

8

1

3

6

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4

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7

8



3

6

2

4

5

7

|   |   |
|---|---|
| 8 | 1 |
|---|---|

3 6

2 4 5 7

8

3

6

1

2

4

5

7



3

6

1

8

2

4

5

7

|   |   |   |   |
|---|---|---|---|
| 3 | 6 | 1 | 8 |
|---|---|---|---|

2 4 5 7

2 4 5 7

1

3 6

8

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8

2 4 5 7

3 6 8

1



4 5 7

3 6 8

1 2

4 5 7

6 8

1 2 3

1 2 3 4

5 7

6 8

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4

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6

1 2 3 4 5 6 7

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1

2

3

4

5

6

7

8





|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 7 | 4 | 5 | 2 | 6 | 3 | 8 | 1 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 7 | 4 | 5 | 2 | 6 | 3 | 8 | 1 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 4 | 7 | 2 | 5 | 3 | 6 | 1 | 8 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 7 | 4 | 5 | 2 | 6 | 3 | 8 | 1 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 4 | 7 | 2 | 5 | 3 | 6 | 1 | 8 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 2 | 4 | 5 | 7 | 1 | 3 | 6 | 8 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 7 | 4 | 5 | 2 | 6 | 3 | 8 | 1 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 4 | 7 | 2 | 5 | 3 | 6 | 1 | 8 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 2 | 4 | 5 | 7 | 1 | 3 | 6 | 8 |
|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|---|---|---|---|---|

$O(n^2)$

$O(n \log n)$  merge sort

$O(n)$

$O(\log n)$

$O(1)$

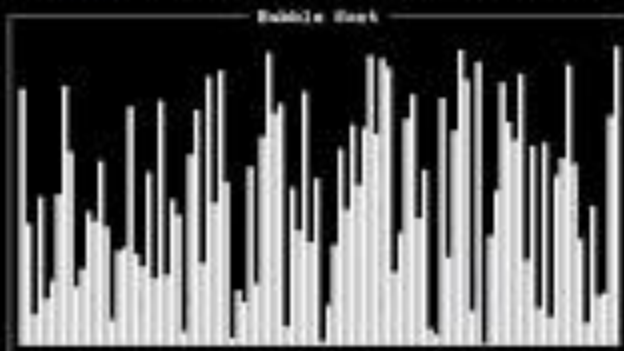
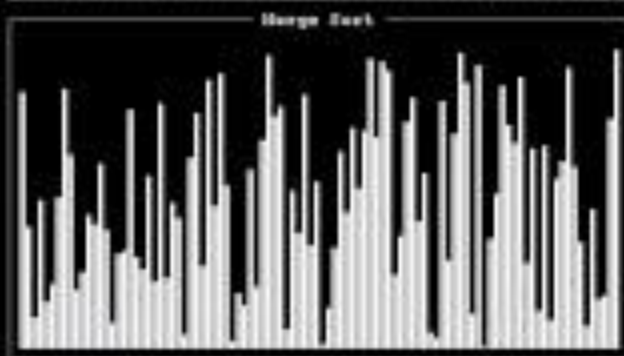
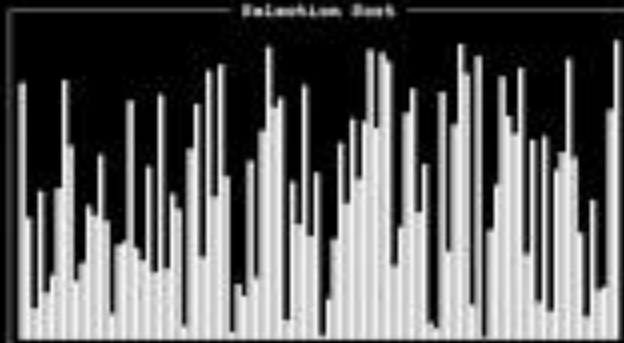
$\Omega(n^2)$

$\Omega(n \log n)$  merge sort

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$







# Assignment 1

# Office Hours

# Lab 0

# CS50 for MBAs

Algorithms