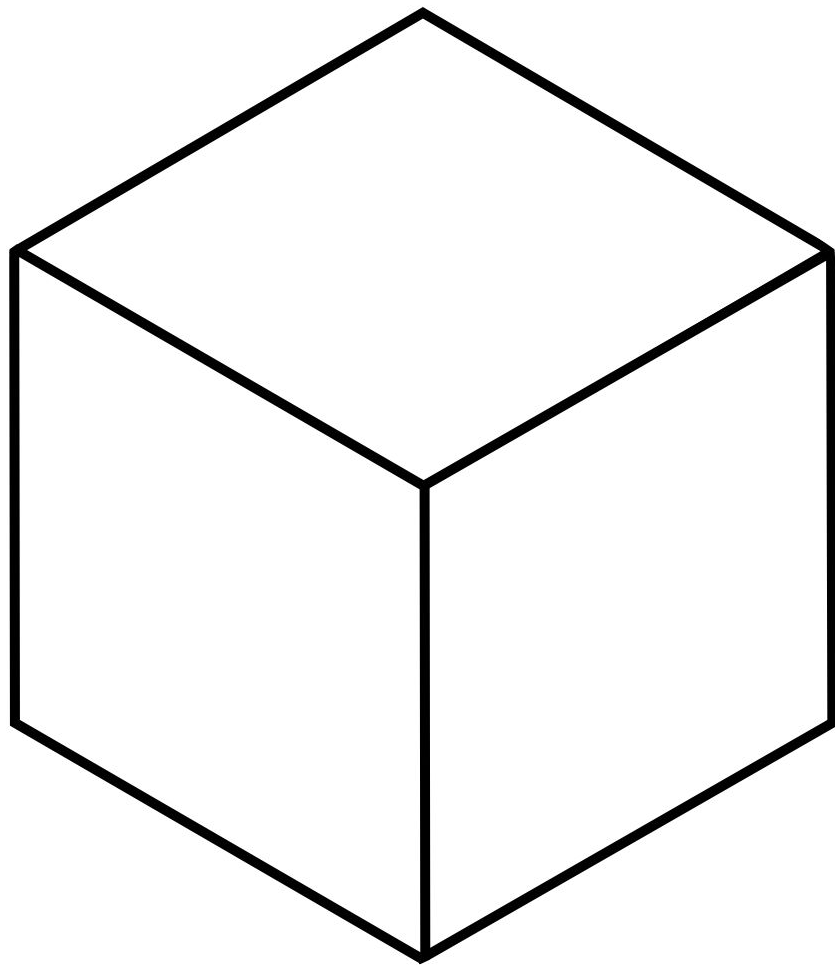


# CS50 for JDs

Algorithms, Data Structures

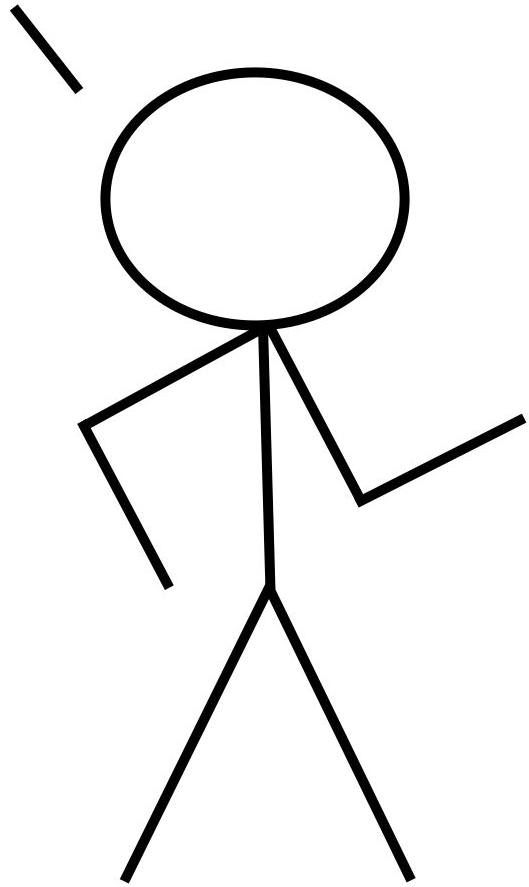
abstraction







Hi



seminars

# Innovative Algorithms and Their Applications

Fri, Jan 6, 9:00 AM – 11:00 AM EST in WCC Room 1010,  
with Catherine Deskur



shorts





algorithms



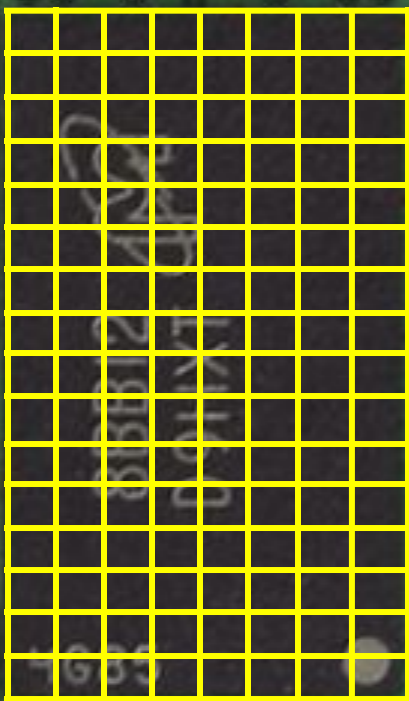
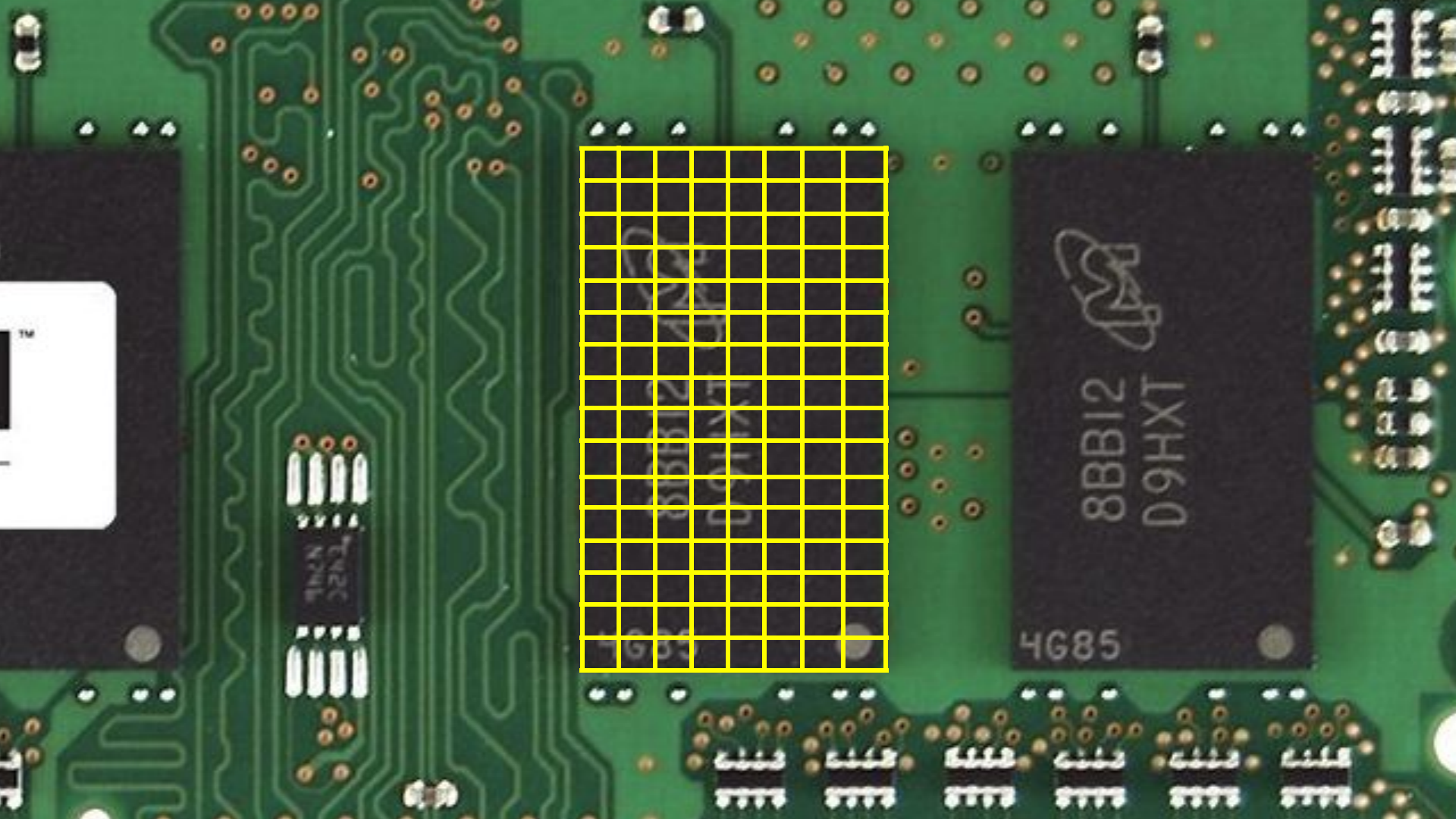
™

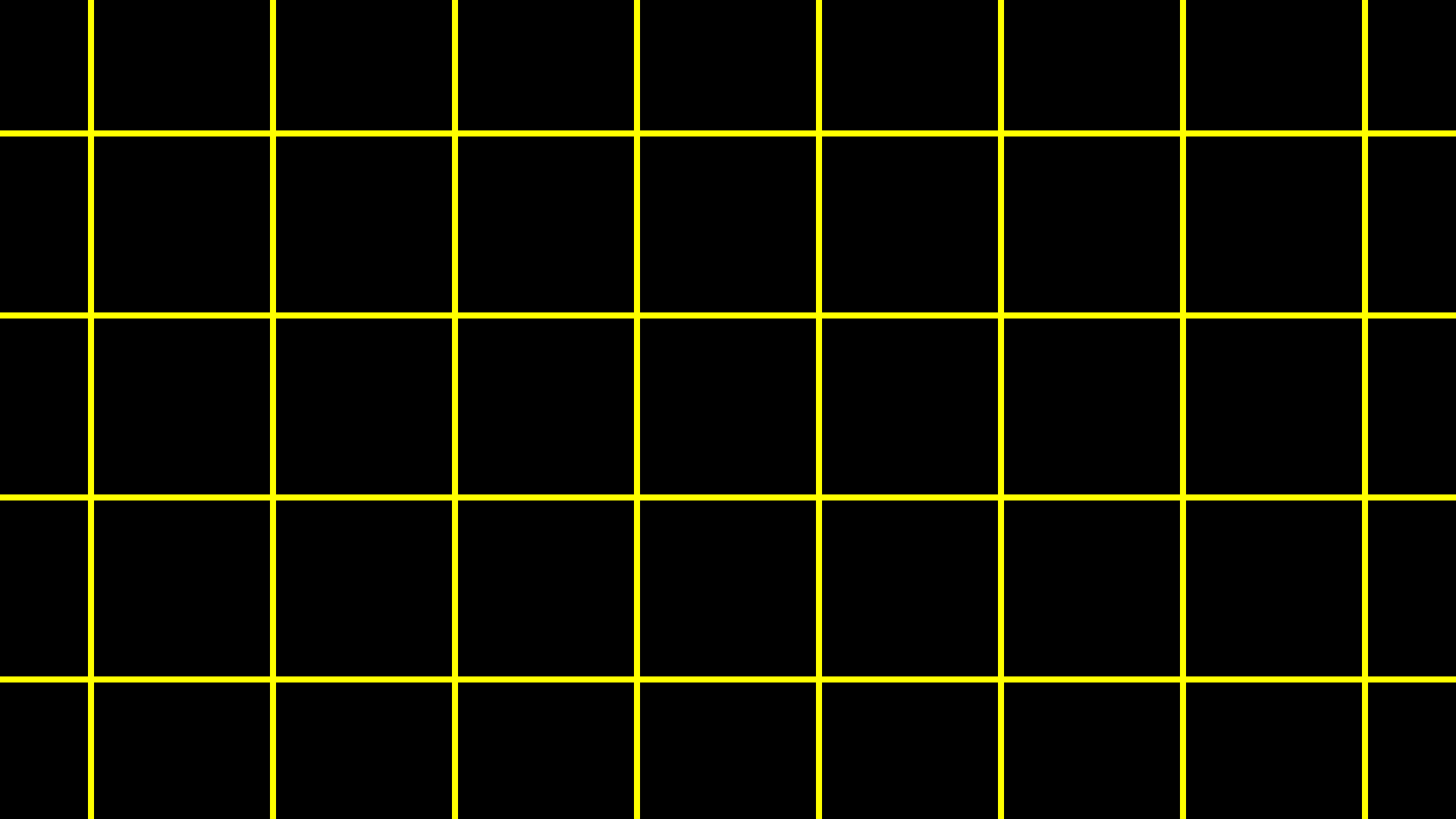
3442  
2502

8BB12  
D9HXT  
4G85

8BB12  
D9HXT  
4G85

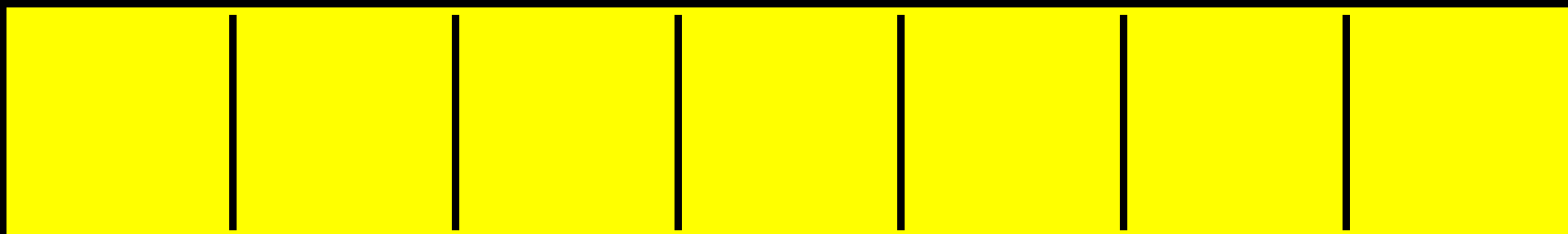






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linear search



```
For each door from left to right
  If number is behind door
    Answer is true
  Else
    Answer is false
```

binary search

```
If number behind middle door
    Return true
Else if number < middle door
    Search left half
Else if number > middle door
    Search right half
```

If no doors

If number behind middle door

Return true

Else if number < middle door

Search left half

Else if number > middle door

Search right half

If no doors

    Return false

If number behind middle door

    Return true

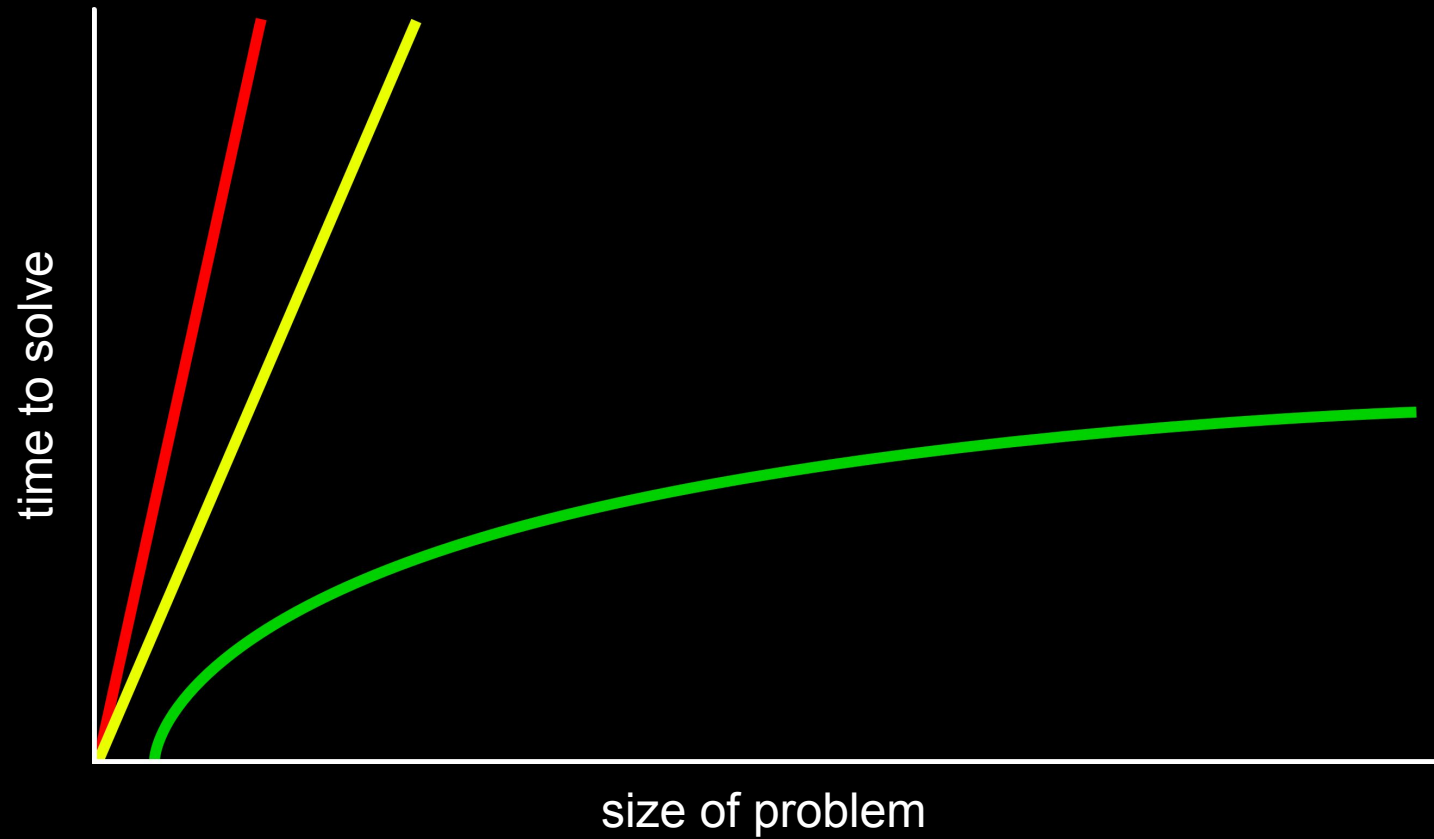
Else if number < middle door

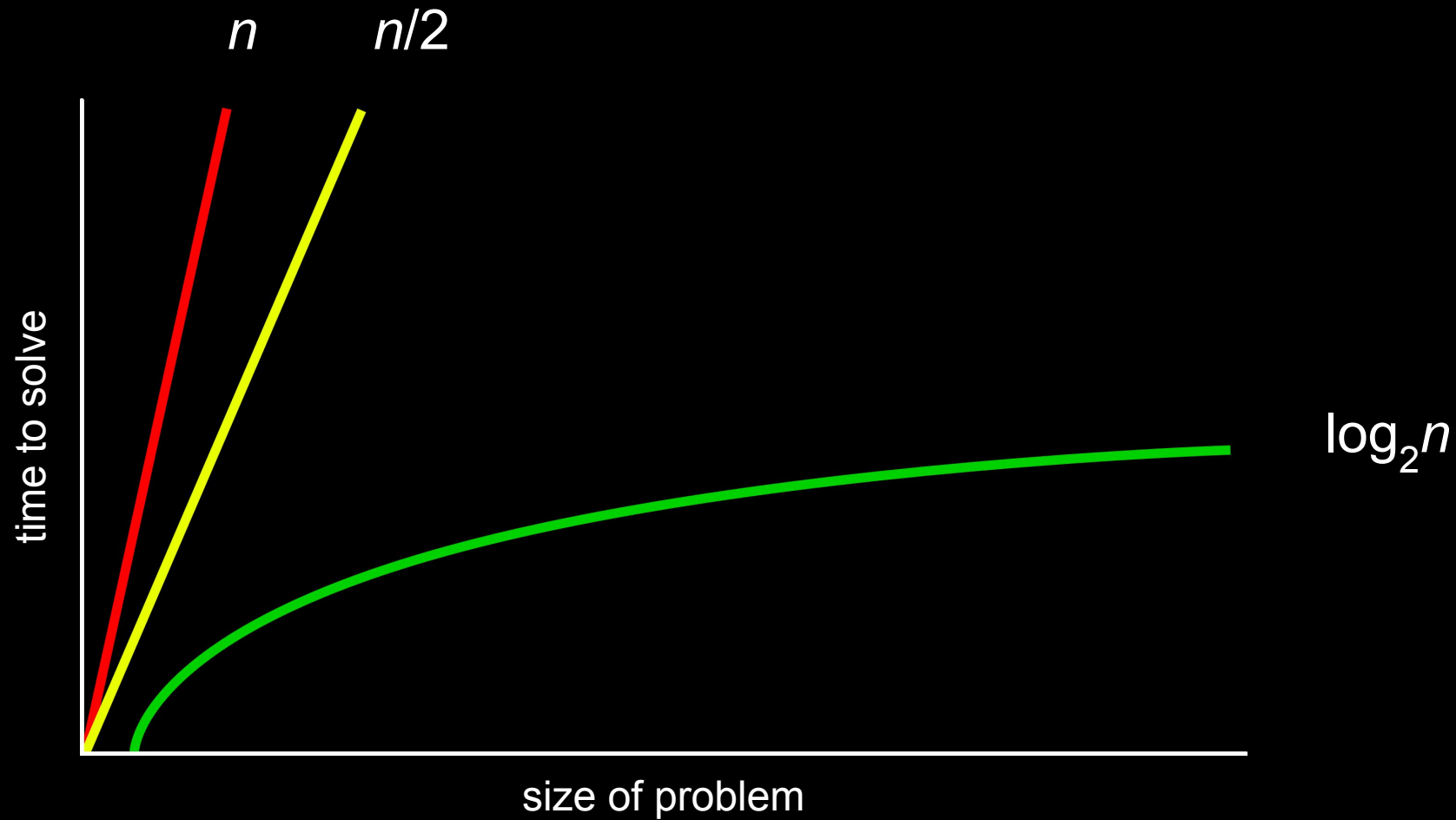
    Search left half

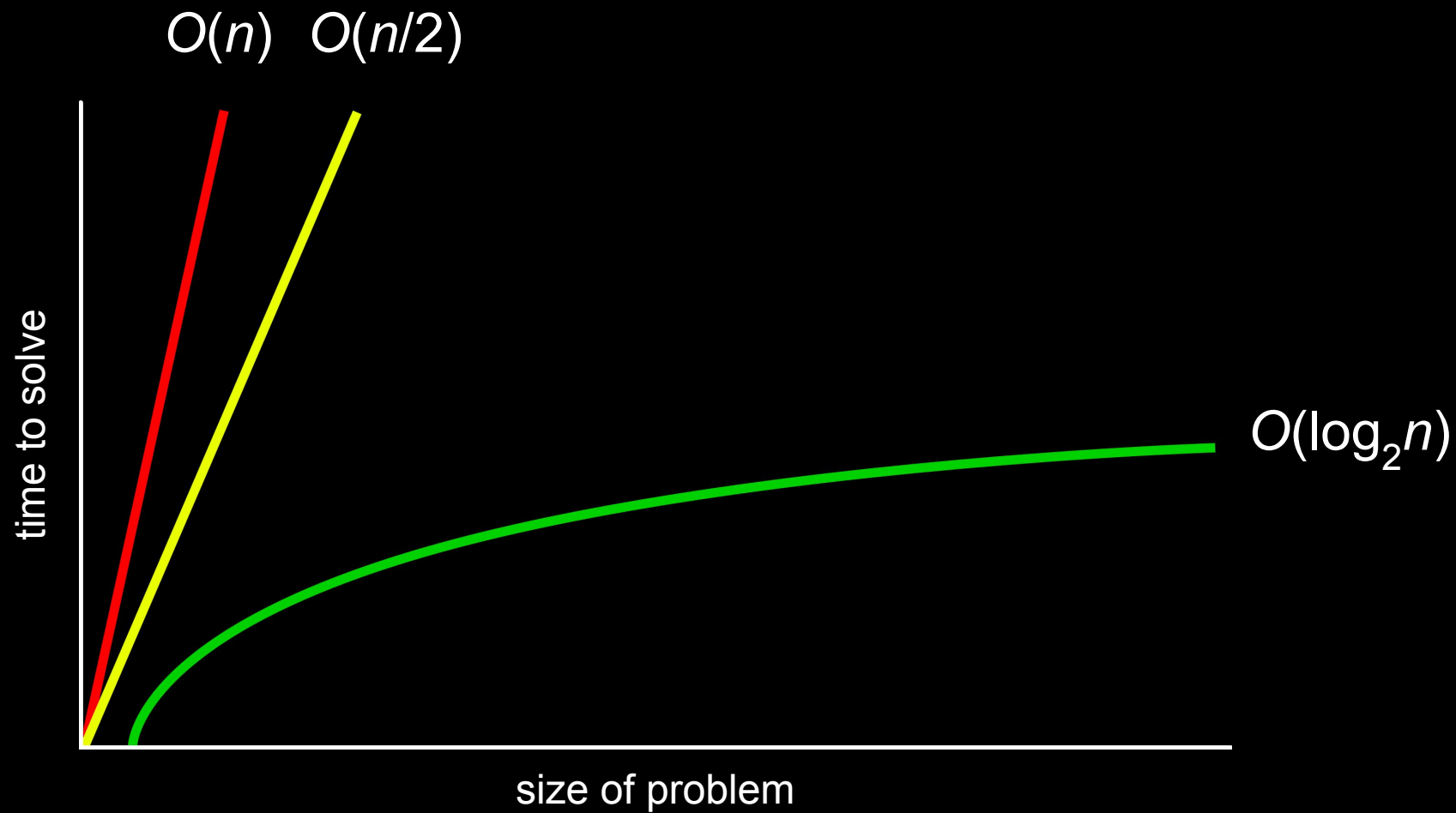
Else if number > middle door

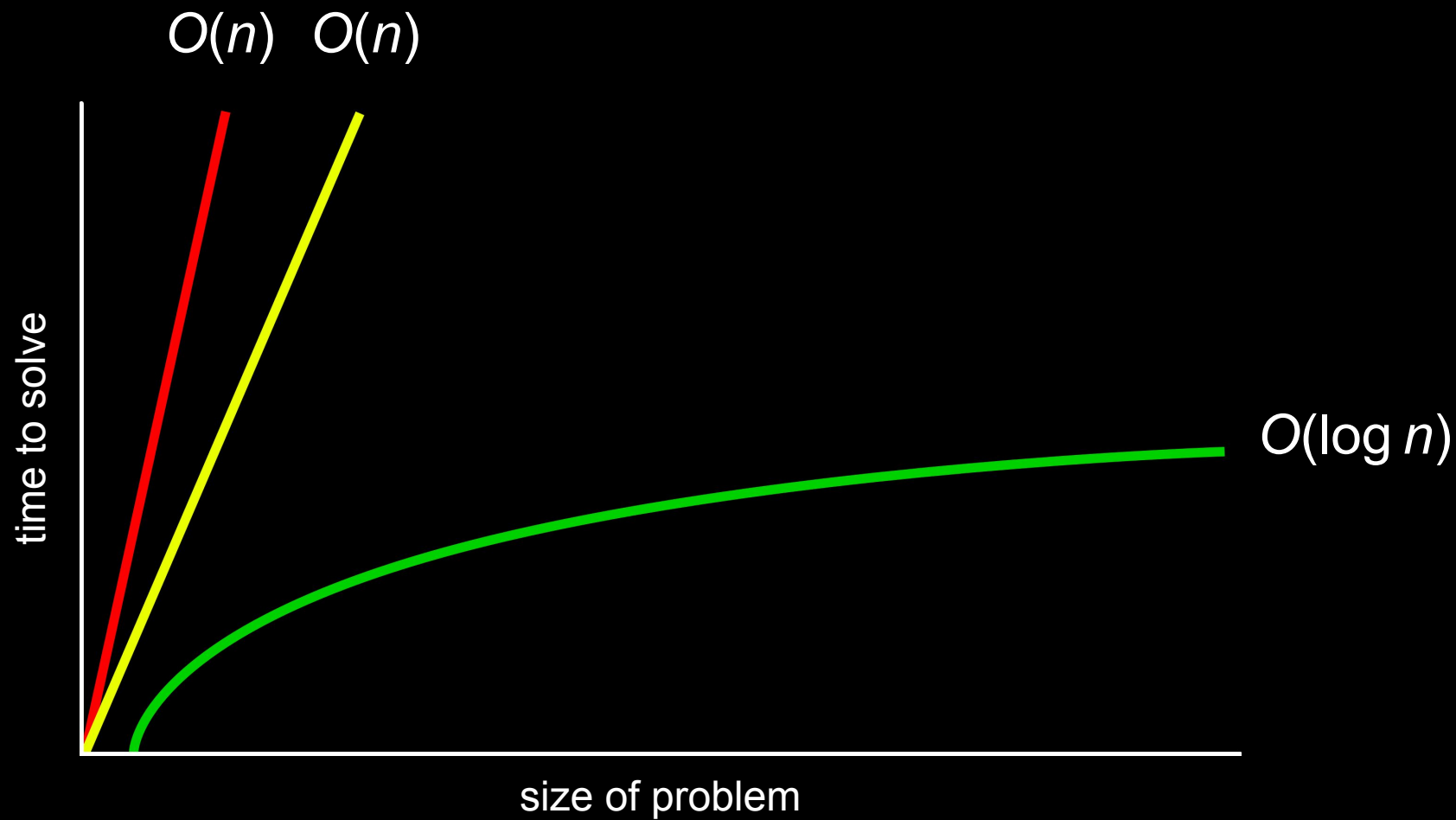
    Search right half











$$O(n^2)$$

$$O(n \log n)$$

$$O(n)$$

$$O(\log n)$$

$$O(1)$$

$O(n^2)$

$O(n \log n)$

$O(n)$           linear search

$O(\log n)$       binary search

$O(1)$

$$\Omega(n^2)$$

$$\Omega(n \log n)$$

$$\Omega(n)$$

$$\Omega(\log n)$$

$$\Omega(1)$$

$\Omega(n^2)$

$\Omega(n \log n)$

$\Omega(n)$

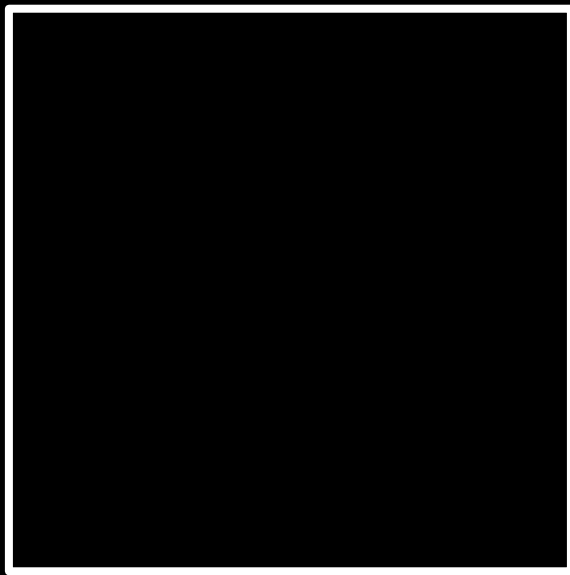
$\Omega(\log n)$

$\Omega(1)$       linear search, binary search



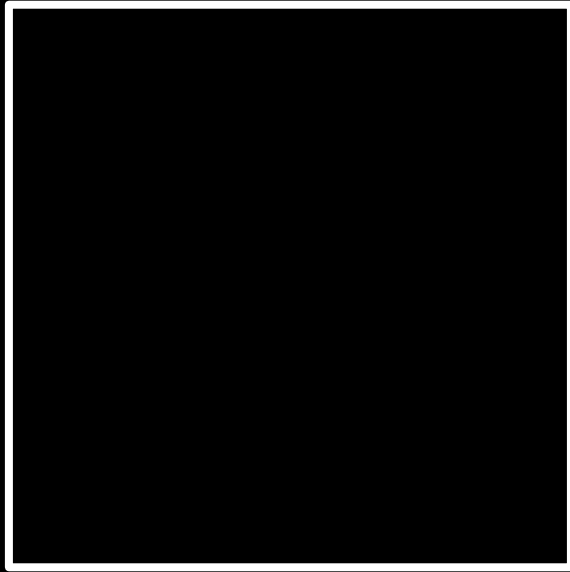


unsorted →



→ output

unsorted →



→ sorted

6 3 8 5 2 7 4 1

selection sort

For  $i$  from 0 to  $n-1$

Find smallest item between  $i$ 'th item and last item

Swap smallest item with  $i$ 'th item



$$(n - 1)$$



$$(n - 1) + (n - 2)$$

$$(n - 1) + (n - 2) + (n - 3)$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$n^2/2 - n/2$$

$$(n - 1) + (n - 2) + (n - 3) + \dots + 1$$

$$n(n - 1)/2$$

$$(n^2 - n)/2$$

$$n^2/2 - n/2$$

$$O(n^2)$$

$O(n^2)$       selection sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$



$\Omega(n^2)$       selection sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

6 3 8 5 2 7 4 1

bubble sort

Repeat  $n-1$  times

For  $i$  from 0 to  $n-2$

If  $i$ 'th and  $i+1$ 'th elements out of order

Swap them



$$(n-1) \times (n-1)$$

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$



$$(n - 1) \times (n - 1)$$

$$n^2 - 1n - 1n + 1$$

$$n^2 - 2n + 1$$

$$O(n^2)$$

$O(n^2)$  bubble sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$\Omega(n^2)$  bubble sort

$\Omega(n \log n)$

$\Omega(n)$

$\Omega(\log n)$

$\Omega(1)$

bubble sort

Repeat  $n-1$  times

For  $i$  from 0 to  $n-2$

If  $i$ 'th and  $i+1$ 'th elements out of order

Swap them

Repeat until no swaps

For  $i$  from 0 to  $n-2$

If  $i$ 'th and  $i+1$ 'th elements out of order

Swap them

$O(n^2)$  bubble sort

$O(n \log n)$

$O(n)$

$O(\log n)$

$O(1)$

$$\Omega(n^2)$$

$$\Omega(n \log n)$$

$$\Omega(n) \quad \text{bubble sort}$$

$$\Omega(\log n)$$

$$\Omega(1)$$





recursion

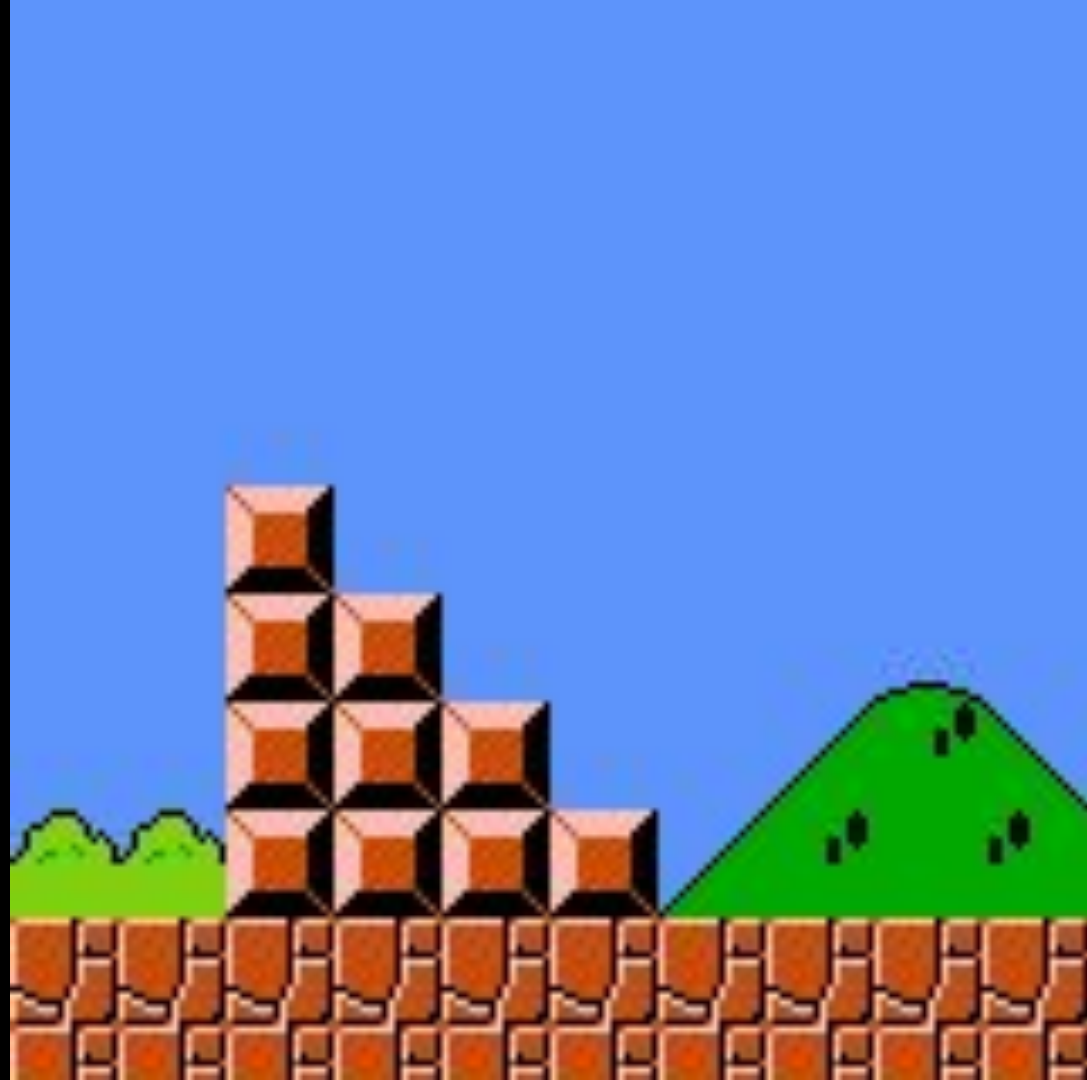
```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Open to middle of left half of book
8      Go back to line 3
9  Else if person is later in book
10     Open to middle of right half of book
11     Go back to line 3
12 Else
13     Quit
```

```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Open to middle of left half of book
8      Go back to line 3
9  Else if person is later in book
10     Open to middle of right half of book
11     Go back to line 3
12 Else
13     Quit
```

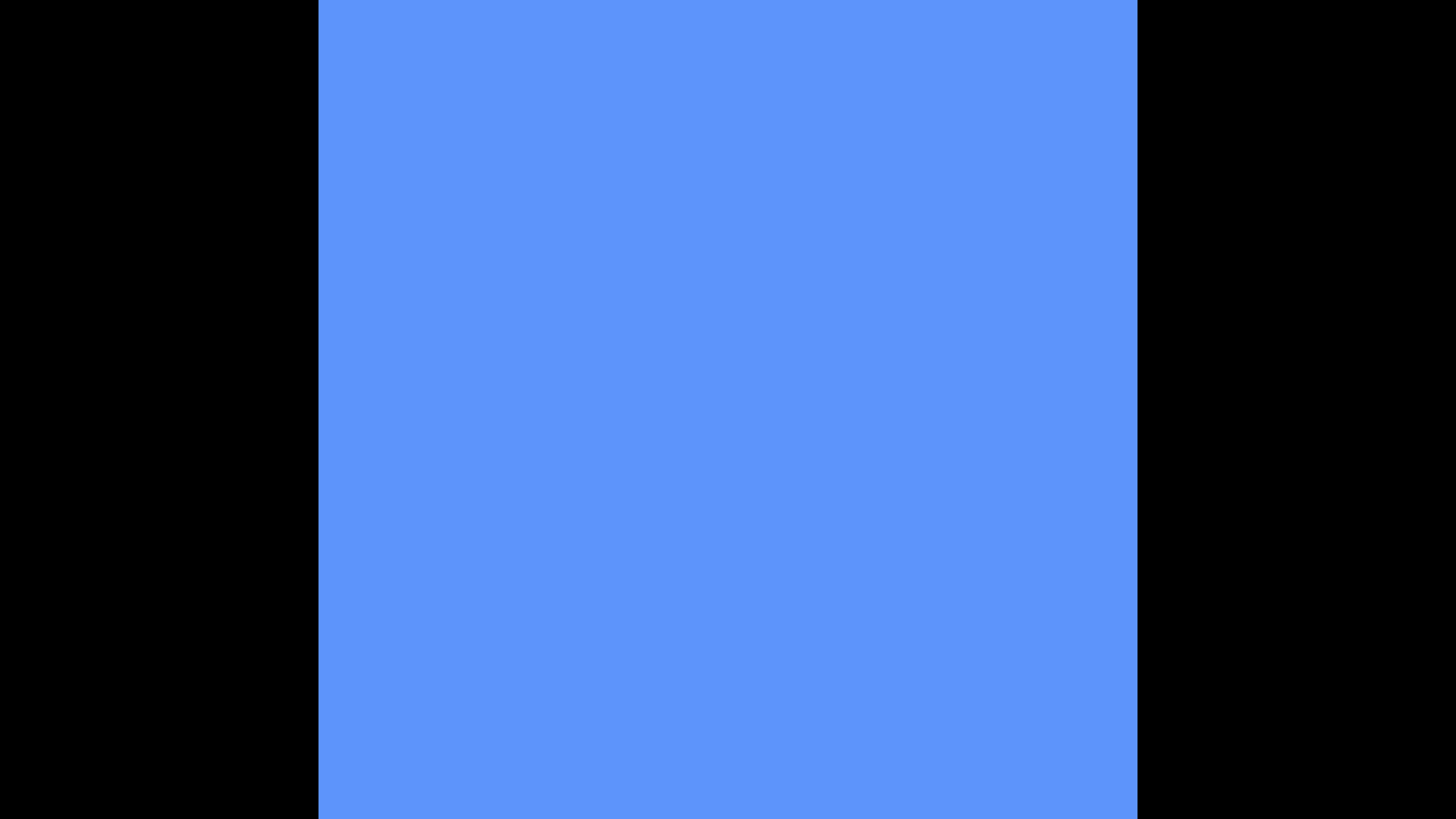
```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Open to middle of left half of book
8      Go back to line 3
9  Else if person is later in book
10     Open to middle of right half of book
11     Go back to line 3
12 Else
13     Quit
```

```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Search left half of book
8
9  Else if person is later in book
10     Search right half of book
11
12 Else
13     Quit
```

```
1  Pick up phone book
2  Open to middle of phone book
3  Look at page
4  If person is on page
5      Call person
6  Else if person is earlier in book
7      Search left half of book
8  Else if person is later in book
9      Search right half of book
10 Else
11     Quit
```















merge sort

If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves

If only one item

Return

Else

Sort left half of items

Sort right half of items

Merge sorted halves



7 4 5 2 6 3 8 1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

4

5

2

6

3

8

1

7

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5

2

6

3

8

1

7

5

2

6

3

8

1

4

5 2 6 3 8 1

4 7



5

2

6

3

8

1

4

7

5

2

6

3

8

1

4

7

5

2

6

3

8

1

4

7

5 2 6 3 8 1

4 7

5

6

3

8

1

4

7

2

6 3 8 1

4 7 2 5

6 3 8 1

4	7	2	5
---	---	---	---

6 3 8 1

4 7

5

2



6 3 8 1

7

5

2

4

6 3 8 1

7

2 4 5

6 3 8 1

2 4 5 7

6 3 8 1

2 4 5 7

6

3

8

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2 4 5 7

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3 6

2 4 5 7

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3 6

2 4 5 7

8

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1

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3

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8

2

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1

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1

3

6

8

2	4	5	7	1	3	6	8
---	---	---	---	---	---	---	---

2 4 5 7

3 6 8

1

4 5 7

3 6 8

1 2



4 5 7

6 8

1 2 3

1 2 3 4

5 7

6 8

7

6

8

1

2

3

4

5

7

8

1

2

3

4

5

6

8

1

2

3

4

5

6

7

1 2 3 4 5 6 7 8



7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---



7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

2	4	5	7	1	3	6	8
---	---	---	---	---	---	---	---

7	4	5	2	6	3	8	1
---	---	---	---	---	---	---	---

4	7	2	5	3	6	1	8
---	---	---	---	---	---	---	---

2	4	5	7	1	3	6	8
---	---	---	---	---	---	---	---

1	2	3	4	5	6	7	8
---	---	---	---	---	---	---	---

$O(n^2)$

$O(n \log n)$     merge sort

$O(n)$

$O(\log n)$

$O(1)$

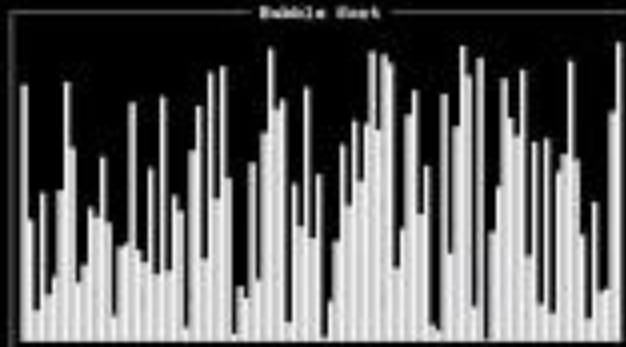
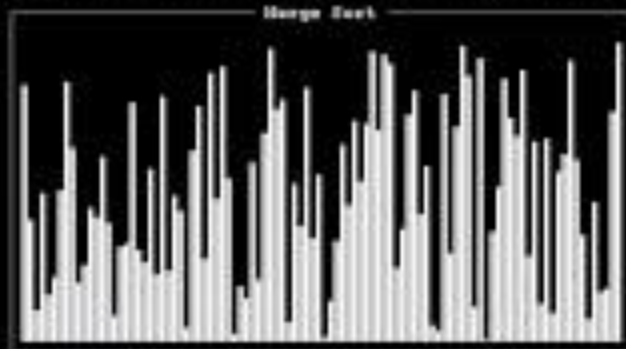
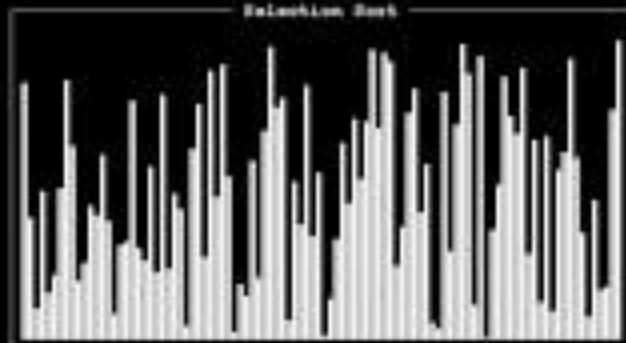
$$\Omega(n^2)$$

$$\Omega(n \log n) \quad \text{merge sort}$$

$$\Omega(n)$$

$$\Omega(\log n)$$

$$\Omega(1)$$





data structures



bool	Boolean value
float	floating-point value
int	integer
str	string
...	

dict

list

range

set

tuple

...





8BB12  
D9HXT

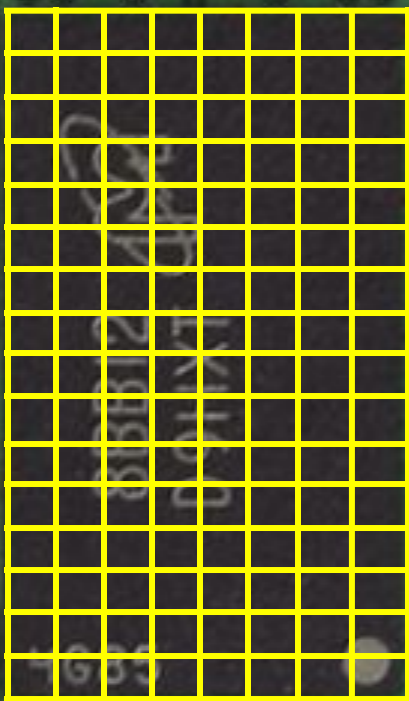
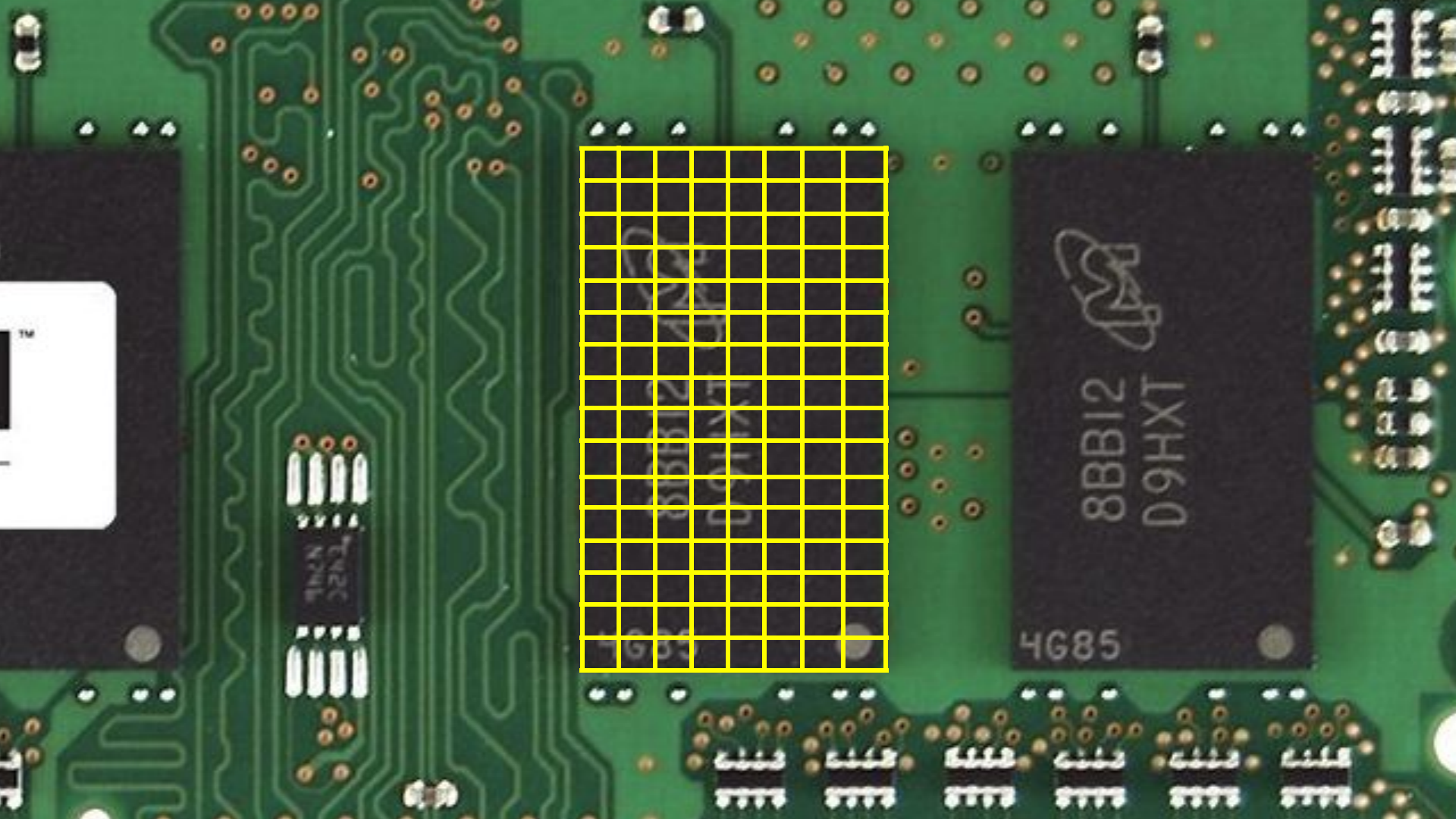
4G85

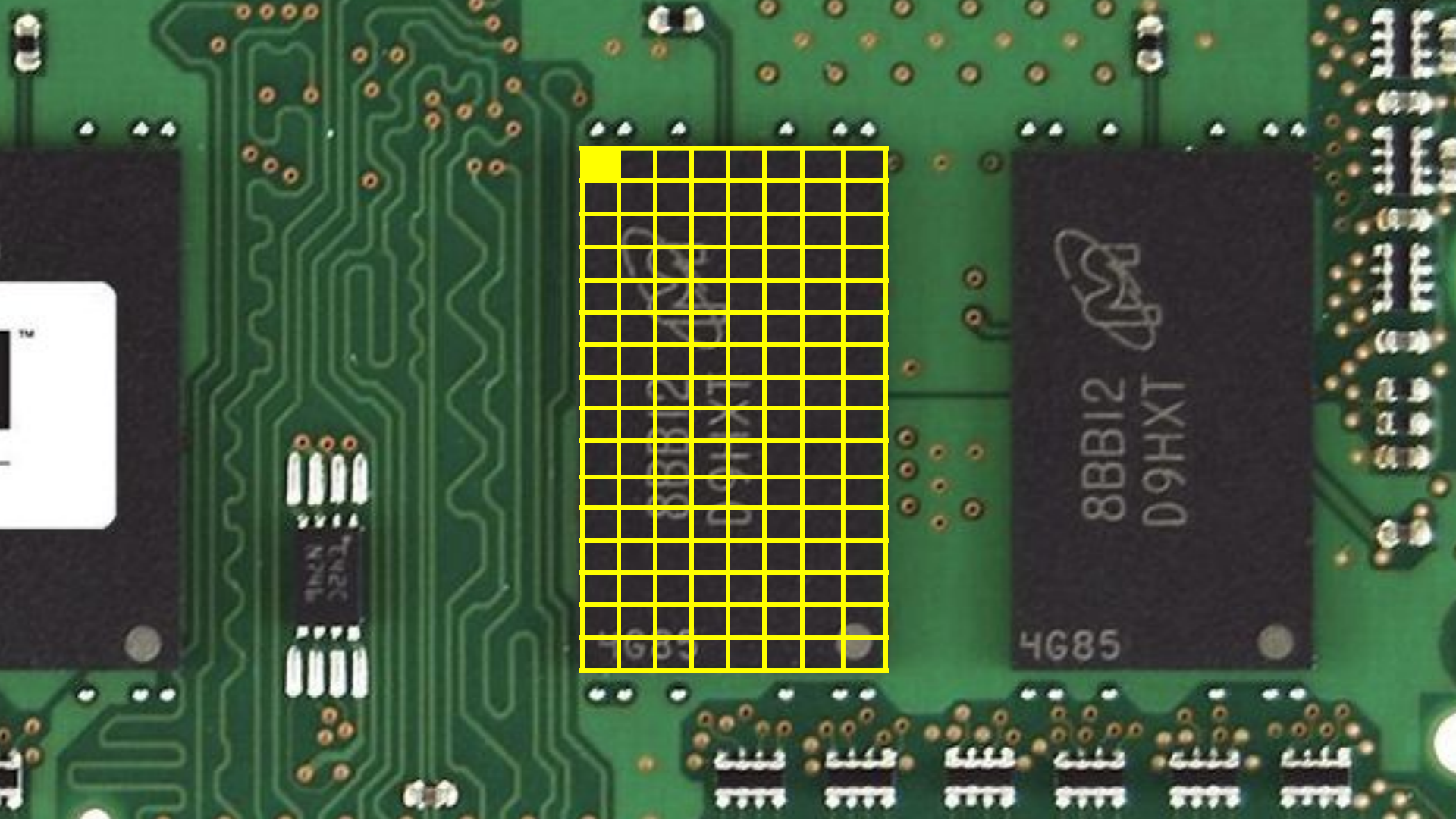


8BB12  
D9HXT

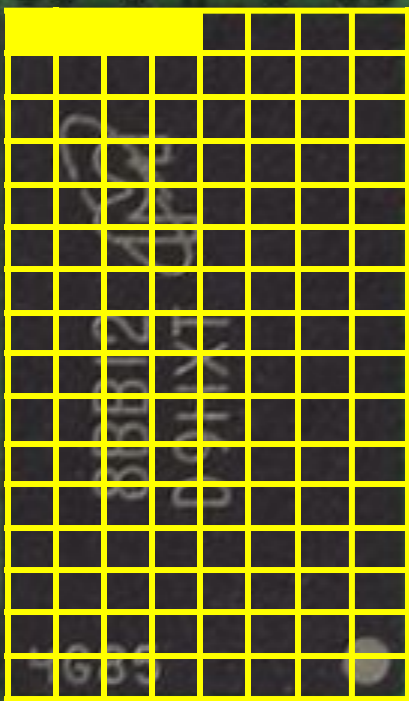
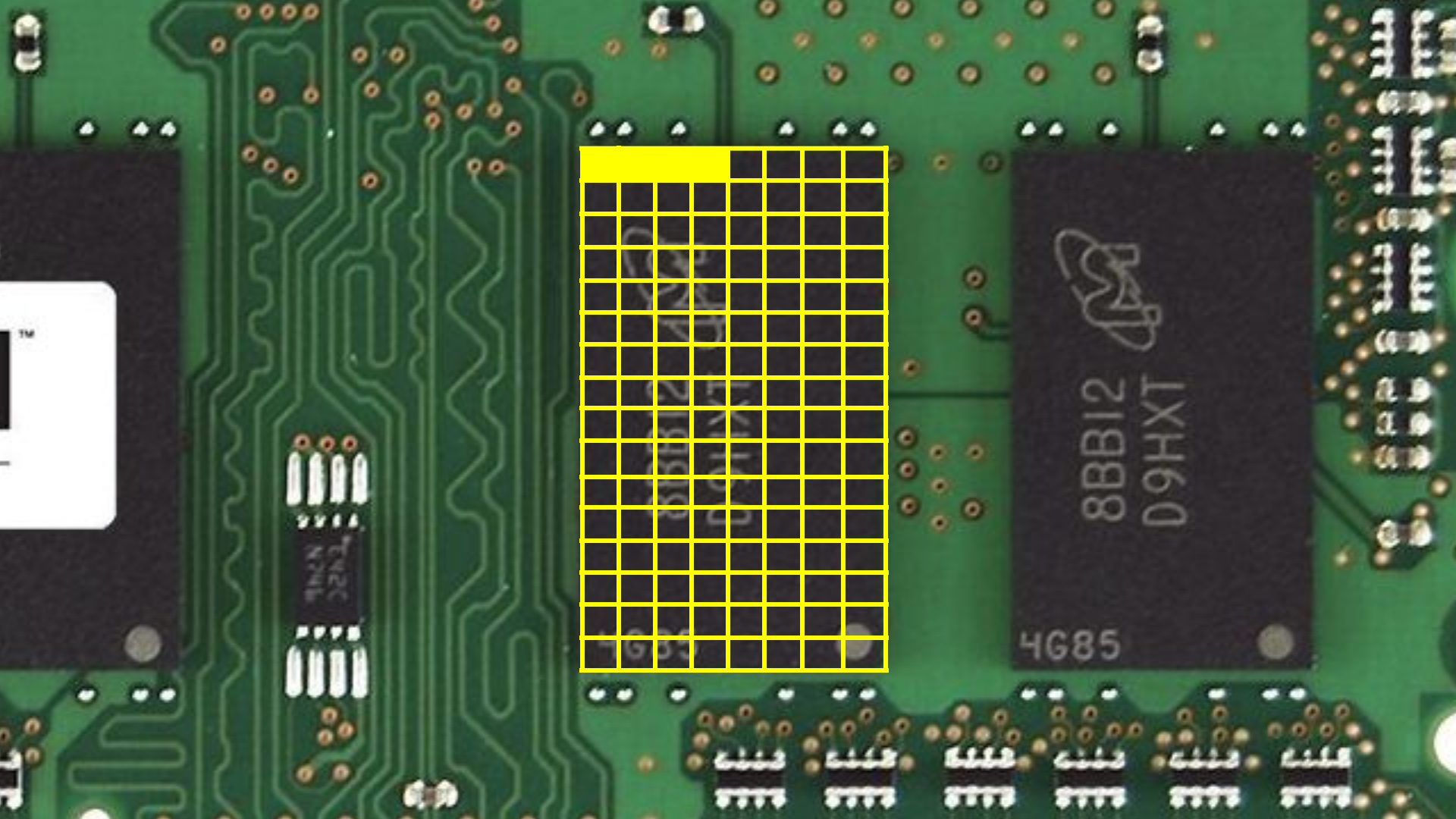
4G85

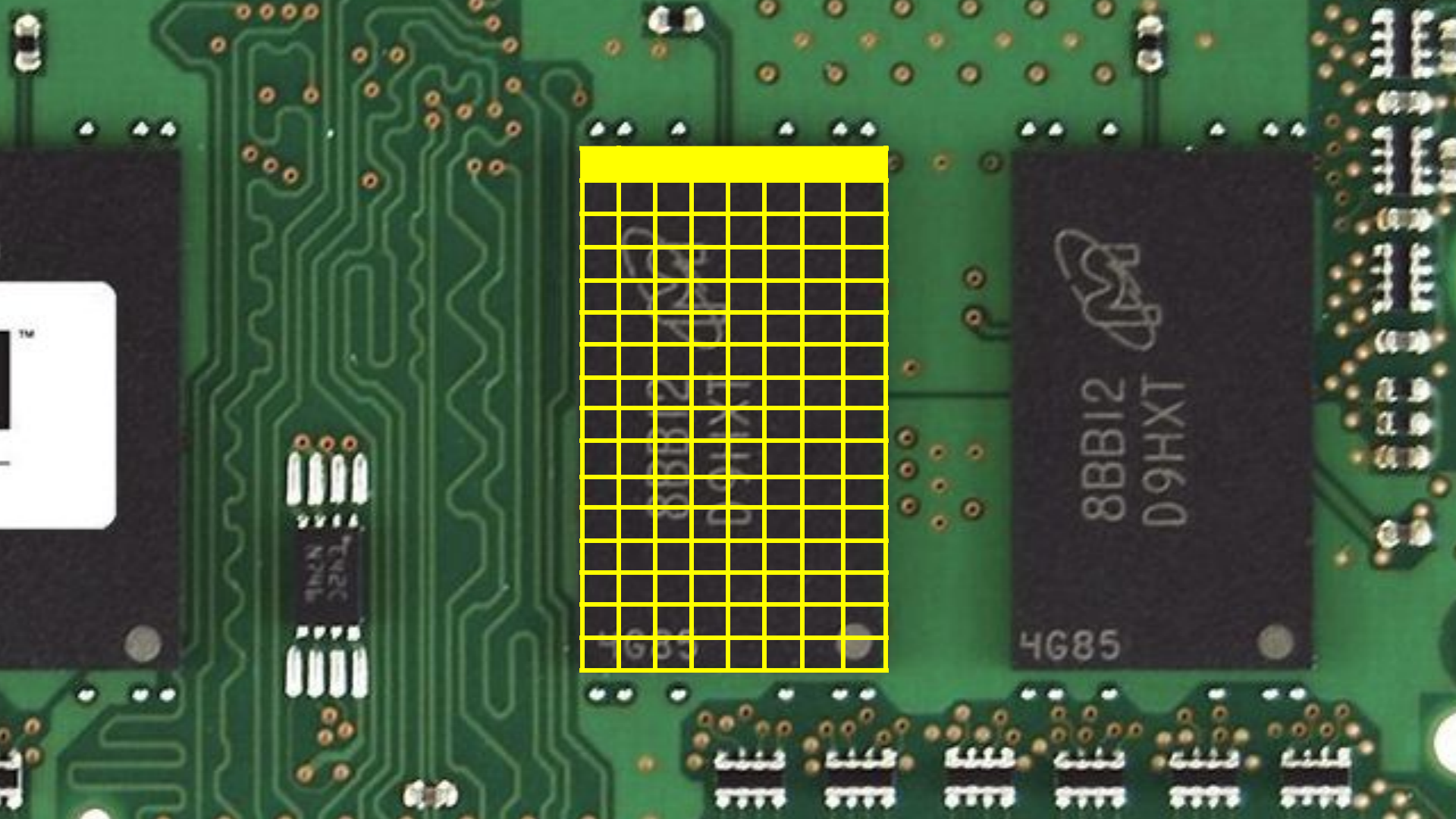














arrays





8BB12  
D9HXT

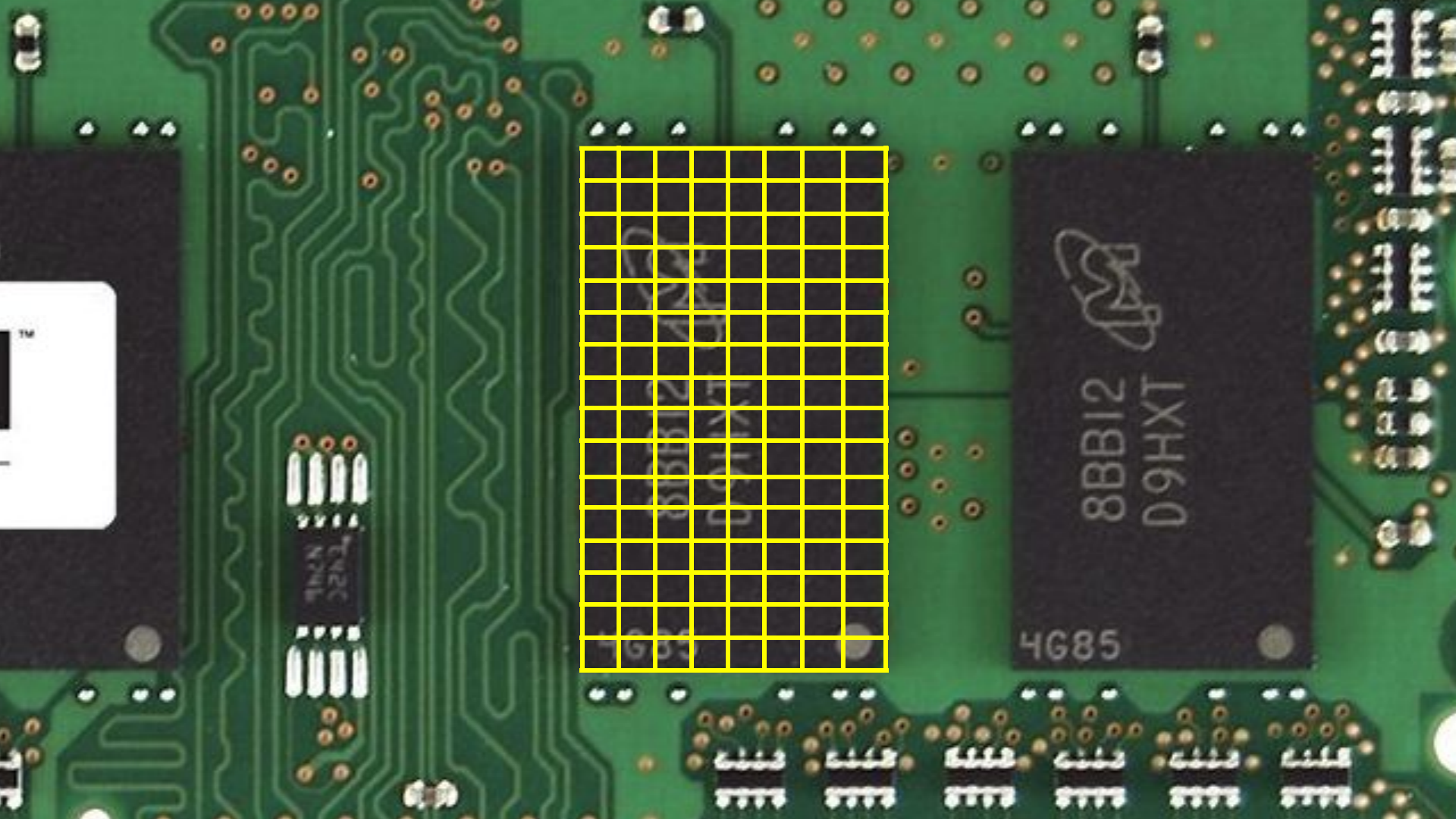
4G85

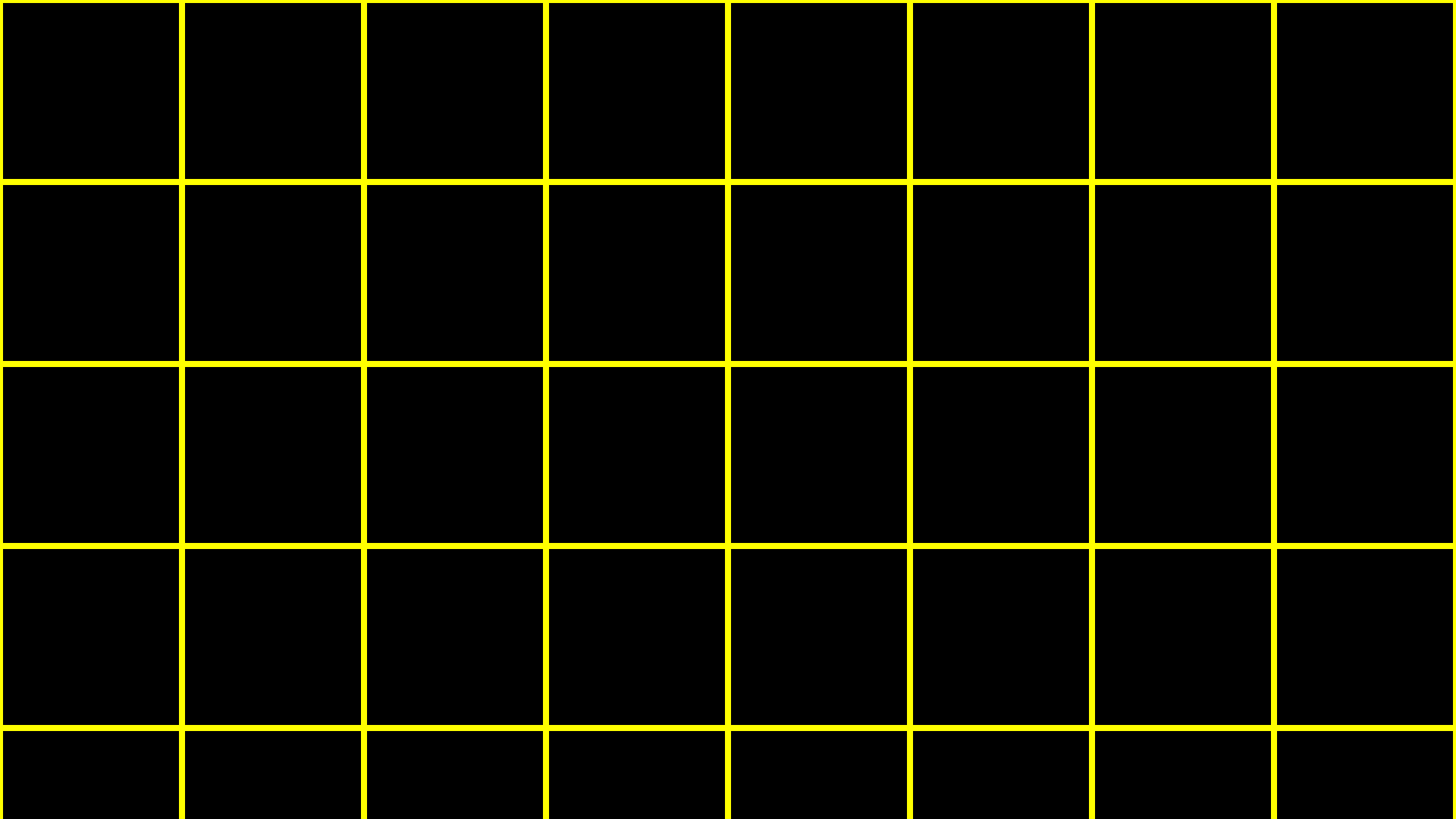


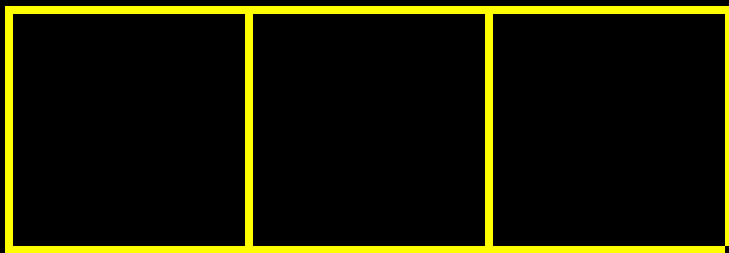
8BB12  
D9HXT

4G85







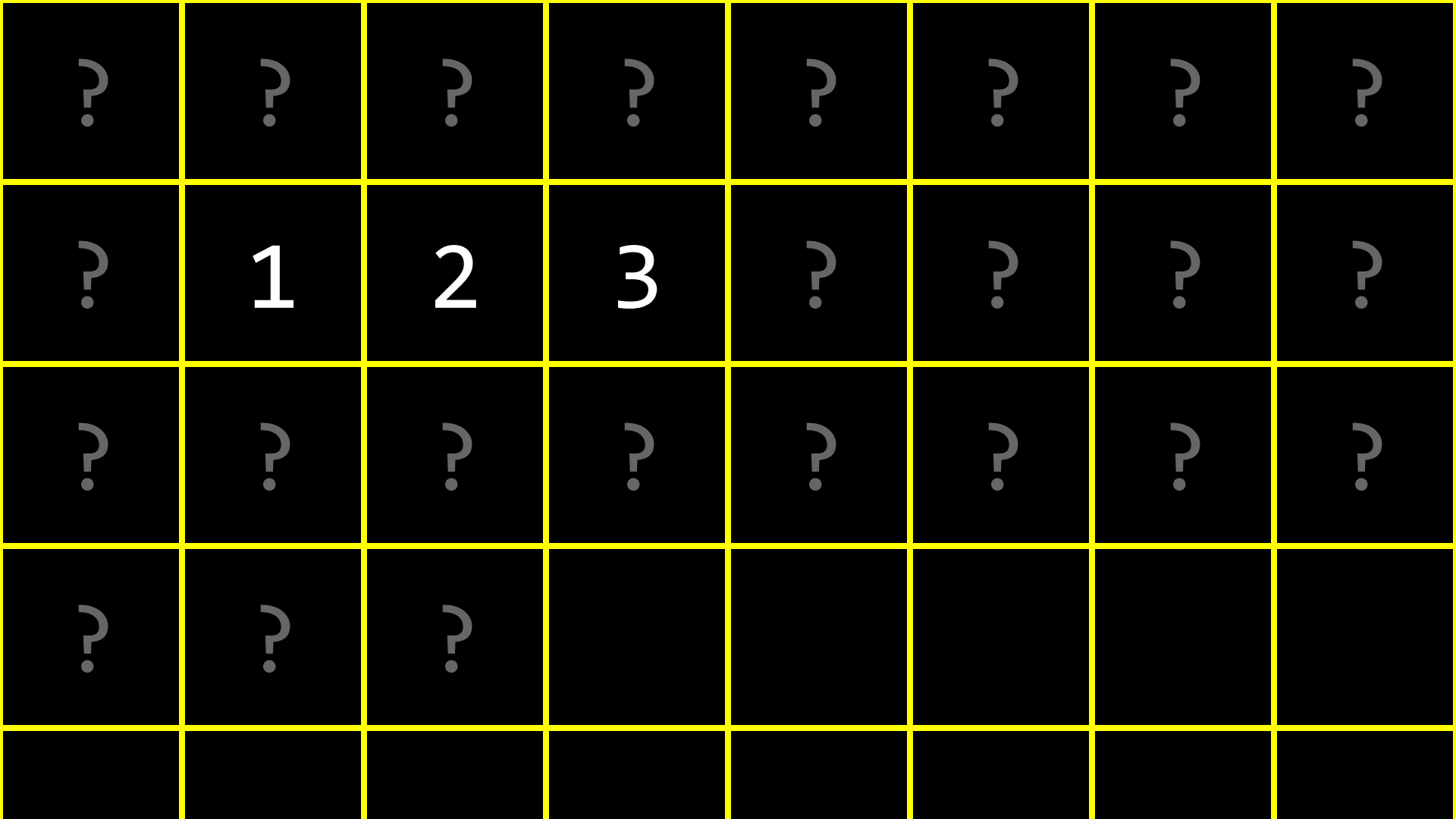


1	2	3
---	---	---

1	2	3	
---	---	---	--



	1	2	3				



1	2	3
---	---	---

--	--	--	--

1	2	3
---	---	---

1			
---	--	--	--

1	2	3
---	---	---

1	2		
---	---	--	--

1	2	3
---	---	---

1	2	3	
---	---	---	--

1

2

3

1

2

3

4



$$O(n^2)$$

$$O(n \log n)$$

$$O(n)$$

$$O(\log n)$$

$$O(1)$$

$O(n^2)$

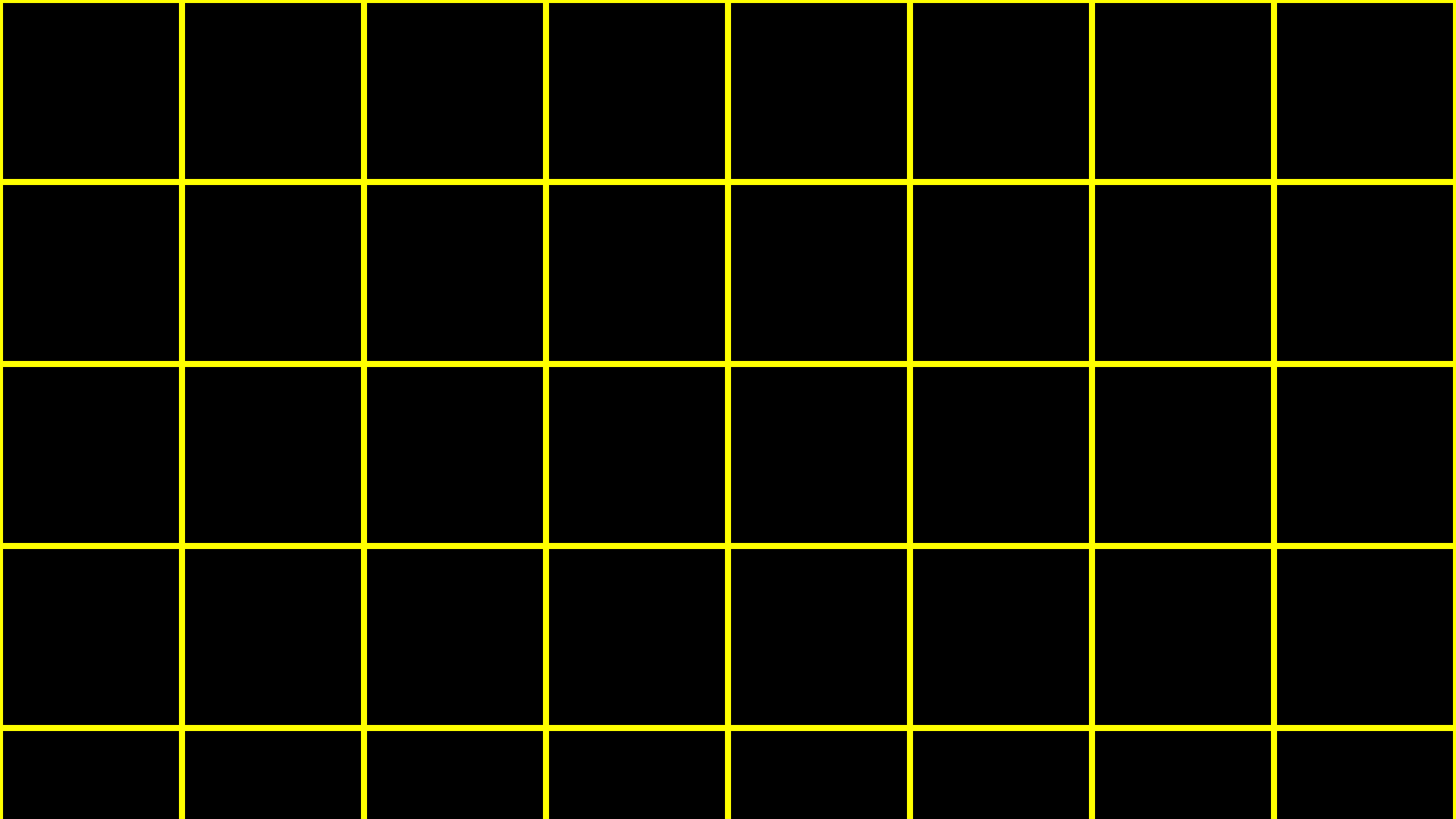
$O(n \log n)$

$O(n)$       insert

$O(\log n)$       search

$O(1)$

linked lists



1

0x123

1

0x123

2

0x456

1

0x123

2

0x456

3

0x789

1

0x123

2

0x456

3

0x789



1

0x123

0x456

2

0x456

3

0x789

1

0x123

0x456

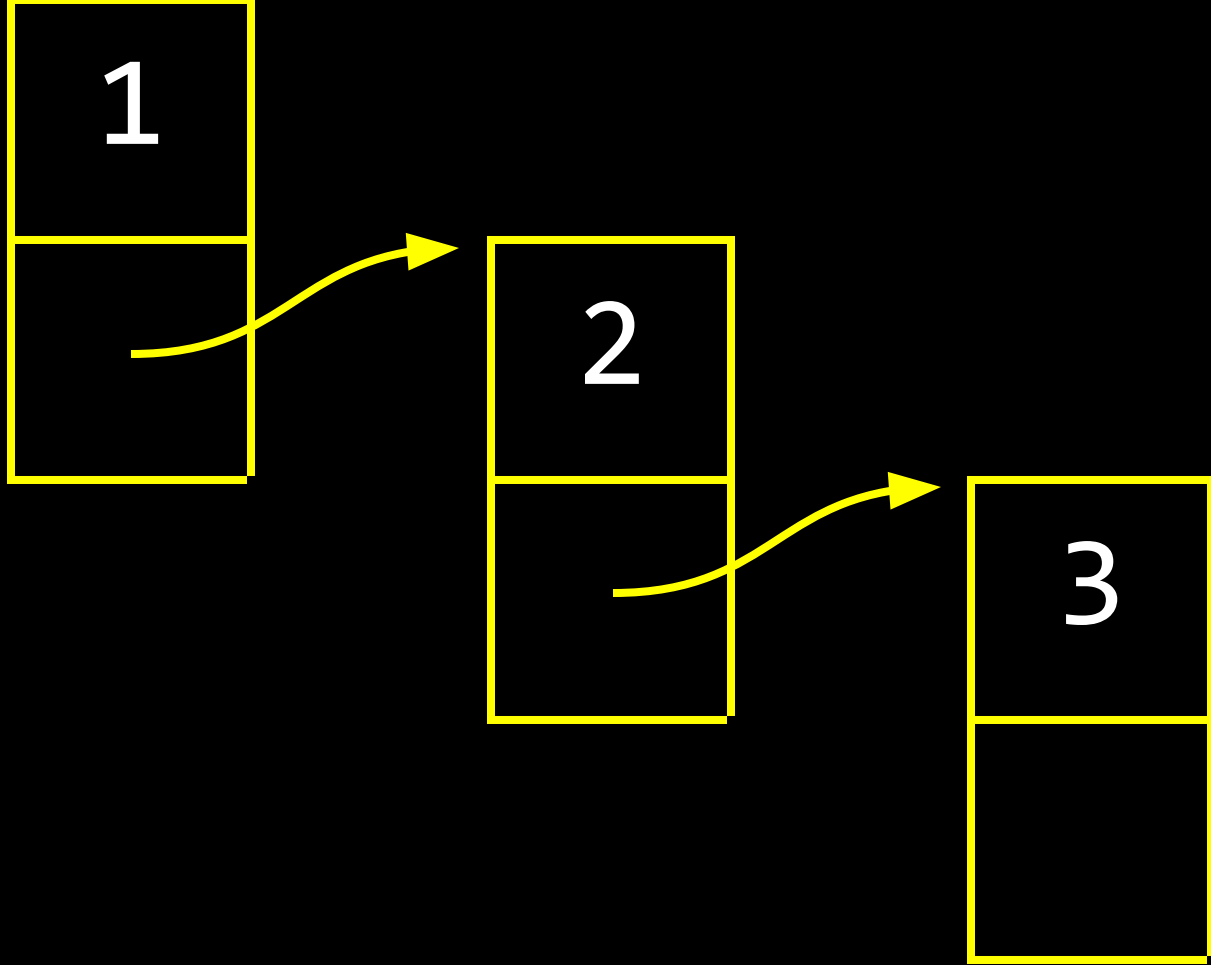
2

0x456

0x789

3

0x789



dict

list

range

set

tuple

...

trees

binary search trees

1

2

3

4

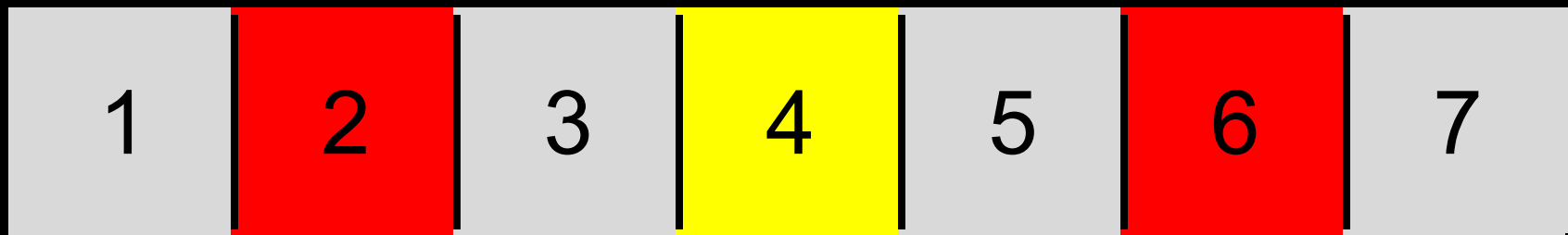
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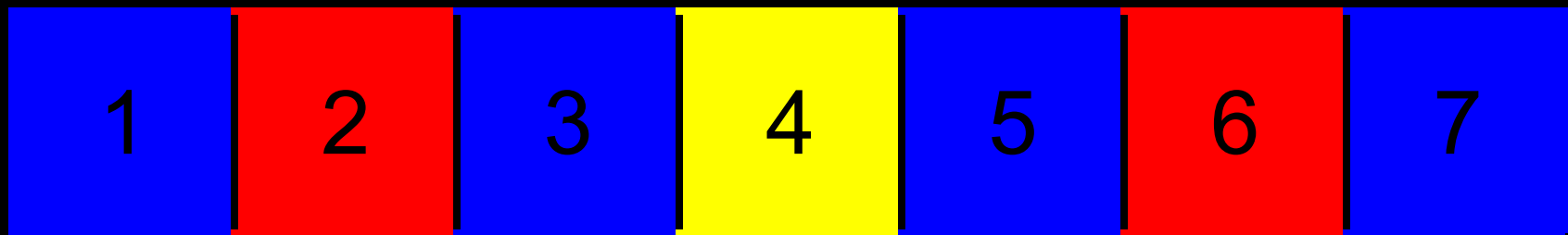
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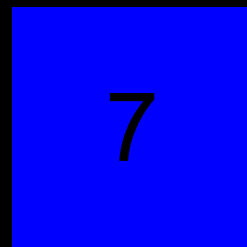
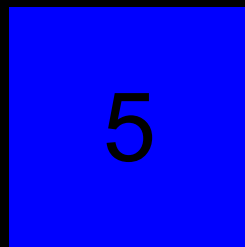
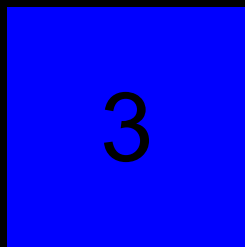
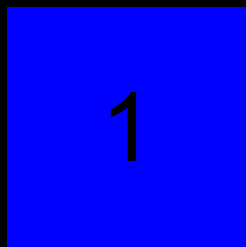
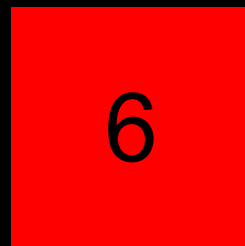
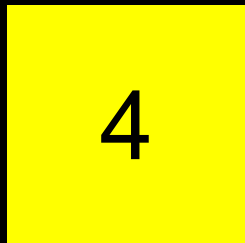
7

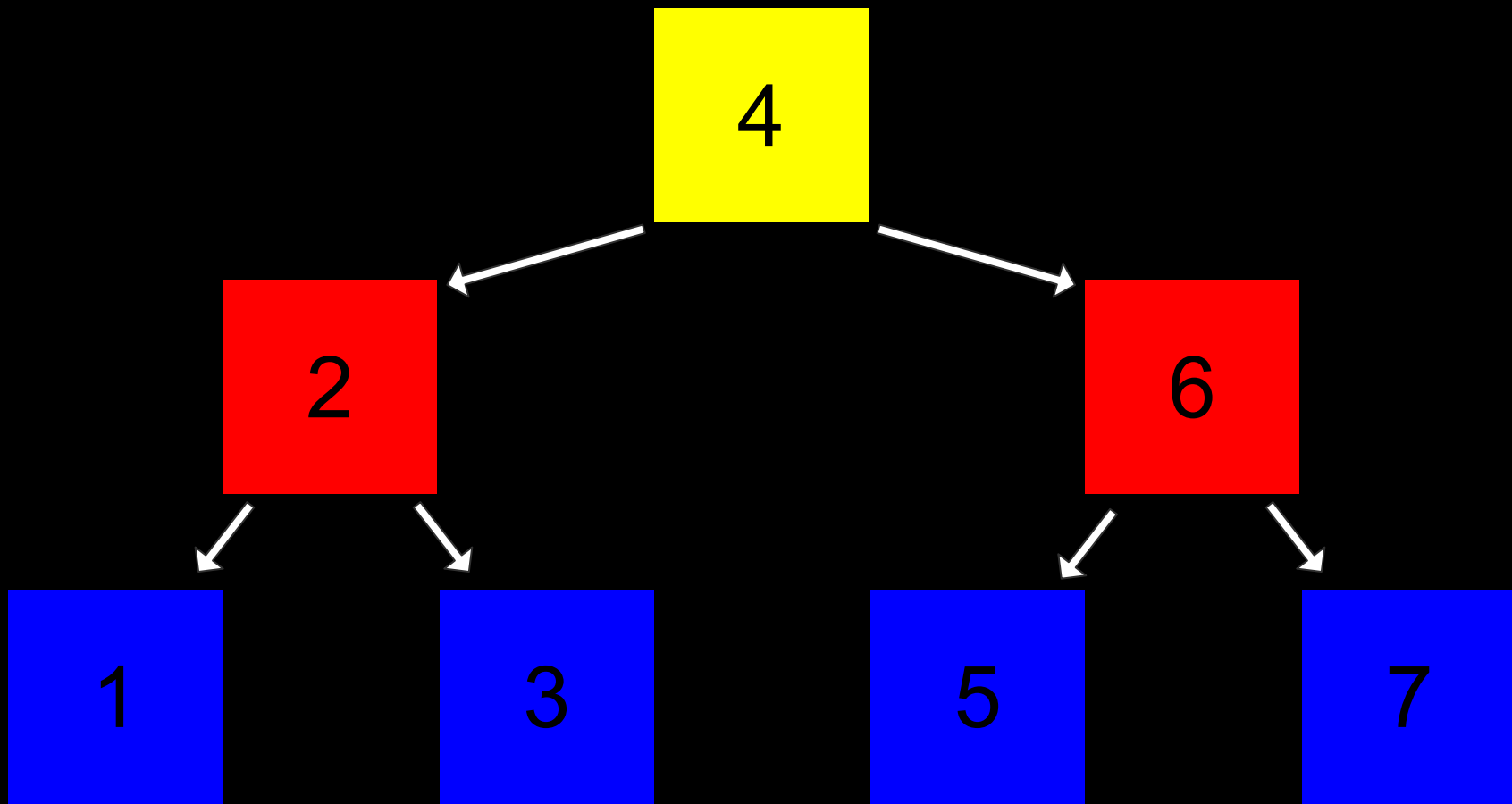
1	2	3	4	5	6	7
---	---	---	---	---	---	---











hash tables

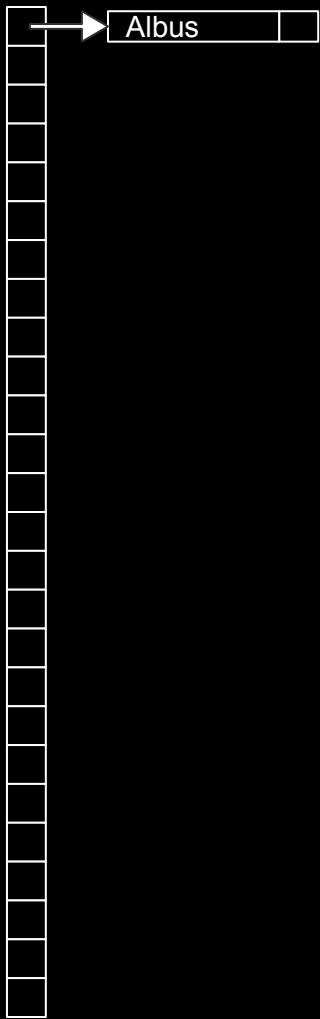
[illegible]

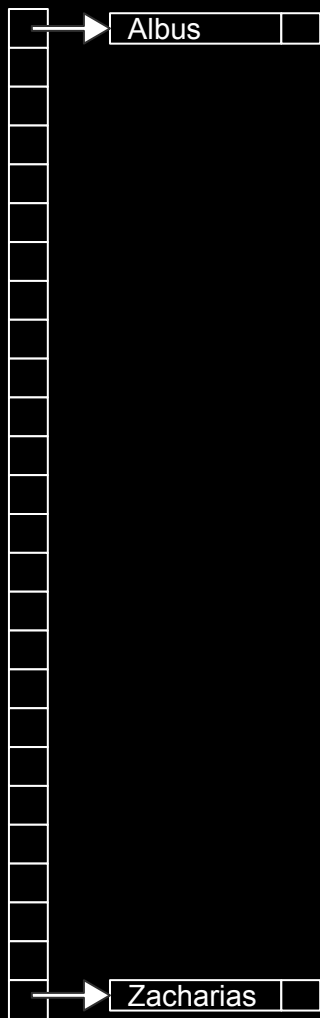
0	
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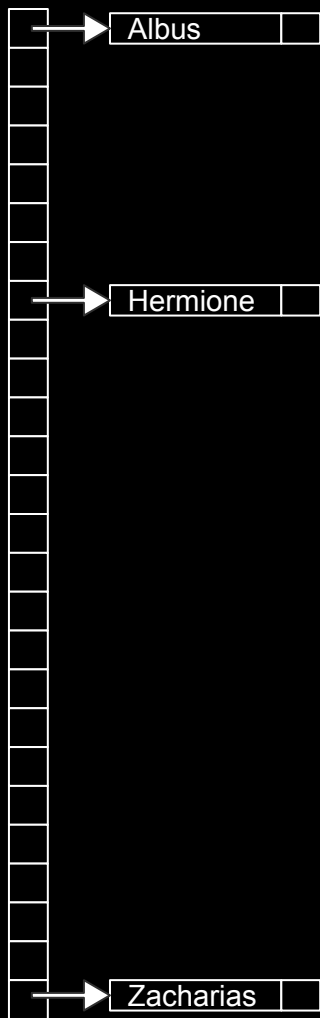
A	
B	
C	
D	
E	
F	
G	
H	
I	
J	
K	
L	
M	
N	
O	
P	
Q	
R	
S	
T	
U	
V	
W	
X	
Y	
Z	

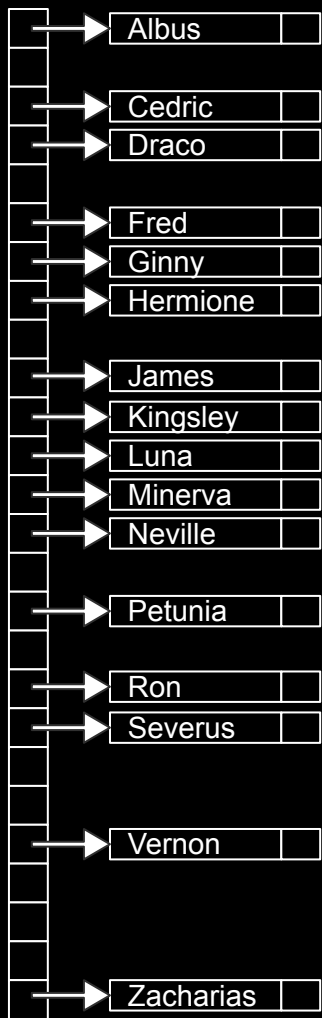


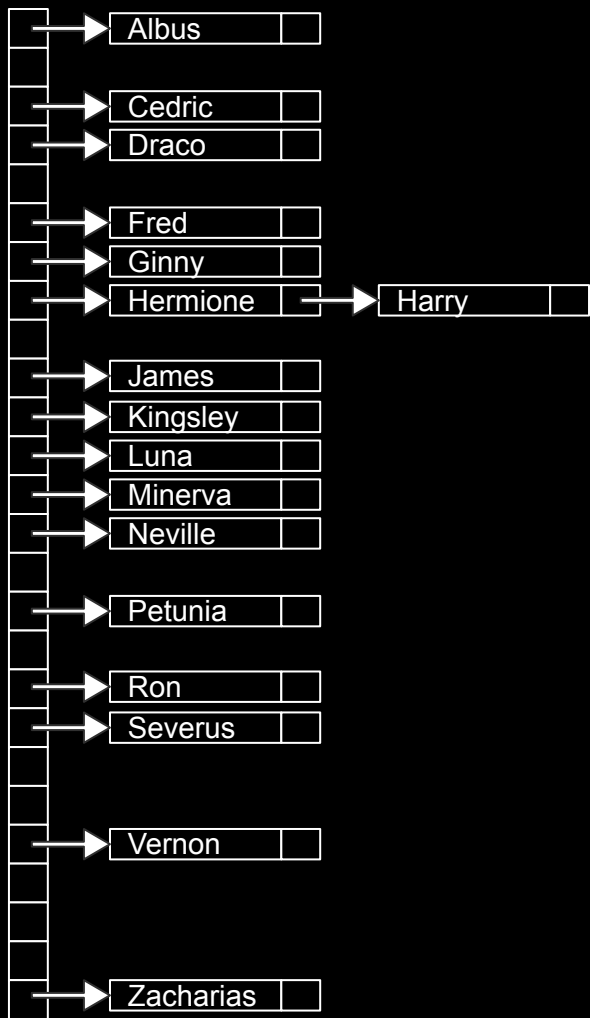
[illegible]

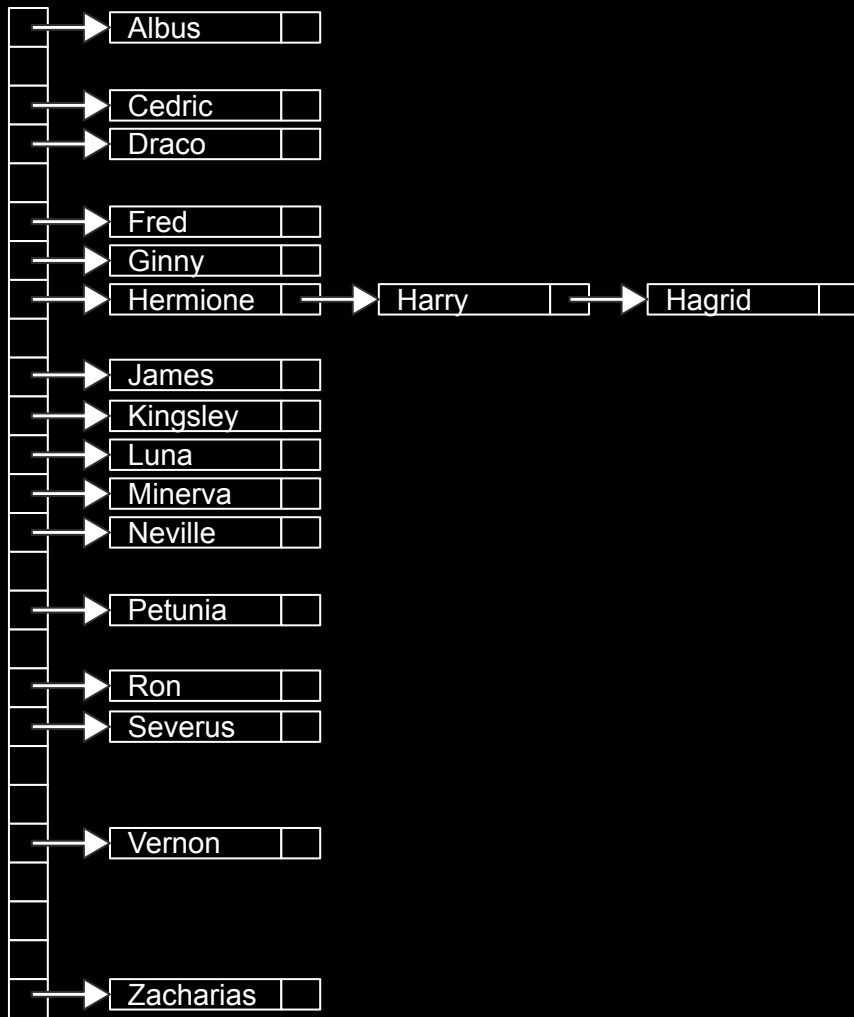


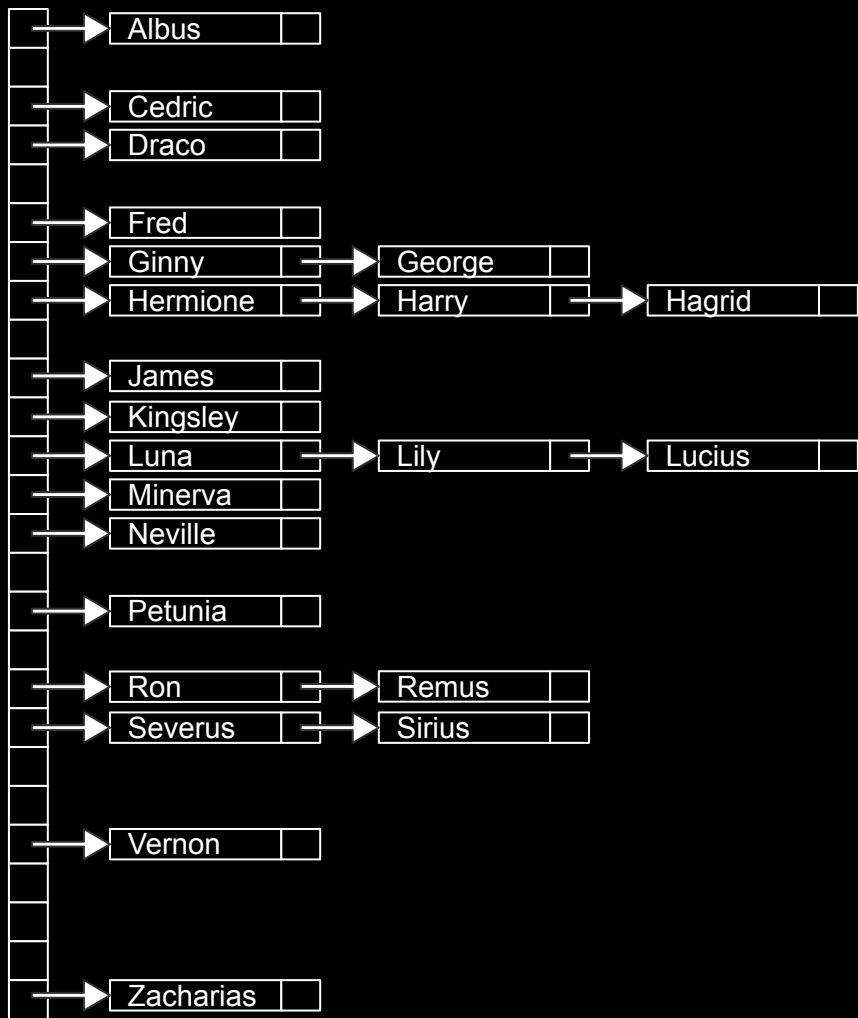










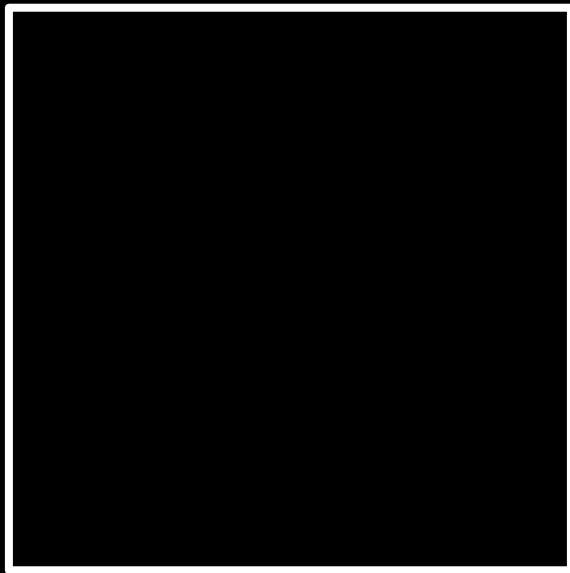






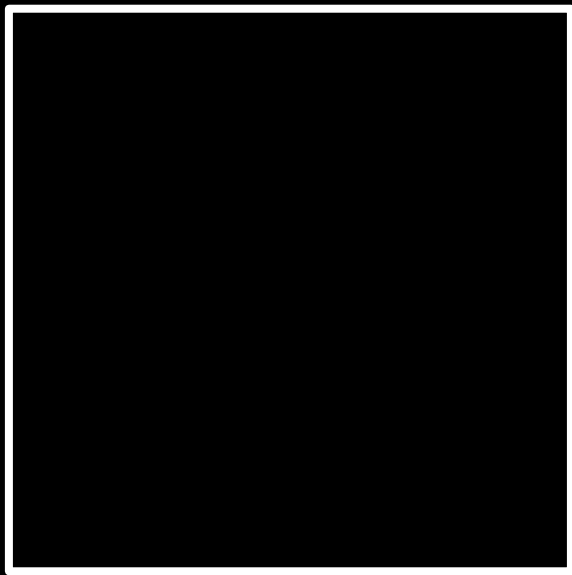
hash function

Albus

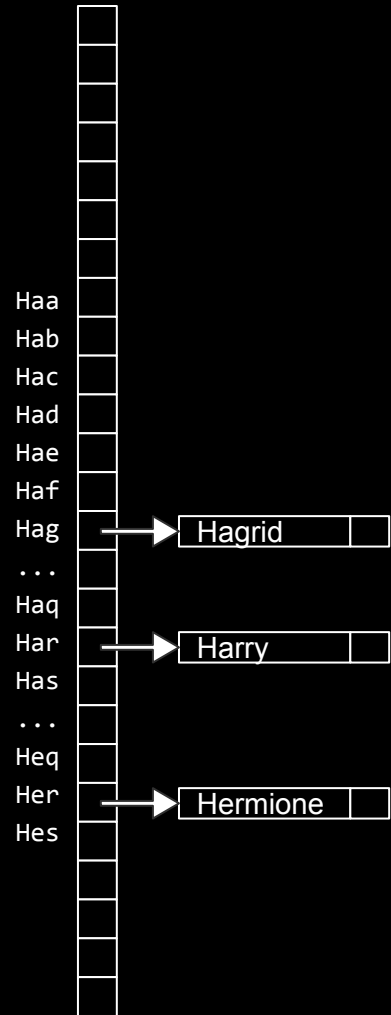


0

Zacharias →



→ 25



$$O(n^2)$$

$$O(n \log n)$$

$$O(n)$$

$$O(\log n)$$

$$O(1)$$

$O(n^2)$

$O(n \log n)$

$O(n)$           search

$O(\log n)$

$O(1)$

$O(n^2)$

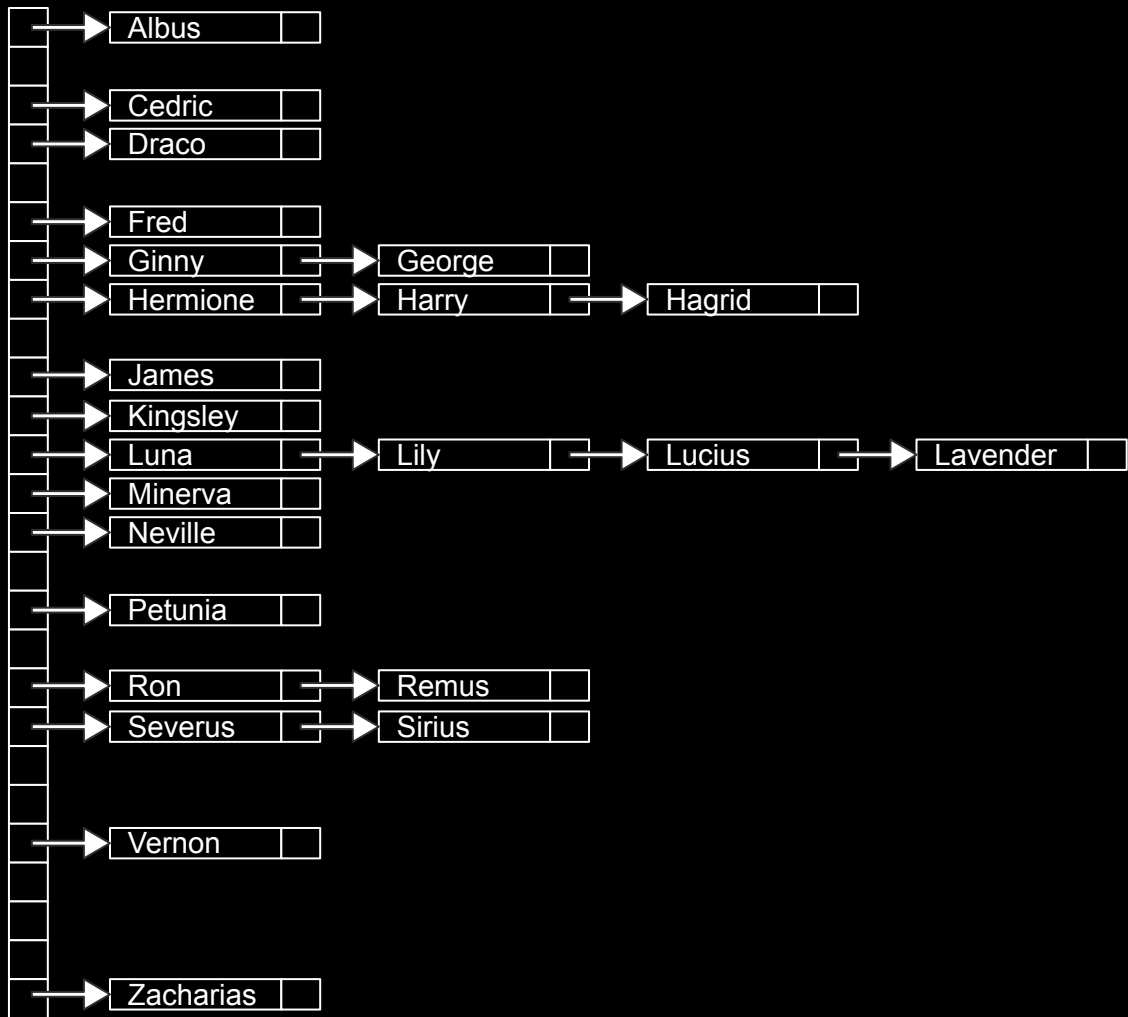
$O(n \log n)$

$O(n)$           search

$O(\log n)$

$O(1)$           insert





dictionaries

dict

list

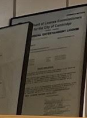
range

set

tuple

...

PICK ME UP



B

C

D

E

F

G

H

I

K

L

M



N

O

P

Q

R

T

U-

V

W

X

Y

Z



queues

stacks



# Lab 0



# Assignment 2

Office Hours

# CS50 for JDs

Algorithms, Data Structures